

Meson Loops and the $g_{D^*D\pi}$ Coupling

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The $D^*D\pi$ form factor is evaluated at low and moderate Q^2 in a hadronic loop model, for off-shell D mesons. The results contain arbitrary constants, which are fixed so as to match a previous QCD sum rule calculation valid at higher Q^2 . The form factor obtained in this way is used to extract the coupling constant, which is in very good agreement with the experimental value.

Keywords: Effective Lagrangian; Chiral symmetry; Hadronic loop model; Heavy form factor; QCD sum rule

I. INTRODUCTION

The measurement of the $D^*D\pi$ coupling, made by the CLEO collaboration [1], yielding the result $g_{D^*D\pi} = 17.9 \pm 0.3 \pm 1.9$, created embarrassment in the community of QCD sum rules (QCDSR) which, by means of various schemes, had predicted much smaller values. Several different approaches of QCDSR were employed: two point function combined with soft pion techniques [2, 3], light cone sum rules (LCSR) [4, 5], light cone sum rules including perturbative corrections [6], sum rules in an external field [7], double momentum sum rules [8] and double Borel sum rules [9]. The LCSR prediction made in ref. [4] became even smaller after the radiative corrections have been included [6]. The upper limit of these predictions was $g_{D^*D\pi} = 13.5$ [6] and it turned out to be 30% lower than the central value of the CLEO measurement.

Although the QCD sum rule approach certainly suffers from large uncertainties, in several other cases good agreements with experiment were obtained. Therefore, we cannot simply be skeptical about the whole sum rule approach. The $g_{D^*D\pi}$ coupling constant does not seem, a priori, to be particularly exotic and other theoretical approaches did not produce such large discrepancies for this quantity. A careful discussion meant to reduce the uncertainties presented by quark models, performed in the framework of Dirac equation [10], and prior to the experimental measurement, has led to the result $g_{D^*D\pi} \simeq 18$. It should be stressed that this result has been obtained in the heavy quark limit. The recent (quenched) lattice QCD calculation has produced $g_{D^*D\pi} = 18.8 \pm 2.3_{-2.0}^{+1.1}$ [11]. It is therefore important to understand the specific difficulty which the standard sum rule approach seems to encounter in this case.

After the appearance of experimental data, three works [12–14] tried to reconcile the LCSR estimates with the measured figure. In [12], it was noted that the inclusion of an explicit radial excitation contribution to the hadronic side of the LCSR (often referred to as the left hand side of the sum rule) could significantly improve the value of $g_{D^*D\pi}$ and, at the same time, the stability of the sum rule with respect to the Borel parameter M^2 .

In the standard QCDSR approach of [9], a modification in the continuum contribution (such as the explicit inclusion of a radial excitation) does not seem to be neither necessary nor

promising, because there the Borel suppression is much more effective. In ref. [9] the $g_{D^*D\pi}(Q^2)$ form factor was estimated as a function of the off-shell pion momentum Q^2 . Since the sum rule obtained from the three-point function adopted is not valid at $Q^2 = 0$, in order to determine the $D^*D\pi$ coupling, it was necessary to extrapolate the Q^2 behaviour of the form factor. Of course there are large uncertainties in this procedure, and, the value of $g_{D^*D\pi} = 5.7 \pm 0.4$ obtained was much smaller than the experimental result. In a subsequent calculation of the $DD\rho$ vertex [15], the $DD\rho$ form factor was calculated for both D and ρ off-shell mesons and the QCDSR results were parameterized by analytical forms such that the respective extrapolations to the D and ρ poles provided consistent values for the $g_{DD\rho}$ coupling constant. This method of double parameterization plus matching at the on-shell point was then employed in [16] to recalculate the $D^*D\pi$ coupling and led to the value

$$g_{D^*D\pi} = 14.0 \pm 1.5. \quad (1)$$

While this number is much closer to the experimental value, there is still a discrepancy. Moreover, the procedure of fitting the QCDSR points in the deep euclidian region and extrapolating them to the time-like region still contains uncertainties, such as, for example *the analytical form chosen for the parameterizations*, i.e., monopole, exponential or gaussian.

