

Experimental design and response surface methodology applied to the dielectric properties of hydroalcoholic solutions containing sodium chloride

Planejamento de experimentos e metodologia de superfície de resposta, aplicados às propriedades dielétricas de soluções hidroalcoólicas com cloreto de sódio

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Abstract

The main focus of this study was to use an experimental design to and the response surface statistical technique to predict and optimize the dielectric properties of hydrated ethanol-sodium chloride blends. Several samples of these blends were prepared considering the following variables: hydrated ethyl alcohol concentration, sodium chloride concentration and temperature. The main dielectric properties of these blends, i.e., the dielectric constant, dielectric loss factor and dissipation factor, were measured in a calibrated device suitable for liquid or pasty substances. For this study, experimental tests were carried out according to a Central Composite Design (CCD). Response surface techniques were used to predict the magnitude of the effect of the input variables on the responses investigated, particularly on the dissipation factor. This factor represents the ability of the substance to convert electromagnetic energy into heat. Within the experimental range studied here, the values of the variables that optimized the response were as follows: sodium chloride concentration of 2.21%, hydrated ethanol concentration of 4.64% and temperature of 87 °C.

Keywords: *Ethanol; Dielectric properties; Microwave; Response surface.*

Resumo

O foco principal do trabalho desenvolvido foi utilizar o planejamento de experimentos e as técnicas estatísticas de superfície de resposta para prever e otimizar as propriedades dielétricas de misturas etanol hidratado-cloreto de sódio. Várias amostras dessas misturas foram preparadas, considerando-se as seguintes variáveis: concentração de álcool etílico hidratado, concentração de cloreto de sódio e temperatura. As principais propriedades dielétricas, como constante dielétrica, fator de perda dielétrica e fator de dissipação das misturas, foram medidas num equipamento calibrado, indicado para substâncias líquidas ou pastosas. Para este estudo, ensaios experimentais foram conduzidos, seguindo um Planejamento Composto Central (PPC). Técnicas de superfície de resposta foram utilizadas para prever a magnitude do efeito das variáveis de entrada nas respostas investigadas, particularmente no fator de dissipação. Tal fator representa a habilidade da substância em converter energia eletromagnética em calor. Considerando-se a faixa experimental estudada, os valores das variáveis que otimizaram a resposta foram os seguintes: concentração de cloreto de sódio de 2,21%, concentração de etanol hidratado de 4,64% e temperatura de 87 °C.

Palavras-chave: *Etanol; Propriedades dielétricas; Microondas; Superfície de resposta.*



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1 Introduction

The productive capacity and sustainable development of the Brazilian sugar and ethanol industry have aroused strong interest worldwide, since this is the first economy that has achieved the sustainable use of biofuels.

These days, sugarcane alcohol is recognized worldwide for its environmental and socioeconomic advantages, and first world countries are interested in this technology. In Brazil, the sugarcane supply chain employs more than four million people in direct and indirect jobs, generating more than R\$ 41 billion per year in the sector (BICALHO *et al.*, 2012).

Brito (2003) stated that the Brazilian sugarcane sector may become the main global fuel alcohol supplier as well as using modern technologies to set up distilleries in other countries. Thus the growing demand for ethanol and the increasing competitiveness of the current world market are driving researchers and companies operating in the sector to seek high productivity processes allied to lower operating costs, e.g., energy consumption during the heating of the fermented sugarcane juice in the distillation operation. Experts have warned that efficiency gains in commodity production are predominant factors for competitiveness on world markets (BICALHO *et al.*, 2012).

In the conventional processes used by most Brazilian distilleries, sugarcane juice is heated in tubular heat exchangers (reboilers), using water vapour to provide the energy needed for partial vaporization.

Microwave heating has made advances in recent years and the number of relevant industrial applications has increased, particularly in the food sector. Interest in this type of heating has increased, to a great extent due to the energy crisis, but also due to greater familiarization with and wider acceptance of this technology (ZHANG *et al.*, 2006).

Knowledge about dielectric properties such as the dielectric constant (ϵ') and the dielectric loss factor (ϵ''), as well as their relationships in liquid substances, is essential in order to determine the amount of electromagnetic energy needed for the dielectric heating of compounds (PROSETYA; DATTA, 1991).

Dielectric materials have low conduction current when a given external electric field is applied. Thus, the molecules and atoms of these materials present a dipole movement that creates friction, dissipating energy in the form of heat (PEYRE *et al.*, 1997). Dielectric properties, which vary with the frequency applied, play an important role in the efficient heating of these substances. However, it is difficult to predict heat transfer in microwave heating, due to the nonlinear variations in the properties of materials as a function of temperature and composition, as was noted by Campañone and Zaritzky (2005) and Koskiniemi *et al.* (2011).

These variations may cause thermal instabilities, which are known as hot spots (AHMED *et al.*, 2007).

Earlier studies, for instance that of Chen and Zhao (2007), reported values for the (ϵ') and (ϵ'') of pure ethanol and water. However, these properties need to be determined for blend of these substances, since this information is important for their microwave heating.

Gadani *et al.* (2012) attributed significant improvements in the dielectric properties of water to the addition of salts. Their results indicated that the highest conversion of electromagnetic energy into heat was achieved by increasing the concentration of sodium chloride in aqueous solutions.

Electromagnetic energy is transformed into heat by microwaves via two main mechanisms: dipole rotation and ionic conduction. The first mechanism involves the alignment of the molecules with the electric field applied. In the second mechanism, the heat produced is due to friction losses that occur due to the migration of dissolved ions under the action of an electromagnetic field (electromigration) (KOSKINIEMI *et al.*, 2013).

