



Diffraction and reflection of irregular waves in a harbor employing a spectral model

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*Manuscript received on June 11, 2008; accepted for publication on June 17, 2009;
presented by ALCIDES N. SIAL*

ABSTRACT

The SWAN wave model is widely used in coastal waters and the main focus of this work is on its application in a harbor. Its last released version – SWAN 40.51 – includes an approximation to compute diffraction, however, so far there are few published works that discuss this matter. The performance of the model is therefore investigated in a harbor where reflection and diffraction play a relevant role. To assess its estimates, a phase-resolving Boussinesq wave model is employed as well, together with measurements carried out at a small-scale model of the area behind the breakwater. For irregular, short-crested waves with broad directional spreading, the importance of diffraction is relatively small. On the other hand, reflection of the incident waves is significant, increasing the energy inside the harbor. Nevertheless, the SWAN model does not achieve convergence when it is set to compute diffraction and reflection simultaneously. It is concluded that, for situations typically encountered in harbors, with irregular waves near reflective obstacles, the model should be set without the diffraction option.

Key words: wind waves, SWAN model, wave reflection, wave diffraction, wave transformations in a harbor.

INTRODUCTION

Wave exposure is an important consideration in planning, designing and operating in the coastal zone. Careful analysis is necessary to determine the main characteristics of the waves as significant height, period and direction of propagation covering intervals of time long enough for the characterization of their spatial and temporal variability. In order to do so, wave measurements are employed, with sensors operating remotely such as altimeters (Robinson 2004, Chelton et al. 2001) and Synthetic Aperture Radars (Violante-Carvalho et al. 2005, Rousseau and Forget 2001), or *in situ* as buoys and PUV gauges (Tucker and Pitt 2001).

The description of the variability of the wave climate is of utmost importance for the construction of any coastal structure such as groins, seawalls, jetties and breakwaters. A considerable part of the energy transferred from the atmosphere to the ocean is carried on in the form of wind waves, which is released very quickly in the surf zone affecting the local hydrodynamics, the transport of sediments and the coastal morphology. Exposure analysis is used to evaluate the need to reduce wave energy, while the investigation of wave energy dissipation is required to support the design of these coastal structures.

The disturbance within harbor basins is one of the most important factors in selecting its physical location and best design configuration. The problem of excess

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wave agitation should be explored in either a mathematical or physical model in order to arrive at an optimum harbor layout. Wind waves are the main responsible for the movement of moored vessels from their berthing positions, causing efforts in mooring cables and structures of the pier. The propagation of waves in the vicinity of breakwaters is a complex process that involves shoaling, refraction, diffraction and reflection (Losada et al. 1990, Dingemans 1997, Cho et al. 2001, Ocampo-Torres 2001).

With the advance of computer science, numerical models have been widely improved. However, to be used effectively, it is important that the data are supplied to the model with wealth of details. Modeling an area around a breakwater is a difficult task for numerical models due to the complex transformations undergone by the water waves. From the point of view of coastal research, an effective option would be to employ a numerical model and a small scale physical model, simultaneously, together with wave measurements carried out in the area.

Numerical models may be employed to estimate the main wave characteristics. They can be divided into two general classes (Young 1999): phase resolving and phase averaging models. Phase resolving models predict both the amplitude and phase of the waves, but are computationally much more demanding. Among the main physical processes of interest, only diffraction and three wave interactions require phase resolving models, hence its applications are generally confined to small areas around harbors and the nearshore zone. Phase averaging models, on the other hand, predict average quantities such as the spectrum or significant wave height. If the wave properties vary slowly over a length of order 10 wavelengths or more, computations over large areas are feasible and phase averaging models are more convenient than phase resolving models.

The most employed phase resolving models are those based either on the Mild Slope Equation derived by Berkhoff (1972) or on the Boussinesq Equations (Madsen et al. 1991, Madsen and Sorensen 1992). These models have been applied mainly to the areas where there is an interaction between the waves and any structure like a breakwater or an island. They do not, or only to some extent, account for wave-wave inter-

actions, generation and dissipation and require a high spatial resolution over the entire computational region.

Spectral (phase averaging) models, such as WAM (WAMDI Group 1988), WAVEWATCH III (Tolman 1991) and SWAN (Booij et al. 1999), can account for the processes of generation, propagation, refraction, dissipation and wave-wave interactions. However, these models are not normally used to account for diffraction. In coastal regions, diffraction plays a relevant role in the wave transformations, especially around emerged structures. In general so far, phase-averaged models have been used to estimate the wave conditions in the coastal area and phase-resolving models have been used to compute the wave conditions in the nearshore zone. Recently, a phase-decoupled refraction-diffraction approximation has been incorporated into the spectral wave model SWAN (Holthuijsen et al. 2003), widening its range of applications. Phase-averaged are more efficient than phase-resolving models, therefore, the incorporation of a diffraction approximation into spectral models is a highly desirable feature.