In the present work we return to this question and employ hadronic loops, calculated by means of effective field theories (EFT), in order to produce a better parameterization for $D^*D\pi$ results derived by means of QCDSR. Purely hadronic calculations are independent from QCDSR and involve the choice of an effective Lagrangian, including the possible requirements of chiral symmetry and/or $SU(4)$. However, beyond tree level, one has to deal with the problems and uncertainties associated with renormalization. As we discuss in the sequence, a suitable combination of EFT and QCDSR results allows the elimination of undesired indeterminacies of both approaches, improving significantly their predictive powers. Effective interactions are discussed in section II, whereas results and conclusions are presented in sects. IV and V. As an straightforward exercise we also make a prediction for $g_{B^*B\pi}$.

II. EFFECTIVE DYNAMICS

The full $D^*D\pi$ vertex function is shown in Fig. 1. Leading contributions to this vertex when the external particles are not too off-shell come from both the tree interaction and the three classes of diagrams depicted in Figs. 2, 3 and 4. Meson loops are a necessary consequence of quantum field theory and do contribute to several hadronic observables. In practice, due to problems associated with infinities, renormalization becomes unavoidable in the evaluation of loop corrections to observables. Nowadays, this kind of procedure is rather well established at the hadronic level, in processes such as pion-pion and pion-nucleon scatterings. In the case of D mesons, on the other hand, the theory is much less developed and hence we resort to an alternative. The basic idea is to isolate the unknown loop parameters into some basic constants, in such a way that they can be determined by matching the results of loop and QCDSR results.

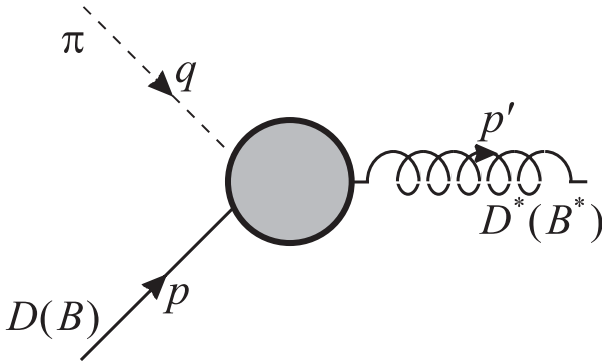


FIG. 1: The full $D^*D\pi$ ($B^*B\pi$) form factor.

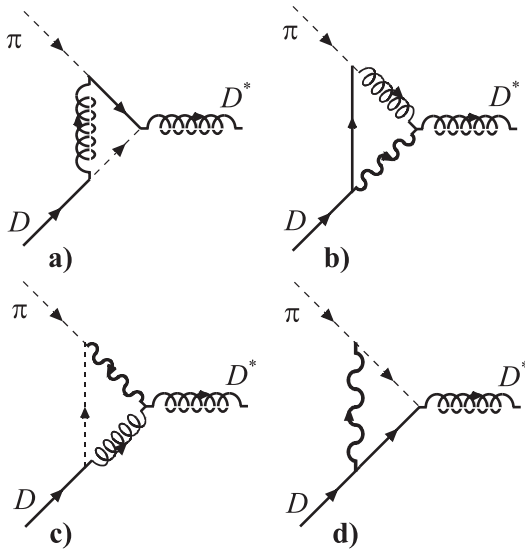


FIG. 2: Meson loop contributions to the $D^*D\pi$ form factor: “triangle” diagrams.

Before proceeding, some remarks are in order. We first note

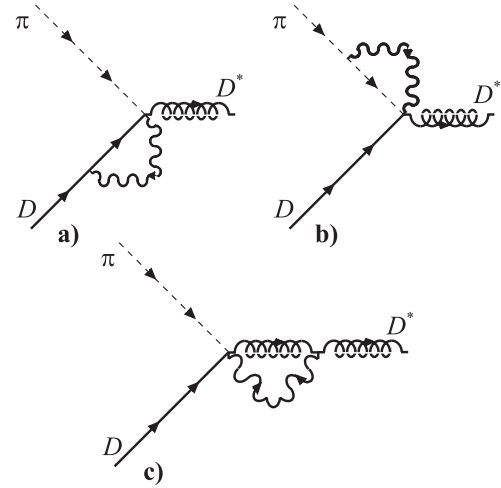


FIG. 3: Meson loop contributions to the $D^*D\pi$ form factor: “quartic couplings”.