Microwave heating is one of the most interesting methods for heating materials with favourable dielectric characteristics. Unlike other heat sources, which involve the application of heat externally to the surface of a material, microwave irradiation heats the entire volume of the material (GEEDIPALLI *et al.*, 2007).

This type of heating offers several advantages over conventional methods, such as minimization of the heating time and a uniform distribution of temperature in the material (OLIVEIRA; FRANCA, 2002).

Sun *et al.* (2007) reported that these characteristics can provide improvements in the quality of products in various industrial fields, e.g., sterilization of materials, sewage treatment, pyrolysis (carbonization), drying, pasteurization, etc.

Authors such as Metaxas and Meredith (1993), Meredith (1998), Yin (2012), Maskan (2000) and Drouzas and Schubert (1996) carried out experimental studies involving microwave technology to process a variety of materials, such as juice pasteurization, drying processes, sample preparation, etc.

The U.S. Federal Communications Commission (FCC) defined the frequencies of 0.915 GHz and 2.45 GHz for the purpose of industrial microwave heating. However, the frequency bandwidth of from 0.9 to 18 GHz is already used by some microwave heating systems (BOOTY; KRIEGSMANN, 1994).

This work involved a study of the variation in the dielectric properties of hydrated ethanol-sodium chloride blends at a frequency of 2.45 GHz, aiming to select the best microwave heating conditions for these blends. To this

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end, the Design of Experiments (DOE) and Response Surface Methodology were used.

The independent variables analysed were: the salt (NaCl) concentration – C_{NaCl} , the ethanol (C_2H_5OH) concentration – C_{EtOH} and the temperature of the blend – T , while the dependent variables were: the dielectric constant (ϵ'), the dielectric loss factor (ϵ'') and the dissipation factor ($\tan\delta = \epsilon''/\epsilon'$).

2 Dielectric properties

Let us consider two parallel metal plates placed at a fixed distance from each other in a vacuum. There will be a capacitance between them but if one fills the vacuum with some sort of material, the capacitance will change to a new value.

The relationship between the two aforementioned capacitances is called the permittivity of the material (k), and is given by the Debye equation (Equation 1):

$$k = \frac{\epsilon}{\epsilon_0} = \epsilon' - i\epsilon'' \quad (1)$$

where: ϵ' is the real part, ϵ'' is the imaginary part, and $\epsilon_0 = \frac{1}{36\pi} \times 10^{-9}$ F/m to $i = \sqrt{-1}$.

The separation of the real and imaginary parts in Debye's equation allows one to establish the following expressions for the dielectric constants: ϵ' and ϵ'' Equations 2 and 3. These constants are dependent on the frequency of radiation (ω) and the viscosity of the continuous medium and temperature during the relaxation time (τ).

$$\epsilon' = \epsilon_\infty + \frac{(\epsilon_s - \epsilon_\infty)}{(1 + \omega^2\tau^2)} \quad (2)$$

$$\epsilon'' = \frac{(\epsilon_s - \epsilon_\infty)\omega\tau}{(1 + \omega^2\tau^2)} \quad (3)$$

where: ϵ_∞ and ϵ_s are, respectively, the permittivities of the material at very high ($\gg \tau^{-1}$) and extremely low ($\ll \tau^{-1}$) radiation frequencies, and τ is the relaxation time obtained by Debye, based on the Stokes-Einstein theorem (METAXAS; MEREDITH, 1993).

The dielectric loss factor (ϵ'') measures the efficiency of the conversion of electromagnetic energy into heat.

The dielectric constant (ϵ') of a substance is a measure of its degree of polarity. The higher the dielectric constant of a material the more energy can be stored in it (ZHU et al., 2007).

The ϵ''/ϵ' ratio, which is numerically equal to $\tan\delta$ and is called the dissipation factor, indicates the ability of a sample to convert electromagnetic radiation into heat. According to Kingston and Haswell (1997), the higher the value of this factor the greater the ability of a substance to be heated by microwaves.

The dielectric constant (ϵ') is associated with the capacity of the material to store electric energy (in a vacuum $\epsilon'=1$), while the dielectric loss factor (ϵ'') is related to the dissipation of electric energy due to different mechanisms. The dielectric properties describe the ability of a material to absorb, transmit and reflect electromagnetic energy. Foods are neither good electrical insulators nor good electrical conductors; and can therefore be categorized as 'lousy dielectric materials'. The dielectric properties of foods have the ability to drive the influential interaction between the food components and the electric field, and can be influenced by many factors such as temperature, moisture content, salt content, microwave frequency and other ingredients. The microwave heating mechanism is very complex and depends on numerous factors i.e. the propagation of microwaves governed by Maxwell's equations for electromagnetic waves, the interactions between the microwaves and the dielectric properties of the food, and the heat dissipation governed by heat and mass transfer (PULIGUNDLA et al., 2013)

According to Cha-Um et al. (2009), any material that can store energy when an external electric field is applied to it is a *dielectric* material.

Such materials resist the passage of electric current, but have the ability to absorb and store electric energy due to charge displacement (polarization) under the influence of an electric field.

The dielectric properties of materials are often temperature-dependent. Therefore, these properties should be known in a wide range of temperatures to allow for more accurate predictions of the dielectric heating behaviour.

Knowledge of the dielectric properties of materials is required in studies of the microwave heating of these materials, enabling one to select the best operational conditions, and hence, the best use of energy.