For any coastal study, another possible approach is the construction of physical models of a particular region, as a harbor, represented in scale in the laboratory. Small scale physical models are very useful for developing, improving or testing numerical models, which mainly rely on empirical parameters and on field measurements affected by large uncertainties. They allow the representation of structures, in reduced scale, for understanding their behavior when subjected to environmental conditions. Its main purpose is the representation of possible situations that are not easily tractable analytically.

In this paper is presented a comparison between the propagation of irregular waves inside a harbor employing a small scale physical model of the area together with two numerical models. The measurements obtained in the vicinity of the harbor by a Waverider buoy were also available. The main aim of the study is to evaluate the latest version of the SWAN model (SWAN Team 2006), which has as most important improvement the calculation of diffraction. A small number of scientific papers addresses the effect of diffraction in the SWAN model (as, for example, in Enet et al. 2006, Ilica et al. 2007). Seeking to contribute to

the understanding of the effect of diffraction estimated by the SWAN in a harbor, its performance is compared with a small scale model and the numerical model MIKE BW 21 (DHI 1998), a phase-resolving model based on the Boussinesq equations. The structure of the paper is as follows. First, the study area is described in Section 2, while the SWAN and the MIKE BW 21 models are discussed in Section 3. The methodology employed is described in Section 4 and the results are given in Section 5. Section 6 concludes with a summary and main recommendations.

STUDY AREA

The study area (Fig. 1), the port of the Tubarão Siderurgic Company (CST, from its acronym in Portuguese), lies between latitudes 20°14'S and 20°19'S and longitudes 40°12'W and 40°15'W. The worldwide leader in producing steel slabs, CST is located in the city of Vitória, Espírito Santo State, Southeastern Brazil. Vitória, in general, is subject to waves of higher energy from the southern quadrant, associated with the passage of frontal systems (INPH 2003a).

A directional Waverider was deployed during 198 days, from May 28, 2001 until December 11, 2001, by the Brazilian Waterways Research Institute (INPH) off the Port of Tubarão (located in the vicinity of CST, Fig. 1). The buoy measures vertical and horizontal accelerations using accelerometers and an onboard compass to give the directional displacement in two horizontal axes. The instrument was moored in 20°17'18"S and 40°12'54"W, in a water depth of approximately 21 m. Conventional Fourier techniques were employed for the buoy data analysis, as described in Violante-Carvalho and Robinson (2004).

Measurements did not cover a full year, which is the minimum time required for the characterization of the seasonal variability in a region. However, they were carried out during the period considered most critical for the operation of the harbor. During the Southern Hemisphere winter and spring, extra-tropical cyclones pass over the area more often with the consequent increase in wave energy (INPH 2003b). The higher energy events were selected from the data gathered by the Waverider and employed for simulations with the numerical models. The most unfavorable conditions

of operation inside the harbor were determined, which were employed for the configuration of the physical model.

NUMERICAL MODELS

SWAN

SWAN (Simulating WAVes Nearshore) is a third generation numerical model developed for wave computations in coastal regions (see the 'SWAN book' Holthuijzen 2007, chapter 9). The model uses the action balance to compute the evolution of the wave field in time and space, given by:

$$\begin{aligned} \frac{\partial}{\partial t} N + \frac{\partial}{\partial x} c_x N + \frac{\partial}{\partial y} c_y N \\ + \frac{\partial}{\partial \sigma} c_\sigma N + \frac{\partial}{\partial \theta} c_\theta N = \frac{\partial S}{\partial \sigma} \end{aligned} \quad (1)$$

The action balance equation (1) is a first-order partial differential equation with five independent variables: time (t), the two horizontal coordinates (x, y), relative frequency (σ) and direction of propagation (θ). The first term on the left hand side of (1) represents the rate of change of action (or energy) density in time, where $N(\sigma, \theta)$ is the action density spectrum. The second and third terms indicate propagation of action in the geographical area (with speeds of propagation c_x and c_y in x and y , respectively). The fourth term deals with changes of the relative frequency due to variations in depth and currents (with velocity of propagation c_σ). The fifth term represents refraction induced by variations in depth and currents (with velocity of propagation c_θ). The source term $S (= S(\sigma, \theta))$ represents the effects of generation, dissipation and non-linear wave-wave interactions.

The numerical integration of (1) is implemented using a finite difference scheme in five dimensions: time, geographical space (x, y) and spectral space (σ, θ). Spectral models such as WAM and WAVEWATCH III in general consider non-stationary problems in oceanic scales, while SWAN generally computes wave propagation from deep water through the breaking zone. As the time of residence of the waves in this region is small compared with temporal changes associated with the wind, tide and currents, it is acceptable that (1) be solved independently of time (a steady-state solution), the form used in this work.