that some diagrams, such as, for instance, that in Fig. 2a, contain internal vertices involving the $D^*D\pi$ coupling. In general, a full calculation is self consistent, since one uses the $D^*D\pi$ form factor in order to calculate the $D^*D\pi$ form factor. On the other hand, in the framework of perturbation theory, there are differences between the internal particles and the external ones. The former are always virtual, whereas the latter may be either real or put on mass shell in the extraction of the coupling constant.

In perturbation at leading order, internal particles are treated as elementary, without structure. They are assumed to be point-like and the evaluation of leading terms does not require the use of internal form factors. Consistently, one must use bare coupling constants for these interactions.

Nevertheless, our results do not depend on the values of these constants, since they are absorbed into the renormalization constants.

There are heavy mesons circulating in the loops shown in Figs. 2-4 and one might be tempted to argue that other states should also be included. We do have, for example, fermion-antifermion components such as $\bar{N}N$ or $\bar{\Lambda}_c\Lambda_c$ in the loops. An incoming positive pion can split into a p plus a \bar{n} , and so on. However, in a different context [17], it has been shown that this kind of splitting is suppressed with respect to the pion \rightarrow meson-meson splitting, by one order of magnitude. The neglect of this kind of contribution seems therefore justified. The same holds for the possibility of strangeness circulating in the loop, by means of the excitation of a $s\bar{s}$ pair from the sea. As this pair is heavy, the hadronic loops would involve correspondingly heavier virtual states such as D_s , D_s^* , K and K^* , which would also be suppressed, due to their high masses.

Moreover, in the QCDSR analysis of the $D^*D\pi$ vertex the strange quarks appear only as α_s^2 corrections or in terms proportional to the square of the gluon condensate and can therefore be safely neglected. If the hadron loop and QCD approaches to the problem are supposed to have the same physical content, it seems appropriate to neglect the strange meson

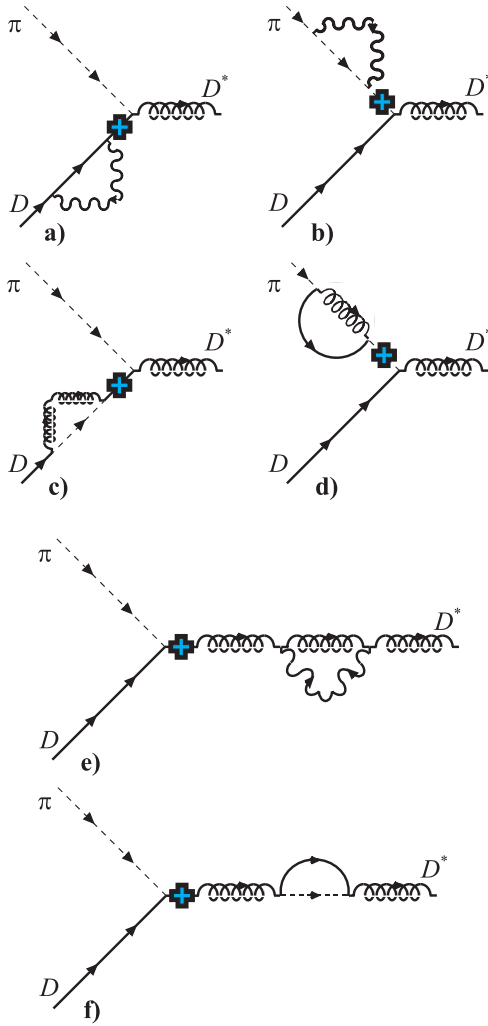


FIG. 4: Meson loop contributions to the $D^*D\pi$ form factor: “self energies”.

loops and baryon loops as well. Using only π 's, ρ 's, D 's and D^* 's we do cover properly the low Q^2 regions of the form factor. Thus it is enough to our purposes to work with a simple effective theory, involving only π 's, ρ 's, D 's and D^* 's that, as has been discussed elsewhere, [18], has proven to be phenomenologically successful. The same happens in this work.