3 Material and methods

3.1 Dielectric properties

First the hydrated ethanol and sodium chloride solutions were prepared at concentrations of C_{NaCl} (0.19, 0.6, 1.2, 1.8 and 2.21% w/w) and C_{EtOH} (4.64, 6, 8, 10 and 11.36% w/w), as defined by the experimental design Table 1.

With the aid of an analytical balance, the samples were prepared using 99.9% ethanol (Merck®), NaCl. p.a. (Synth®) and deionized water, and the mixtures stored in

Table 1. The design variables and levels.

Coded variables	(- α)	-1	0	1	(α)
C_{NaCl}	0.19	0.60	1.20	1.80	2.21
C_{EtOH}	4.64	6.00	8.00	10.00	11.36
T	53.00	60.00	70.00	80.00	87.00

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150 mL containers. The concentrations were selected to match the operating conditions of industrial ethanol distillation.

The dielectric properties of the different hydrated ethanol and sodium chloride blends were determined in a frequency range from 10 MHz to 3.0 GHz, at temperatures of 53 °C, 60 °C, 70 °C, 80 °C and 87 °C Table 1, duly controlled in a thermostatic bath, as illustrated in Figure 1.

The materials used for determining the dielectric properties were: a Coaxial Probe, Transmission Line, Resonant Cavity and Parallel Plates. The coaxial probe method was chosen because it is non-destructive and is recommended for liquid or pasty samples. This method

is used to determine the real and imaginary parts of permittivity (k) and the loss tangent ($\tan \delta$).

3.2 Coaxial probe method

The coaxial probe method consists of determining the dielectric properties of a mixture using a network analyser set up for this purpose, specific software and the probe, as illustrated in Figure 2.

The probe shown in Figure 3 has a hermetic glass-to-metal seal which makes it resistant to corrosion and abrasive chemicals. It can withstand temperatures ranging from -40 °C to 200 °C and allows measurements to be taken as a function of frequency and of temperature.

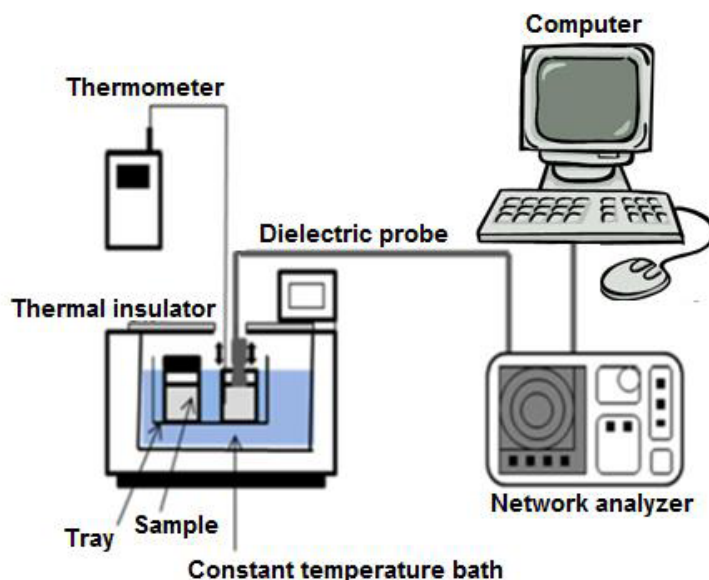


Figure 1. Schematic diagram of the system for determining the dielectric properties. Adapted from Tanaka et al. (2008).



Figure 2. Measuring system setup.

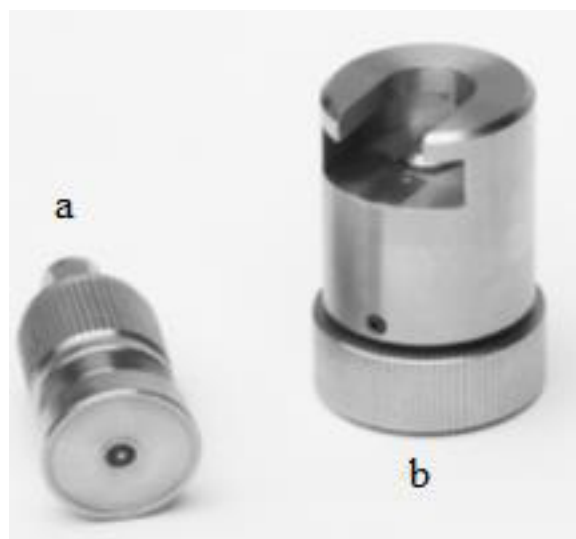


Figure 3. (a) Probe and (b) calibrator.

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The devices used were an Agilent 85070D dielectric probe kit, Agilent E5071C ENA network analyser and Agilent 85070E software.

Before taking the measurements the system was calibrated. This involved selecting the desired frequency range, using a sample of water at approximately 25 °C, and calibrating the system in a pre-selected sequence: testing in air; testing in short circuit, and testing in water.

After the calibration was completed, the dielectric constant of the water and alcohol, both of which were known, were tested for safety. Having confirmed these values it was then possible to measure the dielectric constant of the prepared blends.

3.3 Experimental design and response surface

To select the best operating values to obtain the dielectric properties using the microwave heating system and the cited variables, a Central Composite Design (CCD) was prepared, comprising a factorial design at five levels with three variables, three replicates at the centre point and six experiments at the axial points (α), giving a total of 17 experiments Table 2.

