

Estimate of hourly productivity applied to elaboration and implementation of mining plans

Estimativa de produtividade horária aplicada à elaboração e execução de planos de lavra

Edmo da Cunha Rodovalho

Professor Assistente

ICT / Universidade Federal de Alfenas
Poços de Caldas - Minas Gerais - Brasil
edmo.rodvalho@gmail.com

Ivo Eyer Cabral

Professor Associado

PPGEM / Escola de Minas / Universidade Federal
de Ouro Preto
Ouro Preto - Minas Gerais - Brasil
cabralmg@uai.com.br

Abstract

In order to elaborate a mine plan, it is necessary to adopt hourly production parameters for the equipment available for its execution. This equipment should be in synchrony with the productive capacity of the operational units in the mine for: rock drilling, blasting, loading and transporting ore. This study deals with the estimate of hourly production indexes for loading and transport obtained by the use of multiple regressions. Using a management system database from an operating mine, equations were generated to explain the productive cycle of each of the loading machines and dump trucks. Knowing the behavior of the principle variables that exert influence on the production schedule, it was possible to estimate the index and to guarantee high feasibility for the mine plan, considering the indexes obtained were very close to those executed. The model design was created in a simple manner, using statistical concepts and computational tools, being supported by good correlation between the variables. This factor was decisive in obtaining good results in the execution of the studied mining plan.

Keywords: *Mine planning, hourly productivity, multiple regressions, operational management*

Resumo

Para elaboração de planos de lavra, é necessário adotar parâmetros de produtividade horária dos equipamentos disponíveis para sua execução. Esses equipamentos devem estar em sincronia com a capacidade produtiva das operações unitárias de lavra mineira: perfuração de rocha, desmonte, carregamento e transporte. Esse estudo trata da estimativa de índices de produtividade horária das operações de carregamento e transporte com a utilização de regressões múltiplas. Através da utilização da base de dados do sistema de gerenciamento operacional de uma mina, foram geradas equações que explicam o ciclo produtivo de cada um dos equipamentos de carga e das frota-transporte. Conhecendo-se o comportamento das principais variáveis que exercem influência na produtividade horária, foi possível estimar esse índice e garantir alta exequibilidade para o plano de lavra, pois os índices obtidos foram muito próximos dos reais. A formulação do modelo foi realizada de forma simples, utilizando-se de conceitos estatísticos e de ferramentas computacionais, sendo o modelo sustentado por uma boa correlação entre as variáveis. Esse fator foi decisivo para que esse estudo obtivesse bons resultados na execução dos planos de lavra estudados.

Palavras chave: *Plano de lavra, produtividade horária, regressões múltiplas, gerenciamento operacional.*

1. Introduction

During the 1960's, simulation techniques became popular and had the objective of maximizing mining operation productivity (Brandão and Tomi, 2011). Mining operations should have production goals that are feasible and compatible with the system capacity. In order to describe a productive system, it is necessary to define the main variables according to the objectives of the study (Law and Kelton, 2000). One of the responses of the simulation model is to estimate the performance of the system that is generated and this is achieved by studying the behavior of the main variables of the process (Banks et al., 2001). These variables are linked to the produc-

tion cycle and are stored in databases.

Since the elaboration of the mine plan used historical average production figures, it is important to mention that the cycle time variation, operational delays (change of shifts, fueling time, etc.) and the changes in average transport distance (which in this article is denominated by the acronym ATD) are not taken into consideration. In this way, the plan does not account for possible interferences that could compromise its feasibility, such as possible ATD reductions and variation in the cycle time, which could lead to not achieving the quality and production goals forecasted in the plan.

Herein, data generated by the loading and transport operations of a mine will be presented to illustrate the study. These data were the source used to generate the equations that explain each one of the flows in the transport. In turn, these equations are attributed parameters that were forecasted for each flow, where part is determined through established goals by means of historical averages (operational delays, queuing time, spotting and maneuvering time, etc.), while ATD is informed by the mining plan. Thus, altering the sequence implies in a distinct hourly production estimate, guaranteeing a realistic capacity of the available fleet for the mining plan execution.

2. Methodology

There is no doubt that the development of a complex simulation model demands time and costs (Robinson, 2004), because even if one has the proficiency in a determined computation tool connected with the simulation, the modeling of complex systems requires, in

a proportional manner, vast data collection, model construction, and data output analysis (Chung, 2004). With the objective of estimating productivity indicators for loading and hauling equipment during the execution of the mining plan, the proposed model has the capacity to forecast

the performance of these operations. The use of the multiple regression concepts to explain the steps of the productive process is relatively simple, but what differentiates this study is the integration of various equations to forecast the behavior of the overall productive system.