The diagrams considered in this calculation have been divided into three classes. The first one, represented in Fig. 2, involves only triangular loops. The processes in Fig. 3, on the other hand, contain bubble-type loops and four-leg vertices associated with the gauge structure of ρ interactions. Finally, diagrams given in Fig. 4 involve bubble loops as well as single-particle propagators. This last feature might suggest that these interactions should be considered as mass corrections. However, the nature of the effective interactions described below is such that, in some terms, contributions of the form $[A + B(p^2 - m^2)]/(p^2 - m^2)$ arise. Whenever this happens, the factors proportional to B do correspond to proper three-point functions and are kept in the evaluation of the form factor. This kind of pole cancellations are indicated by crosses

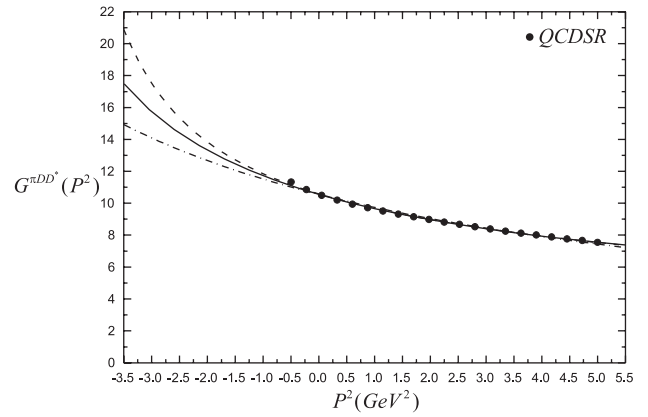


FIG. 5: The $D^*D\pi$ form factor. Dots: QCDSR from [16]; solid, dash and dash-dotted lines are fits obtained with eq. (12), (18) and (19), respectively.

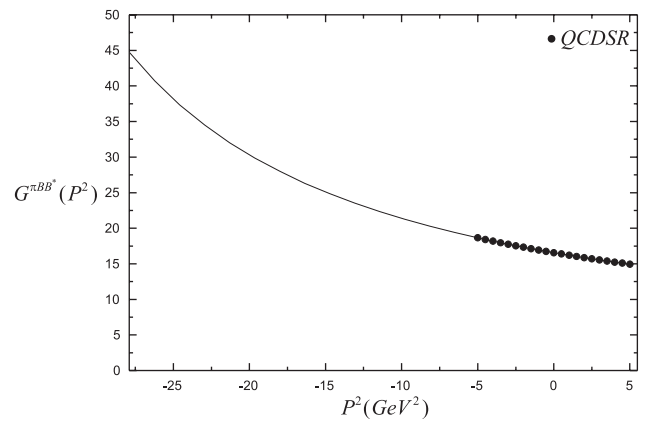


FIG. 6: The same as Fig. 5 for the $B^*B\pi$ form factor.

in Fig. 4.

Leading effects are described by an effective Lagrangian constrained by $SU(2)$ flavor and chiral symmetries, as well as gauge invariance. The πDD^* interaction is given by [18–21]

$$\mathcal{L}_{\pi DD^*} = i \hat{g}_{\pi DD^*} [\bar{D} \tau_a D^*_{\mu} - \bar{D}^*_{\mu} \tau_a D] \partial^{\mu} \phi_a . \quad (2)$$

where τ_a are the Pauli matrices, ϕ_a denotes the pion isospin triplet, while $D \equiv (D^0, D^+)$ and $D^* \equiv (D^{*0}, D^{*+})$ represent the pseudoscalar and vector charm meson doublets, respectively. The *hat* on top of the coupling constant indicates its bare nature.