Each assay lasted for about 1 min after the temperature reached equilibrium, and ϵ'' , ϵ' and $\tan \delta$ were represented by the responses “y, y and y”, respectively. Optimization was only done at the frequency of 2.45 GHz, which is the one most widely used industrially.

A volume of 50 cm³ of solution was used in each assay.

The variables were coded according to Equations 4, 5 and 6. The following variables were selected:

x_1 , sodium chloride concentration (%) – C_{NaCl} ; x_2 , ethanol concentration (%) – C_{EtOH} , and x_3 , temperature (°C) – T.

$$x_1 = \frac{C_{NaCl} - 1.2}{0.6} \quad (4)$$

$$x_2 = \frac{C_{EtOH} - 8}{2} \quad (5)$$

$$x_3 = \frac{T - 70}{10} \quad (6)$$

Response Surface Methodology (RSM) comprises a combination of techniques for experimental designs, regression analysis and optimization methods and is very useful for product and process development, and also to improve existing products.

The model is built by means of a multiple regression analysis, which involves estimating the regression coefficients of the variables. The adoption of a complete quadratic regression model is recommended, as suggested by Equation 7.

$$Y = \beta_0 + \sum_i \beta_i X_i + \sum_i \beta_{ii} X_i^2 + \sum_{i=1}^n \sum_{j=1}^n \beta_{ij} X_i X_j \quad (7)$$

where: β_0 , β_i , β_{ii} and $\beta_{ij} = \beta_{ji}$ represent the coefficients of the polynomial and x_i , x_j are the experimental variables.

After building the model, the fit of the regression must be checked and a procedure that is commonly used for this is the Student's *t*-test and the analysis of variance, as described by Körbahti and Rauf (2008).

After adjusting the model, the next step is to optimize it.

In the case of a second-degree model, quadratic programming can be applied, as proposed by Ravikumar et al. (2005).

El Boulifi et al. (2010) and Montgomery (2001) stated that one way to locate the optimal point is to use the stationary point localization technique and the Central Composite Design (described above). The optimal point, if it really exists in the system under investigation, will be defined by the set of points (x_1, x_2, \dots, x_k) for which the partial derivatives are equal to zero, according to Equation 8.

$$\frac{\partial y}{\partial x_1} = \frac{\partial y}{\partial x_2} = \dots = \frac{\partial y}{\partial x_k} \quad (8)$$

This point, which is called the *stationary point*, may represent a maximum response point, a minimum point or a saddle point.

The general solution for the stationary point is obtained when the second-order calculation of Equation 7 is written in matrix notation, as shown in Equation 9,

$$y = \beta_0 + \mathbf{x}'\mathbf{b} + \mathbf{x}'\mathbf{B}\mathbf{x} \quad (9)$$

Table 2. The design matrix, showing the operating conditions of the 17 experiments.

Experiment	x_1 (%)	x_2 (%)	x_3 (°C)
1	0.60	6.00	60
2	1.80	6.00	60
3	0.60	10.00	60
4	1.80	10.00	60
5	0.60	6.00	80
6	1.80	6.00	80
7	0.60	10.00	80
8	1.80	10.00	80
9	0.19	8.00	70
10	2.21	8.00	70
11	1.20	4.64	70
12	1.20	11.36	70
13	1.20	8.00	53
14	1.20	8.00	87
15	1.20	8.00	70
16	1.20	8.00	70
17	1.20	8.00	70

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where:

$$\mathbf{x} = \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_k \end{bmatrix} \quad \mathbf{b} = \begin{bmatrix} \beta_1 \\ \beta_2 \\ \vdots \\ \beta_k \end{bmatrix} \quad \mathbf{B} = \begin{bmatrix} \beta_{11} & \beta_{12}/2 & \dots & \beta_{11}/2 \\ & \beta_{22} & \dots & \beta_{21}/2 \\ & & \dots & \vdots \\ & & & \beta_{kk} \end{bmatrix}$$

Thus it is possible to estimate the optimal levels of each of the input parameters that maximize or minimize the average response of the system.

4 Results and discussion

The influence of the variables: x_1 sodium chloride concentration (%) – C_{NaCl} ; x_2 , ethanol concentration (%) – C_{EtOH} , and x_3 , temperature (°C) – T on the dielectric properties ϵ'' , ϵ' and $\text{tg}\delta$ were studied according to a central composite design with three replicates at the centre, giving a total of 17 experiments.

The experimental results are shown in Table 3. Based on these results, the parameters of the regression models were estimated by applying Equation 7.

The experimental data were subjected to a multiple regression analysis to quantify the effect of the main variables as well as the effects of the interaction and quadratic contributions to the responses under study. A maximum probability of error of 10% was established in the test and hence the parameters with a significance level higher than 10% were ignored. The statistical analysis and mathematical processing were carried out with the aid of the STATISTICA 8 and MAPLE 9.5 software, respectively.

The accuracy of the experimental results was verified based on an evaluation of the results obtained at the central design level, where the differences between the responses were less than 0.5%.