Data collection

As the focus of this study was to devise a mining plan, the analyses and applications refer to monthly mining plans. An Iron Ore mine located in the Minas Gerais Iron Quadrangle, Brazil, was chosen to demonstrate the applicability of the methodology. The period of the year in which the studies were undertaken was between the months of July and September of 2012, which corresponds to the dry season of the region. The multiple linear regressions performed and equations created used data referring to the month of July, 2012. Mentioning the climatic conditions is decisive, since there is a strong tendency for performance loss in mining

operations during the rainy periods, when compared with the dry period.

The source of information was the fleet management system (electronic dispatch) where the information was stratified in shifts during the month of July, 2012. For the loading fleet, data was collected according to the following variables: loading time, cycle time, operational delays, ATD, average downtime and operational moment ($t \times \text{km/h}$). This last variable is the product of multiplication between the payload and speed of trucks allocated to the load equipment. For the transport equipment, this variable refers to each vehicle of the transport fleet. The

relationship between payload and speed of trucks is considered in the operational management system of the studied mining company because it has effect on tire consumption and fleet performance. Therefore, the operational moment, as this variable is called at the studied mining company, may be considered for this study. For the transportation fleet, data referred to the following variables: operational delay, cycle time, queuing time, maneuvering time, loading time, average load, ATD, operational moment and the ratio between the distance when carrying a full or empty load (herein denominated Km full/empty).

Analysis of the correlated matrixes

Before analyzing the linear regressions using the variables cited in the previous item, it is necessary to evaluate the ones that have the greatest correlation with the productivity hours. To guarantee that the equations have a high correlation index and to explain the productive process, it is of interest that the independent variables be strongly correlated with the dependent variables. In Table 1, a matrix that corre-

lates the information referring to an EX40 excavator used in the study is presented. The table indicates that the smallest correlation with productivity hours is the cyclic time for the trucks assigned to this excavator. Another important item that this matrix reveals is that the relationship can be proportionally direct or reverse. A negative correlation indicates that the variable analyzed is inversely proportional

to the productivity hours. An example of this is the idleness of (-71.8%) that presents a correlation with productivity, indicating that the greater the idleness of this excavator, the lesser the productivity estimated by the equation.

The table indicates which variable could be discarded from the multiple regression analysis when the correlation of the equation is not satisfactory. With the

Minitab® analysis program, it is possible to select the variables. For this study, the *stepwise forward and backward method*

was used for the variable selection. This method begins with the use of all the variables, which are then successively excluded

by order of growing correlation. The selection ends when the equation encounters the adequate correlation.

	HOURLY PRODUCTIVITY	ATD	MOMENT	AVERAGE DOWNTIME	OPERATIONAL DELAYS (HOURS)	CYCLE TIME
ATD	-0,088					
MOMENT	0,422	0,79				
AVERAGE DOWNTIME	-0,718	-0,019	-0,413			
OPERATIONAL DELAYS (HOURS)	-0,191	0,113	0,174	-0,075		
CYCLE TIME	-0,029	0,745	0,58	0,076	0,144	
LOAD TIME	-0,243	0,179	-0,015	-0,126	0,051	0,136

Table 1
Correlation matrix between variables of the EX40 excavator.

This analysis is part of processes that generate equations for each one of the

analyzed flows, and with this, generate a matrix and an equation for each one of the

loading machines and for each vehicle of the transportation fleet.

Generation of the productivity equations

After identification, consultation and collection of all the data referring to the stages of the processes that would influence productivity, it was possible to initiate the analytic process for the correlations between the variables. This analysis is performed using multivariate linear regression that informs the relationship between two or more variables by using a linear equation. The quality of the regression is measured by the determinant coefficient (R-sq) which corresponds to the coefficient of the linear correlation (Charnet, 2008). The greater the correlation is, the greater the representation of the equation in describing the system.

High indexes of correlation indicate a high capacity to explain the process.

In this study, the dependent variables are the loading and transportation fleet's hourly productivity, while the independent variables are those that together can satisfactorily explain the hourly productivity.