The ρ couplings are assumed to be universal and are implemented by covariant derivatives of the form

$$\mathcal{D}^{\mu} = \partial^{\mu} - i \hat{g}_{\rho} T \cdot \rho^{\mu} , \quad (3)$$

where \hat{g}_{ρ} is the universal coupling constant and T is the isospin matrix suited to the field \mathcal{D}^{μ} it is acting upon. In this work we need

Using this prescription in eq. (2), we obtain

$$\mathcal{D}^\mu D = \left[\partial^\mu - i \hat{g}_\rho \frac{\tau}{2} \cdot \rho^\mu \right] D, \quad (4)$$

$$\mathcal{D}^\mu \bar{D} = \bar{D} \left[\partial^\mu + i \hat{g}_\rho \frac{\tau}{2} \cdot \rho^\mu \right], \quad (5)$$

$$\mathcal{D}^\mu \phi_a = \left[\partial^\mu + \hat{g}_\rho \varepsilon_{abc} \rho_b^\mu \right] \phi_c. \quad (6)$$

$$\mathcal{L}_{\rho\pi DD^*} = i \hat{g}_\rho \hat{g}_{\pi DD^*} \left[\bar{D} \tau_b D_\mu^* - \bar{D}_\mu^* \tau_b D \right] \varepsilon_{bca} \rho_c^\mu \phi_a. \quad (7)$$

For the other couplings, we depart from the free Lagrangians and have

$$\mathcal{L}_{\pi\pi} = \frac{1}{2} \partial_\mu \phi_a \partial^\mu \phi_a \rightarrow \mathcal{L}_{\rho\pi\pi} = \hat{g}_\rho \varepsilon_{abc} \phi_a \partial_\mu \phi_b \rho_c^\mu, \quad (8)$$

$$\mathcal{L}_{\bar{D}D} = \partial_\mu \bar{D} \partial^\mu D \rightarrow \mathcal{L}_{\rho DD} = \frac{i}{2} \hat{g}_\rho \left[\bar{D} \tau_c \partial_\mu D - \partial_\mu \bar{D} \tau_c D \right] \rho_c^\mu, \quad (9)$$

$$\begin{aligned} \mathcal{L}_{\bar{D}^* D^*} &= -\frac{1}{2} \left[\partial_\mu \bar{D}_\nu^* - \partial_\nu \bar{D}_\mu^* \right] \left[\partial^\mu D^{*\nu} - \partial^\nu D^{*\mu} \right] \rightarrow \\ \mathcal{L}_{\rho \bar{D}^* D^*} &= -\frac{i}{2} \hat{g}_\rho \left[\bar{D}^{*\nu} \tau_c \left(\partial_\mu D_\nu^* - \partial_\nu D_\mu^* \right) - \left(\partial_\mu \bar{D}_\nu^* - \partial_\nu \bar{D}_\mu^* \right) \tau_c D^{*\nu} \right] \rho_c^\mu. \end{aligned} \quad (10)$$

With these Lagrangians we can write and evaluate the contributions of Figs. 2-4 to the total vertex function.

III. RESULTS

The $\pi^a(q) D(p) D_\alpha^*(p')$ vertex function $\Gamma_\alpha^a(p^2)$ for an off-shell D is written as

$$\Gamma_\alpha^a(p^2) = -\tau^a q_\alpha G(p^2), \quad (11)$$

where $G(p^2)$ is a form factor, such that the physical coupling constant is $g_{\pi DD^*} = G(m_D^2)$. We consider two kinds of loop corrections to this vertex, containing pion and rho intermediate states, denoted respectively by $F_\pi(p^2)$ and $F_\rho(p^2)$. The perturbative evaluation of these functions gives rise to diver-

gent integrals and $G(p^2)$ can be determined only up to yet unknown renormalization constants.

The use of standard loop integration techniques, such as dimensional regularization and \overline{MS} subtraction of divergences, for all diagrams, allows one to write the form factor as

$$G(p^2) = K + C_\pi F_\pi(p^2) + C_\rho F_\rho(p^2), \quad (12)$$

where K , C_π and C_ρ are constants. These constants incorporate the bare couplings $\hat{g}_{\pi DD^*}$ and \hat{g}_ρ , the usual parameters associated with renormalization and, in this work, are determined by comparing the general structure of $G(p^2)$ with the results from QCD sum rules.