Tables 4, 5 and 6 show the results obtained from applying multiple regressions to the responses obtained for ϵ' , ϵ'' and $\text{tg}\delta$. A comparison of the p levels observed and the p level stipulated by the significance of 10% indicates

Table 3. Experimental results.

x_1	x_2	x_3	$y_1 \epsilon''$	$y_2 \epsilon'$	$y_3 \text{tg}\delta$
-1	-1	-1	65.7843	25.7205	2.5577
1	-1	-1	62.7598	16.5267	3.7975
-1	1	-1	63.043	21.9390	2.8736
1	1	-1	61.1245	18.0666	3.3833
-1	-1	1	64.2749	27.7580	2.3155
1	-1	1	60.2523	15.0664	3.9991
-1	1	1	59.9301	22.3730	2.6787
1	1	1	58.5546	14.1140	4.1487
-1.682	0	0	63.084	27.6120	2.2847
1.682	0	0	59.8527	18.3052	3.2697
0	-1.682	0	65.0083	29.1054	2.2336
0	1.682	0	60.2302	26.0313	2.3137
0	0	-1.682	63.6284	21.4045	2.9727
0	0	1.682	59.4921	14.9332	3.9839
0	0	0	61.299	25.6367	2.3911
0	0	0	61.301	25.6363	2.3912
0	0	0	61.298	25.6359	2.3911

Table 4. Multiple regression analysis for $y_1 (\epsilon'')$.

Coefficients	Error	t (10)	P	
β_0	61.4671	0.0977	629.00	2.54E-24
β_1	-1.1551	0.0803	-14.38	5.25E-08
β_2	-1.3513	0.0803	-16.82	1.16E-08
β_3	-1.2196	0.0803	-15.18	3.11E-08
β_{22}	0.4376	0.0822	5.32	3.37E-04
β_{12}	0.4691	0.1050	4.47	1.20E-03
β_{23}	-0.2082	0.1050	-1.98	7.54E-02
Level of significance (α) 0.10				

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Table 5. Multiple regression analysis for y2 (ϵ').

Coefficients	Error	t (13)	P	
β_0	25.9524	1.1114	23.35	5.34E-12
β_1	-3.6367	0.6952	-5.23	1.62E-04
β_{11}	-1.5450	0.7309	-2.11	5.44E-02
β_{33}	-3.2380	0.7309	-4.43	6.79E-04
Level of significance (α) 0.10				

Table 6. Multiple regression analysis for y3 ($tg\delta$).

Coefficients	Error	t (13)	P	
β_0	2.4146	0.1588	15.21	1.16E-09
β_1	0.4803	0.0993	4.84	3.25E-04
β_{11}	0.2033	0.1044	1.95	7.35E-02
β_{33}	0.4511	0.1044	4.32	8.31E-04
Level of significance (α) 0.10				

that, for the response y (ϵ'') only x_1, x_2, x_3, x_2^2 and $x_1 \cdot x_2$ were significant. For the response y (ϵ') only x_1, x_1^2 and x_3^2 were significant, and for the response y ($tg\delta$) only x_1, x_1^2 and x_3^2 were significant.

Thus one can establish equations or models for the ϵ', ϵ'' and $tg\delta$ responses which are represented, respectively, by Equations 10, 11 and 12 for the response surface analysis. It should be noted that these equations contain only the variables and interactions that significantly influenced the response.

$$\epsilon'' = 61.4671 - 1.155 \cdot x_1 - 1.3513 \cdot x_2 - 1.2196 \cdot x_3 + 0.4376 \cdot x_2^2 + 0.4691 \cdot x_1 \cdot x_2 - 0.2082 \cdot x_2 \cdot x_3 \quad (10)$$

$$\epsilon' = 25.9524 - 3.6367 \cdot x_1 - 1.5450 \cdot x_1^2 - 3.2380 \cdot x_3^2 \quad (11)$$

$$tg\delta = 2.4146 + 0.4803 \cdot x_1 + 0.2033 \cdot x_1^2 + 0.4511 \cdot x_3^2 \quad (12)$$

An analysis of the residuals indicated that they followed a normal distribution and were distributed independently with constant variance, as can be seen from the random dispersions in Figures 4, 5 and 6.

The relationships between the predicted and observed dependent variables are shown in Figures 7, 8 and 9. The observed values were measured experimentally and the predicted values were evaluated from the equations generated using function approximation, Equations 10, 11 and 12.

According to the fitted models, the values obtained for the correlation coefficients for the responses of ϵ'', ϵ' and $tg\delta$ were 0.9872, 0.7878 and 0.7680, respectively.

The effects of two independent variables and their interactions in the responses can be seen by analysing the response surfaces in Figures 10 to 18, which were built from Equations 10, 11 and 12, considering the third variable at its central point.

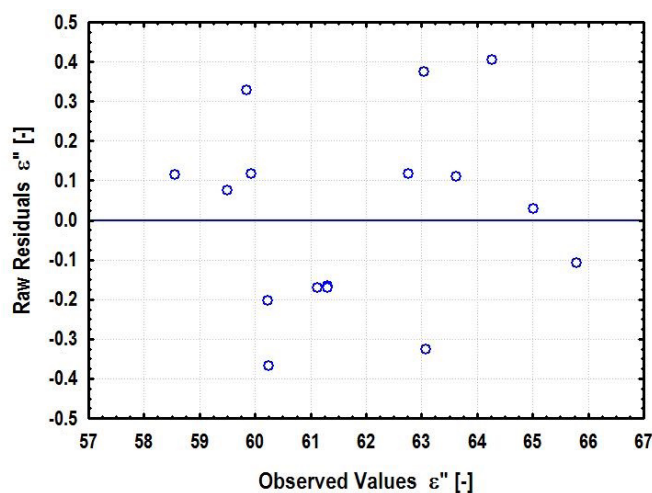


Figure 4. Graph of residuals for y_1 (ϵ'').