Hourly productivity is a term that depends on all of the studied equations and can be called HPF (hourly productivity function). The independent variables for the loading fleet are represented in the following manner: average downtime (ADT), ATD, operational moment (M), operational delays (OD), cycle time (CT)

and loading time (LT). The independent variables for the transportation fleet has the following acronyms: operational moment (M), operational delays (OD), cycle time (CT), queue time (QT), maneuvering time (MT), loading time (LT), average load (AL), ATD, and Km full/ Km empty (KFE). Table 2 shows the coefficients of the equations and the determining coefficients (R-sq) obtained by multiple regressions for the loading machines. Table 3 shows the equations referring to the transportation fleet. Blank fields indicate the variables disregarded following the same procedure described in the previous section.

LOADING MACHINES	COEFFICIENTS FOR THE HOURLY PRODUCTIVITY EQUATION								R -sq
	CONSTANT	ATD	M	ADT	OD	CT	LT		
EX44	2061	-432	0,217	-768	-308		-1924	95,50%	
EX40	2499,8	-369,18	0,17267	-4416	-317,15		-5501	94,90%	
EX41	2153,4	-441,69	0,22989	-2103	-335,46		-4169	83,23%	
EX42	1870,44	-344,99	0,18289	-1547,8	-295	185,6	-1021	95,30%	
EX43	1467,4	-424,96	0,24457	1806	-312,64		3105	95,80%	
EX27	1132,46	-273,73	0,23429	133,5	-192,57		-86,5	94,00%	
EX22	1336,14	-291,4	0,21784	245,5	-241,51		-260,4	94,00%	
EX21	1559,92	-88,61		-7968,5		898		78,60%	
LT03	1670,91	-393,35	0,22658	-465	-291,44			90,90%	
PM30	2133,81	-409,09	0,21569	-1808,5	-366,54		-3384	92,40%	
PM25	2349,42	-89,04	0,01984	-10206,6	-249,07	416,5	-12932	92,50%	
PM26	2279,98	25,98	-0,02171	-12328	-272,15	-60,4	-12327	94,70%	
PM27	2703,24	-25,09	-0,00858	-12497,2	-246,82		-17944	95,00%	

Table 2
Coefficients for the hourly productivity equations for the loading machines

COEFFICIENTS FOR THE HOURLY PRODUCTIVITY EQUATION		CONSTANT	M	OD	CT	QT	MT	LT	AL	ATD	KFE	R -sq
TRANSPORTATION FLEET	FLEET 1	261,8	0,28248	-4,856	-176,83	-322,2	859,6	-152,2	0,7719	-86,375	-9,92	95,3%
	FLEET 2	353,73	0,28042	-3,0467	71,55	-57,2	237,6	198,4	-0,1821	-105,99	21,57	96,8%
	FLEET 3	424,1	0,25516	-5,2592	18,41	133,48	-	-	-0,1508	-104,74	5,501	97,6%

Table 3
Coefficients for the hourly productivity equations for the transportation fleet.

3. Case study

The equations herein presented

were applied to an actual plan for a large

iron ore open-pit mine for the month of

September, 2012. The information used as the base for the equations and the database that defined the parameters refer to six-hour shifts, 24 hours a day, 7 days a week during these months.

The first step of the study involved the elaboration of the monthly mining plan which was designed in two phases. The first phase consisted in determining the monthly ore production needed to feed the plant, remove the waste and other actions informed in the budget. In this phase, performance indicators are also used to demonstrate physical usage

(PU), physical availability (PA) and overall hourly productivity for delimiting the advance in accordance with the budget forecasted. These are preliminary advances and are utilized in the generation of the mass through flux and in obtaining the transport route profile.

In each of the shifts, it is possible that there exists a part that is destined to feed the processing plant, another destined for the waste pile and another destined for strategic storage of ROM. As each shift has a different transport profile in relation to destination, the masses

are used as weighting values. Thus, it is possible to calculate the average transportation distance (ATD) for each of the mining shifts.

After consolidating the information of the plan, such as: demands and identification of the shifts and design of the transport profile, it is possible to calculate the total ATD of the plan for each shift, and its stratification by destiny. In table 4, each one of the shifts has its transport profile that when considered in connection with the mass, generates the ATD by shift and globally.