Keeping only the terms which depend on p^2 , the explicit evaluation of the diagrams given in Figs. 2-4 yields:

$$\begin{aligned} F_\pi &= \frac{1}{(4\pi)^2} \left\{ \left[(m_{D^*}^2 - m_D^2) - \frac{1}{4m_{D^*}^2} (m_{D^*}^2 - m_D^2 + \mu^2)^2 \right] \Pi_{\pi DD^*}^{(001)} \right. \\ &\quad \left. - \frac{1}{4m_{D^*}^2} \left[(m_{D^*}^2 + m_D^2 - \mu^2) \Pi_{\pi D^*}^{(01)} + 6 (m_{D^*}^2 - m_D^2 + \mu^2) \Pi_{\pi D^*}^{(00)} \right] \right\}, \end{aligned} \quad (13)$$

$$\begin{aligned} F_\rho &= \frac{1}{(4\pi)^2} \left\{ - \left(2m_{D^*}^2 - 2m_D^2 - 2\mu^2 + m_\rho^2 \right) \left[\Pi_{\rho\pi D}^{(000)} + \Pi_{\rho\pi D}^{(010)} + \Pi_{\rho\pi D}^{(001)} \right] \right. \\ &\quad + (m_{D^*}^2 - m_D^2 + \mu^2) \left[2\Pi_{\rho\pi D^*}^{(000)} + \Pi_{\rho\pi D^*}^{(001)} \right] + 2 (m_{D^*}^2 - m_D^2) \left[\Pi_{\rho\pi D^*}^{(010)} \right] \\ &\quad - \frac{1}{2} (m_{D^*}^2 + m_D^2 - \mu^2) \left[\Pi_{\rho DD^*}^{(000)} \right] - \frac{1}{8} (m_{D^*}^2 + 3m_D^2 - \mu^2) \left[\Pi_{\rho DD^*}^{(010)} \right] \\ &\quad \left. - \frac{1}{8} (-m_{D^*}^2 + 5m_D^2 - 5\mu^2) \left[\Pi_{\rho DD^*}^{(001)} \right] + \frac{3}{8} \Pi_{\rho D}^{(00)} \right\}, \end{aligned} \quad (14)$$

where μ is the pion mass. The functions Π_{xyz} and Π_{xy} entering these results are Feynman integrals, with lower labels indicating the intermediate propagating states. Upper indices represent the Lorentz tensor structure, which is realized in terms of the external variables q , p and p' , and defined by the relationships

$$\begin{aligned}\Pi_{xyz}^{(klm)} &= - \int_0^1 da a \int_0^1 db [- (1-a)]^k [-a(1-b)]^l [-ab]^m [1/D_{xyz}] , \\ D_{xyz} &= (1-a) m_x^2 + a(1-b) m_y^2 + ab m_z^2 \\ &\quad - a(1-a)(1-b) (p_x - p_y)^2 - a(1-a)b (p_x - p_z)^2 - a^2b(1-b) (p_y - p_z)^2 ,\end{aligned}\quad (15)$$

and

$$\begin{aligned}\Pi_{xy}^{(kl)} &= - \int_0^1 da [- (1-a)]^k [-a]^l \ln [D_{xy}/\bar{D}_{xy}] , \\ D_{xy} &= (1-a) m_x^2 + a m_y^2 - a(1-a) (p_x - p_y)^2 , \\ \bar{D}_{xy} &= (1-a) m_x^2 + a m_y^2 .\end{aligned}\quad (16)$$

Using (13) and (14) into (12), we obtain the form factor as a function of p^2 , the D four-momentum squared. At this stage, it still contains three unknown parameters, which are determined by adjusting the function $G(p^2)$ to the QCD sum rule points taken from ref. [16]. Those results are displayed in Fig. 5, where $P^2 \equiv -p^2$, together with our best fit ($\chi^2 \sim 10^{-3}$) represented by the solid line. Computing the value of $G(p^2)$ at $p^2 = m_D^2$, we arrive at the following value for the coupling constant:

$$g_{D^*D\pi} = 17.5 \pm 1.5 , \quad (17)$$

in very good agreement with experiment. The errors quoted come from the QCDSR points, which are typically about $\simeq 10\%$. In the same figure we also show the results of the fits of the QCDSR points with two mixed monopole-dipole structures with three free parameters, namely