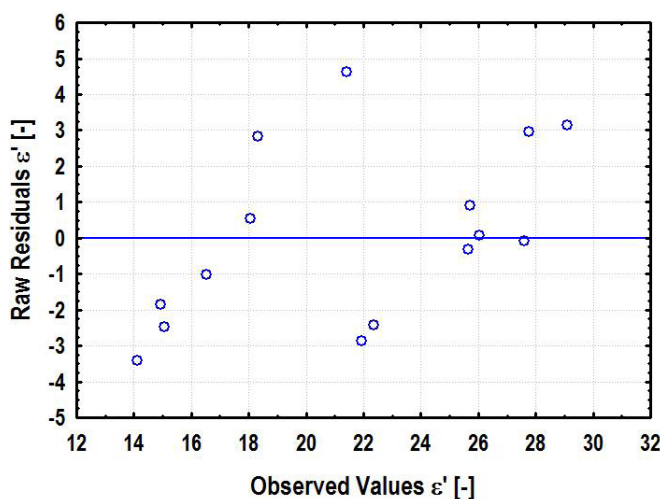


Figure 5. Graph of residuals for y_2 (ϵ').

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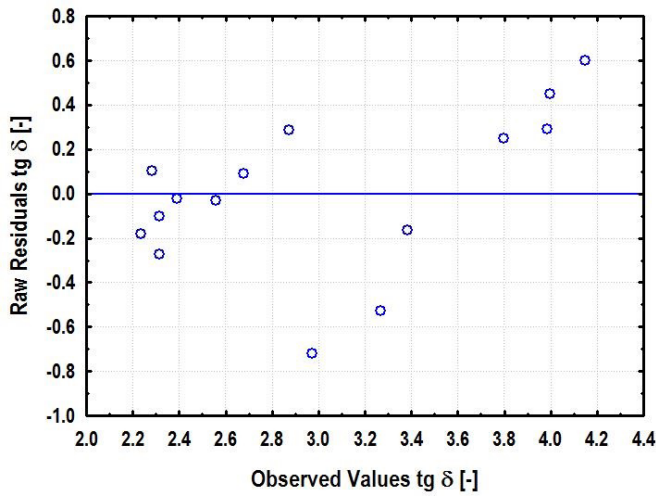


Figure 6. Graph of residuals for y_3 ($tg\delta$).

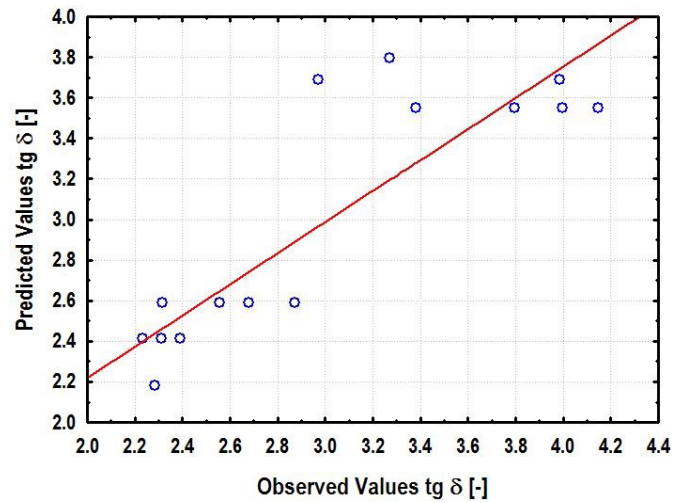


Figure 9. Estimated vs. observed values for y_3 ($tg\delta$).

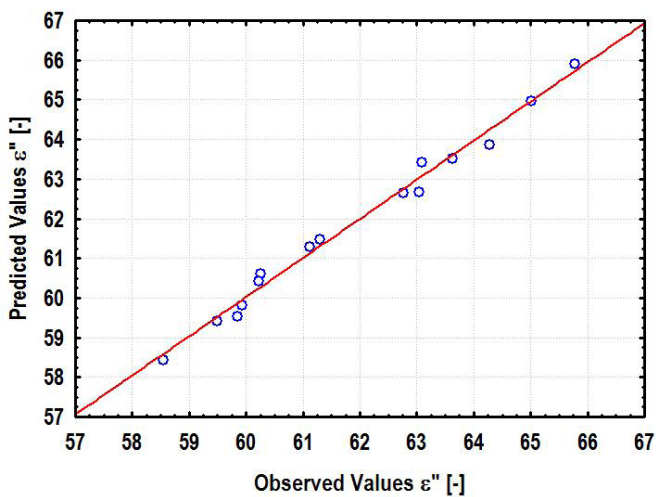


Figure 7. Estimated vs. observed values for y_1 (ϵ'').

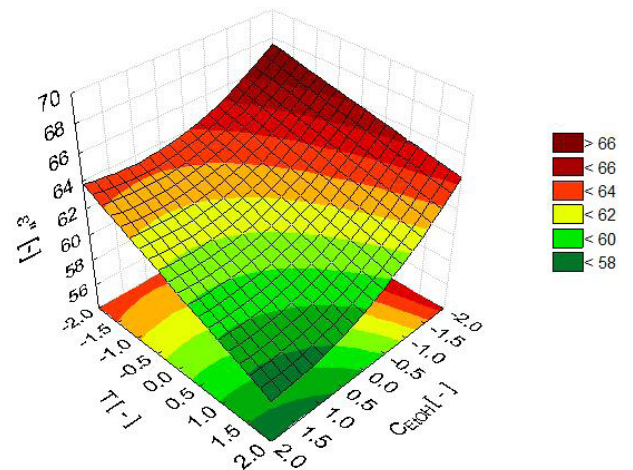


Figure 10. Response surface for $y_1 - \epsilon''$ [-] with fixed $C_{NaCl} x$ [-].