MINE AREAS	SHIFTS	MASS (t) / DESTINATION			TRANSPORTATION DISTANCE (m)			ATD (Km)
		Crusher	Stock	Waste pile	Crusher	Stock	Waste pile	
NORTHPT	20K_1360/47 (EX44/PM)	111.627	60.013	9.288	4.306	5.597	7.130	4,88
	20K_1373/60 (EX44/PM)	257.344	253.075	26.627	4.306	5.597	7.130	5,05
	19K_1386/73 (EX22)	336.622	443.104	102.578	3.366	4.657	5.998	4,32
	15I_1490/77 (EX40/PM)	155.326	185.697	194	4.077	5.113	3.820	4,64
	15I_1477/64 (EX40/PM)	240.102	70.340	685	3.867	4.903	3.610	4,10
	14H_1464/51 (PM)	7.513	4.292	180.821	3.498	4.534	3.241	3,28
	20J_17K_18K_1399/86 (EX22/EX27/EX21)	392.746	793.482	24.265	3.366	4.657	5.998	4,27
	NP_TOTAL	1.501.280	1.810.003	344.458				
MEANPT	10M_1178/65 (EX43)	84.077	68.354	187.378	2.023	3.022	3.202	3,15
	100_1178/65 (EX42)	0	222.484	771.587	2.082	3.498	5.013	4,67
	9N_1048/35 (EX41)	197.000	90.693	138.762	2.141	3.655	4.794	3,33
	9N_1061/48 (EX41)	136.023	43.577	391	2.050	3.564	4.703	2,42
	MP_TOTAL	417.100	425.108	1.098.118				
STOCK PILES	Stock 1 e 12	375.867			300			0,30
	Stock 15	150.000			3.234			3,23
	Stock 13	150.000			4.235			4,24
	TOTAL STOCKS	675.867						
TOTAL ATD								3,85

Table 4
Mass profile and average transportation distance forecasted in the mining plan.

The next step was to establish a goal for operational delays that were generated according to the behavior of this variable during the last twenty months before this study began. This variable was used because it is the only one that depends on manageable mining events. In the studied mine, this goal is established by the average of the delays in relationship with the available hours (AH).

Available hours (AH) are the result of the subtraction of the hours in which the machinery are under maintenance in relationship with the calendar hours (CH). The ratio AH/CH informs the index of physical availability (PA) of a

machine or a fleet. The value of CH is 6 hours in each shift, resulting in 24 hours of CH each day. With the establishment of a goal and with the gathering of the PA of the studied fleets, it is possible to establish a goal for operational delays (OD) in number of hours by their input in the multiple regression equations. Table 5 presents the OD goals in stratified hours according to shifts, loading machines, and transport fleet for the month of September 2012.

The last step is the input of the inherent parameters for the process, such as: average idleness, operational moment, loading time, cycle time, queuing time,

maneuvering time, average load and relationship Km full/empty. It is important to notice that for these parameters, considered are their updated averages that were executed by the productive process during the study. Besides, it is also necessary to add the variables connected with the management of the mining operation (OD) and the variables related to the excavation of the ore (monthly plan) that is represented by ATD. The ATD and OD variables are related to productive process management and the advances forecast in the mining plan, which in turn, attempts to fulfill production and development programs.

LOAD													TRANSPORT				
	EX21	EX22	EX27	EX40	EX41	EX42	EX43	EX44	PM25	PM26	PM27	PM30	LT-03		FLEET 1	FLEET 2	FLEET 3
OD/AH GOAL (%)	13,0%	13,8%	13,3%	9,9%	12,8%	11,8%	13,7%	12,5%	13,1%	13,1%	13,1%	14,7	14,7%	OD/AH GOAL (%)	13,3%	12,9%	13,0%
PA (%)	60,0%	63,9%	65,0%	71,8%	71,0%	73,1%	74,0%	71,5%	61,3%	63,6%	65,6%	61,9%	56,1%	PA (%)	76,0%	77,7%	63,5%
CH	6	6	6	6	6	6	6	6	6	6	6	6	6	CH	6	6	6
AH	3,6	3,8	3,9	4,3	4,3	4,4	4,4	4,3	3,7	3,8	3,9	3,7	3,4	AH	68,4	60,6	76,2
SHIFT GOAL OD (HOURS)	0,47	0,53	0,52	0,43	0,55	0,52	0,61	0,54	0,48	0,50	0,51	0,54	0,49	SHIFT GOAL OD (HOURS)	9,12	7,81	9,90

Table 5
Goals for operational delays referring to the month of September, 2012.

Having on hand the values of these variables and with the regression equation, the productivity of each loading machine

and the transportation fleet was obtained. Equation (1) refers to the EX40 excavator. Equations for the other loading machines

were already presented in Table 2. The coefficients referring to the transportation fleet were presented in Table 3.

$$HPF = 2499,8 - 369,2. ATD + 0,173.M - 4416.ADT - 317.OD - 5501.LT \tag{1}$$

With the substitution of the ATD and OD unknowns by their respective values referring to the EX40 excavator (informed in Tables 4 and 5), and the in-

formation presented in Table 6 (informs the rest of the plan's parameters), it is possible to estimate the hourly productivity of the EX40 excavator. The same

procedure was applied to estimate the hourly productivity of the other loading machines.