$$G^{FI}(p^2) = C \left[\frac{\Lambda_1^2 - m_D^2}{\Lambda_1^2 - p^2} + \left(\frac{\Lambda_2^2 - m_D^2}{\Lambda_2^2 - p^2} \right)^2 \right] , \quad (18)$$

$$G^{FH}(p^2) = C_1 \frac{\Lambda^2 - m_D^2}{\Lambda^2 - p^2} + C_2 \left(\frac{\Lambda^2 - m_D^2}{\Lambda^2 - p^2} \right)^2 , \quad (19)$$

which yield $\chi_I^2 \sim 10^{-3}$ (dashed line) and $\chi_{II}^2 \sim 10^{-2}$ (dash-dotted line), respectively. Inspecting Fig. 5 one learns that these alternative structures, reasonable as they are, diverge significantly from the loop calculation in the region where the D is not too off-shell, stressing the importance of a proper hadronic treatment of the form factor in that region.

In this work we also consider the $B^*B\pi$ vertex with an off-shell B , which can be obtained by a straightforward replacement of the charmed particles with those containing the quark b in the results described above. Using the same Lagrangians

and fitting procedure with results from ref. [16], we obtain the curve shown in Fig. 6. The resulting coupling constant is:

$$g_{B^*B\pi} = 44.7 \pm 1.0 , \quad (20)$$

in good agreement with lattice estimates.

As far as practical applications are concerned, our numerical results for the form factors $G_{D^*D\pi}(p^2)$ and $G_{B^*B\pi}(p^2)$, in the whole range $m_{D(B)}^2 \leq p^2 < -5$ GeV, are very well described by the mixed monopole-dipole structure given by eq.(18) with the parameters

$$G_{D^*D\pi}(p^2) \rightarrow C = 8.7 ; \Lambda_1 = 5.1 \text{ GeV} ; \Lambda_2 = 2.9 \text{ GeV} ,$$

$$G_{B^*B\pi}(p^2) \rightarrow C = 22.4 ; \Lambda_1 = 7.8 \text{ GeV} ; \Lambda_2 = 7.1 \text{ GeV} \quad (21)$$

Our good results allow us to believe that the use of meson loops can significantly reduce the uncertainty in the extrapolation of form factors, computed in the space-like region by means of QCDSR, to the time-like region, with the corresponding increase in the reliability of predictions for coupling constants. It is worth stressing that, apart from the approximations described in the introduction, our procedure has no new source of errors.

IV. CONCLUSIONS

We have developed a new method of improving QCDSR calculations of hadronic form factors. It consists in matching QCDSR results, valid mainly in the deep euclidian region, to meson loop calculations, valid when the D is not too off-shell. The basic idea is to reduce the freedom of the function used to interpolate between these two regions by imposing the best possible behaviour in the region where the D is almost on-shell. In the spirit of chiral perturbation theory, this region is described by a tree diagram corrected by processes involving loops. The leading order (LO) corrections are given by one-loop diagrams containing internal pions. Diagrams containing the ρ , on the other hand, may be understood as a subclass of two-loop corrections, in which the resonance simulates a two-pion system. This class of contributions does not represent a systematic next-to-leading order chiral correction, but it allows a reasonable extension of the LO results.

The matching between chiral and *QCDSR* results is well justified from the following physical point of view: in the intermediate and large Q^2 regions the relevant degrees of freedom are the quarks and gluons, with non-perturbative corrections taken into account through the QCD condensates. The opposite happens for low values of Q^2 , where sum rules calculations become non-reliable. At this point, the meson exchange dynamics becomes the most reliable tool, but it depends on unknown constants associated with the renormalization of the mesonic vertices.

Although the exact frontier between meson dynamics and *QCDSR* cannot be precisely known, the success of the method

in the instances considered here supports the view that the matching may become useful in increasing the predictive power of both procedures. In order to validate this assumption, it would be useful to apply it to other processes of the same kind. This encourages us to reconsider our previous form factor studies.

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