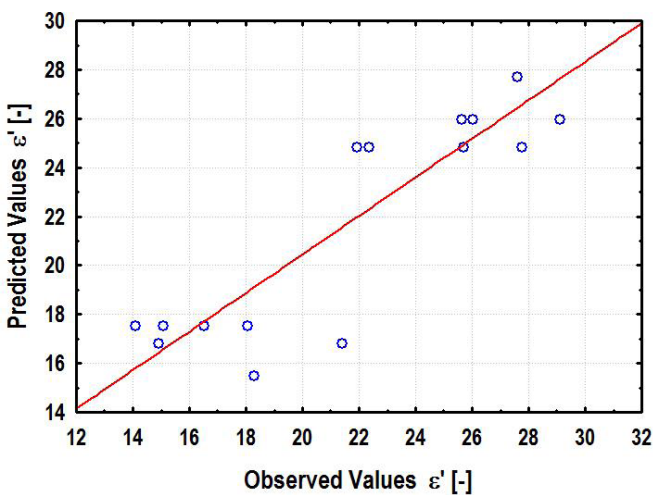


Figure 8. Estimated vs. observed values for y_2 (ϵ').

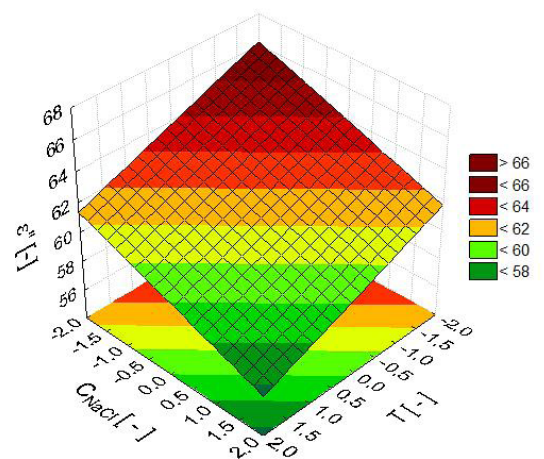


Figure 11. Response surface for y_1 (ϵ'') with fixed $C_{EtOH} x$ [-].

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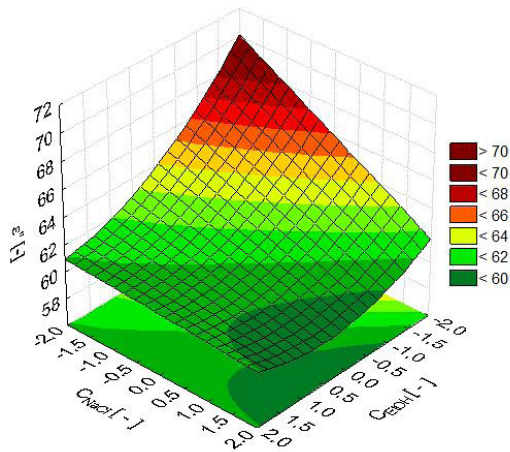


Figure 12. Response surface for $y_1 - \epsilon'' [-]$ with fixed $x T [-]$.

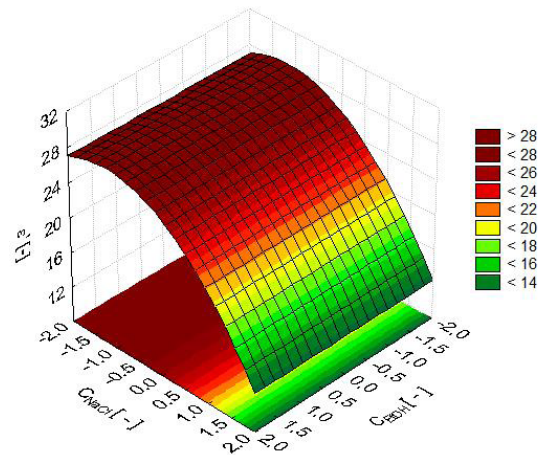


Figure 15. Response surface for $y_2 - \epsilon' [-]$ with fixed $T x [-]$.

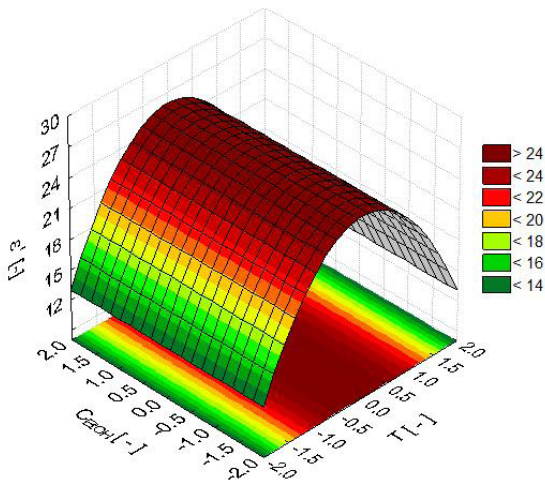


Figure 13. Response surface for $y_2 - \epsilon' [-]$ with fixed $C_{NaCl} x [-]$.