OPERATIONAL PARAMETERS SEPTEMBER/2012													
LOADING MACHINES													
	EX44	EX40	EX41	EX42	EX43	EX27	EX22	EX21	LT03	PM30	PM25	PM26	PM27
ATD (Km)	5,01	4,38	3,06	4,67	3,15	4,27	4,29	4,27	3,00	3,71	2,20	1,84	2,03
M (t. Km/h)	9813,91	9470,72	6545,11	9463,63	6026,84	4802,44	7085,79		5061,00	5827,60	2698,74	2481,56	2655,44
ADT (h)	0,04	0,04	0,03	0,03	0,03	0,05	0,04	0,04	0,04	0,04	0,04	0,03	0,04
OD (h)	0,54	0,43	0,55	0,52	0,61	0,52	0,76		0,49	0,54	0,77	0,74	0,51
CT (h)				0,03				0,34			0,19	0,17	
LT (h)	0,05	0,04	0,04	0,05	0,05	0,07	0,06			0,06	0,04	0,04	0,04
HPF (t/h)	1.735,9	1.969,3	1.873,4	1.745,5	1.632,9	989,7	1.440,3	1.199,6	1.476,2	1.414,8	1.082,9	1.161,5	1.328,9

Table 6
Hourly productivity estimated by multivariate regression for each of the excavators available for implementing the mining plan.

Table 7 presents the HPF of the transportation fleet when using the

same calculative process as that of the loading machines.

OPERATIONAL PARAMETERS - SEPTEMBER/2012		M (t. Km/h)	OD (h)	CT (H)	QT (h)	MT (h)	LT (h)	AL (h)	ATD (Km)	KFE	HPF (t/h)
TRANSPORTATION FLEET	FLEET 1	854,49	9,12	0,1966	0,0210	0,0193	0,0390	133,95	2,13	0,90	338,10
	FLEET 2	1171,89	7,81	0,2579	0,0243	0,0189	0,0438	165,03	2,77	0,91	385,24
	FLEET 3	1490,84	9,9090	0,3350	0,0286	-	-	225,28	3,40	0,91	377,05

Table 7
Parameters used to estimate the hourly productivity of the plan's available transportation fleet.

With the HPF results, and the physical utilization and availability values

referring to the loading and transportation operations, it is possible to delimitate the

advances of the mine for the period of one month.

4. Discussion of the results

Once the tasks referring to the elaboration of the monthly mining plan were concluded, their execution begins. With the use of the estimated HPF, it was possible to evaluate the forecasted and executable parameters, as well as the impact of each of these parameters

on the hourly productivity. Figure 1 shows the EX40 excavator performance analysis during the month of September 2012. When analyzing its performance using Equation 1, for example, a 72 t/h total loss was identified. The operational moment and loading time were respon-

sible for losses of 380.25 t/h and 14.05 t/h, respectively. On the other hand, there was also an increase in productivity because of the following variables: 32.63 t/h because of the number of downtime hours due to operational delays (OD); 29.29 t/h because of the

reduction of average loading down time (ADT); and 446.7 t/h because of a reduction in the ATD performed.

Even though the equation uses the principal variables related to productivity in order to estimate it, other variables

that were not covered in this study using multivariate regression could have influence on the actual results of hourly productivity. Among these, can be listed: dump time of the transportation vehicles and operational time for

the excavation equipment when dealing with harder rocks. It was necessary to limit the number of variables in order to guarantee a high number of correlations between the selected variables for the HPF estimates.