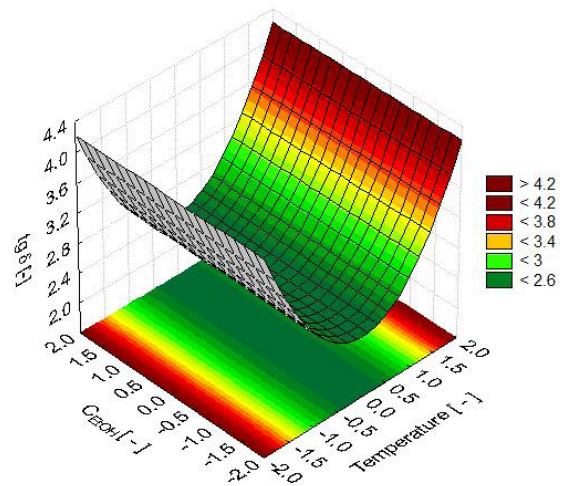


Figure 16. Response surface for $y_3 - tg\delta [-]$ with fixed $C_{NaCl} x [-]$.

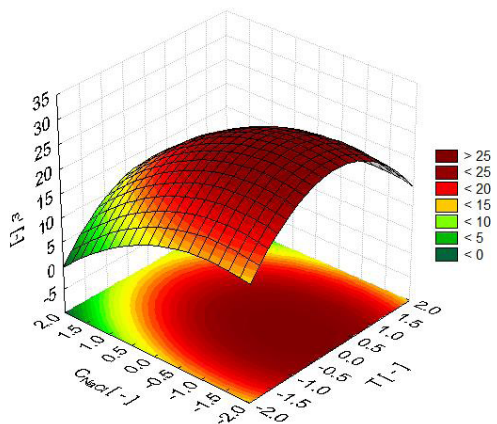


Figure 14. Response surface for $y_2 - \epsilon' [-]$ with fixed $C_{EtOH} x [-]$.

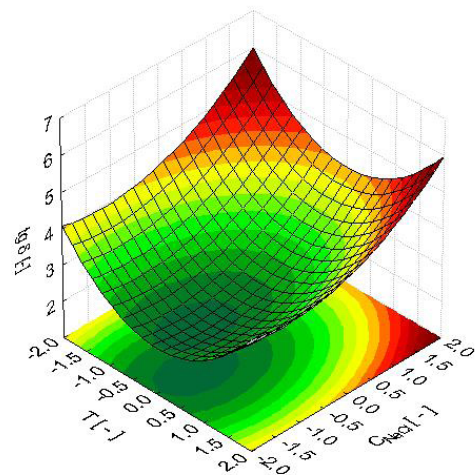


Figure 17. Response surface for $y_3 - tg\delta [-]$ with fixed $C_{EtOH} x [-]$.

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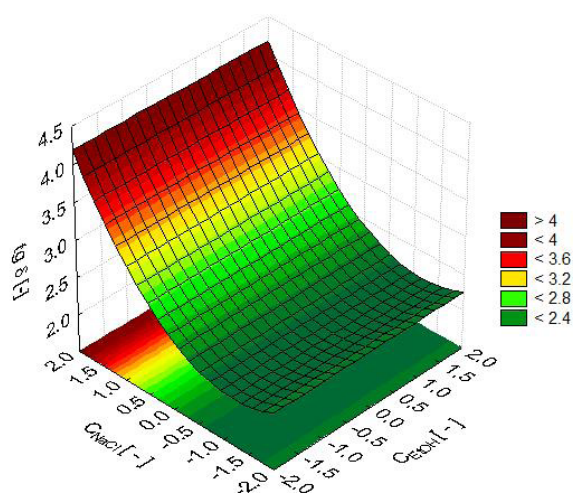


Figure 18. Response surface for $y_3 - \text{tg}\delta$ [-] with fixed T X [-].

An evaluation of the surfaces shown above revealed that all the responses were influenced by the NaCl concentration (x) and the temperature (x). On analysing the concentration of EtOH (x), it can be seen that this variable did not influence ϵ' (y) or $\text{tg}\delta$ (y), but for ϵ'' (y), the EtOH concentration was the variable that most influenced the response. These findings are consistent with the p significance levels presented in Tables 4, 5 and 6.

The variables that most affected the ϵ' (y) and $\text{tg}\delta$ (y) responses were the NaCl concentration (x) in the linear form and the operating temperature (x) in the quadratic form.

Considering the experimental range investigated, the optimum point for dielectric heating was determined by means of a canonical analysis of the model fitted by the y function. The y function is related to the other responses (y_1 and y_2), because this variable represents the ability of the substance to convert electromagnetic energy into heat.

The Maple 9.5 software was used to determine the operating conditions that would maximize the y_3 ($\text{tg}\delta$) response, and an analysis of Equation 12 indicated their optimal values, i.e., $C_{\text{NaCl}} = 2.21\%$; $C_{\text{EtOH}} = 4.64\%$ and $T = 87^\circ\text{C}$.

5 Conclusions

The results of this study indicated that the variables that most strongly influenced the responses of dielectric constant (ϵ') and dissipation factor ($\text{tg}\delta$) were the sodium chloride concentration, followed by the temperature of the blend. The variable that most influenced the response of dielectric loss factor (ϵ'') was the ethanol concentration. The variable that exerted the least influence on the responses ϵ' and $\text{tg}\delta$ was also found to be the ethanol concentration.

The dielectric properties of an ethanol solution undergo significant changes in response, for example, to variations in the NaCl concentration and in the temperature.

This indicates that such variations exert an influence during the microwave heating of these mixtures, a finding that is consistent with other studies published in the literature and cited in this paper.

In this study, we also found that, within the interval of ethanol concentrations investigated, the properties that define the ability of the material to convert electromagnetic energy into heat were not affected by microwave heating.

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