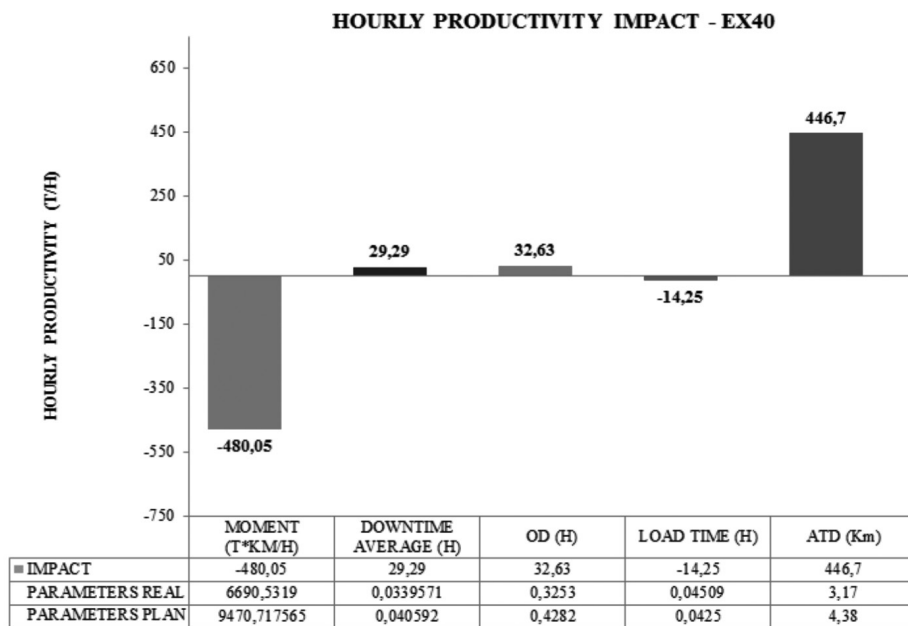


Figure1
Parameter variation impact on the EX40 excavator's hourly productivity.

Similar analyses were performed for each of the loading machines and transport vehicles in order to verify

the negative and positive deviations observed during the implementation of the mining plan for September, 2012.

Table 8 shows the productivity variations, comparing estimated against real.

HOURLY PRODUCTIVITY ANALYSIS SEPTEMBER/2012																	
	LOADING MACHINES													TRANSPORT FLEET			
	EX21	EX22	EX27	PM25	PM26	PM27	EX40	EX41	EX42	EX43	EX44	LT03	TOTAL	FLEET 1	FLEET 2	FLEET 3	TOTAL
ESTIMATE	1199,6	1440,3	989,7	1083,0	1190,0	1329,0	1969,0	1873,0	1745,0	1633,0	1736,0	1476,0	1468,5	338,0	385,0	377,0	367
REAL	948,8	1278,8	1113,9	1149,6	1200,7	1182,1	1897,0	1750,9	1579,9	1492,9	1933,6	1381,8	1437,2	344,2	366,3	385,3	367
VARIATION (%)	26%	13%	-11%	-6%	-1%	12%	4%	7%	10%	9%	-10%	7%	2,2%	-2%	5%	-2%	0,0%

Table 8
Estimated and real productivity when implementing the mining plan during the month of September, 2012.

Table 8 shows the variation between the estimated and actual productivity for the each transportation fleet and loading machines. The overall productivity of the loading machines is proportional to the number of hours that each equipment operated in September 2012 and shows a variations of 2,2%, but there was a high

variation between the loading equipments locally. There were constant interruptions in the operation of excavators EX21 and EX22 due to the high number of hours in operating. These failures affected the stability of the production cycle. There was a decrease in productivity of the front-end-loader PM27 by operational failures.

But some loading machines reached an actual productivity result better than the estimated. These equipments offset the negative deviations. While the deviation for the transportation fleet that occurred in fleets 1, 2 and 3 were balanced in a way that total productivity achieved the same value as estimated.

5. Conclusion

The possibility of being able to estimate hourly productivity indicators makes mining plans more realistic, as-

sertive and coherent with the equipment assigned to execute the loading and transport operations. Another benefit

of this tool is the possibility to quantify, with relative precision, the degree that each variable influences the deviations

between forecasted and executed productions. With the mapping of the bottlenecks identified through the comparison between the considered parameters in the estimate and reality, it is also possible to utilize management tools to control HPF.

The multiple regression techniques are simple and affordable because there is software available to assist their application. These concepts can be used on monthly plans, weekly plans or even mining plans with larger time horizons. For the loading machines, the model

did not perform well locally presenting a high variance between 26% to -11%. But the final result, considering all of the equipment, was balanced in a way that total productivity achieved a value near reality. For the transportation fleet, the estimate informed actual productivity, without variation. This result shows that the integration of various equations obtained by multivariate regressions was efficient in estimating the productivity of the loading and transportation operations of a determined mine.

Future studies may reduce the variations presented locally by providing greater detail of operations. The proposed methodology can be utilized in the future for the management of operational deviations that occur in the execution of mining plans. Besides, these results can be uploaded to a fleet management center that could apply direct actions to block factors that penalize the productivity. Above all, these same results could identify the implementation of good practices.

6. References

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Received: 18 December 2012 - Accepted: 04 April 2014.