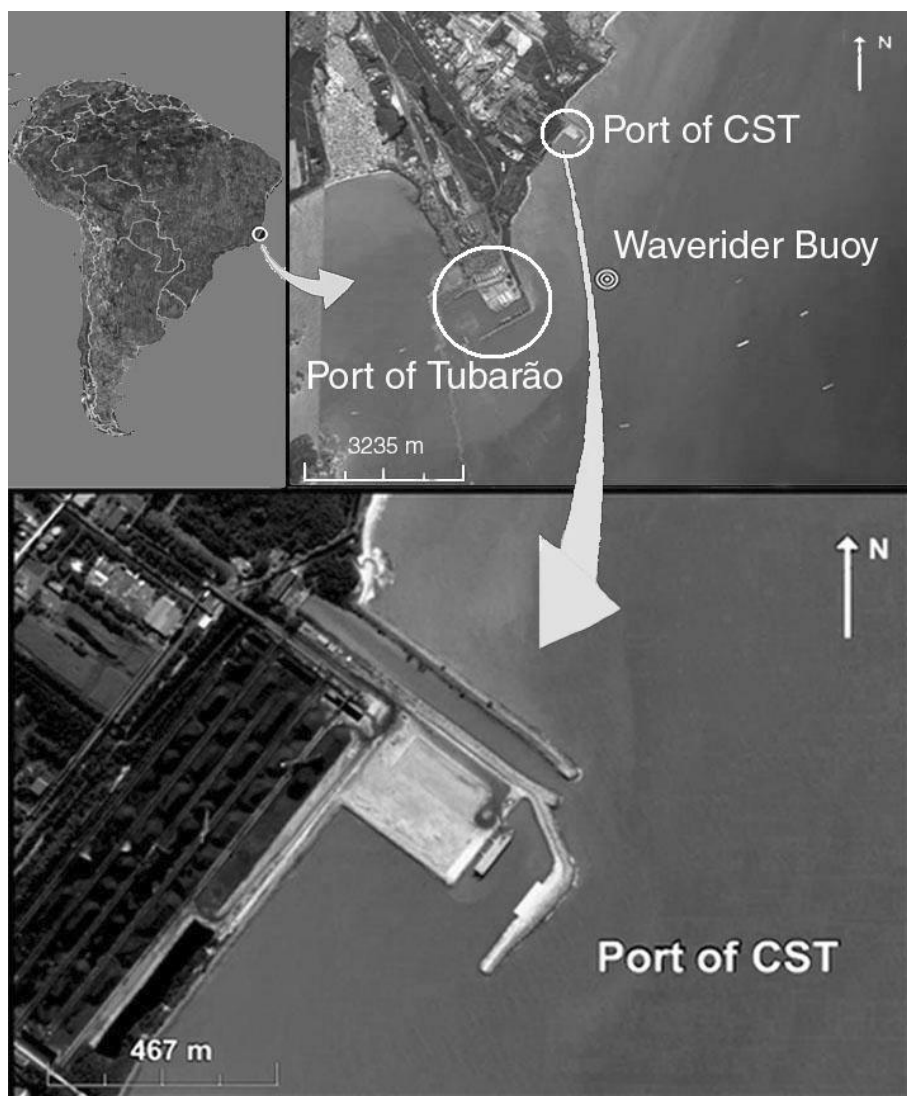


Fig. 1 – The study area, off of the city of Vitória, Espírito Santo State, Southeastern Brazil. The Waverider buoy position is also shown, together with the Port of CST and the Port of Tubarão. Source: Google Earth.

The steady state solution, hence neglecting the first term on the left hand side of (1), is achieved through a number of iterations. The propagation step in the geographical space is carried out for each grid point decomposing the directional space in four quadrants. In each quadrant the computations are carried out independently of the other quadrants with propagation of these components called *sweep*. By rotating each quadrant of 90° becomes possible to propagate energy in all directions over the entire geographical domain.

However, effects that can change the direction of propagation of the wave components, as refraction in-

duced by bathymetry or currents, diffraction and non-linear wave-wave interactions, can shift action density from one quadrant to another. This effect is taken into account through successive iterations, where in each of them the 4 *sweeps* are computed. The computation is over when the iteration process converges indicating that, between two successive iterations, the change in significant wave height is less than 2% and the change in mean wave period is less than 2% in more than 98% of the water covered grid points (Zijlema and van der Westhuysen 2005). While that figure is not reached, the iterations keep going until a maximum number,

previously stipulated, is achieved whether the process turned out to converge or not.

The effects of refraction are easily accounted for with phase-averaged models. Diffraction, on the other hand, is incorporated into the model as presented in Holthuijsen et al. (2003). The approximation is based on the Mild Slope Equation for refraction-diffraction, omitting, however, information about the phase of the waves. The implementation is achieved by adding a parameter δ_E to the propagation velocities c_x , c_y and c_θ given by

$$\delta_E = \frac{\nabla \cdot (cc_g \nabla \sqrt{E})}{\kappa^2 cc_g \sqrt{E}}, \quad (2)$$

where c and c_g are the phase and group velocity, respectively. The energy density is represented by $E = E(\sigma, \theta)$ and κ is a separation parameter.

Apart from the possibility of turning diffraction on and off, the model has some programmable parameters to control how diffraction is computed. The parameters SMPAR and SMNUM are basically used to control the amount of smoothing among adjacent grid points, avoiding numerical instabilities (SWAN Team 2006).

MIKE 21 BW

The phase-resolving model MIKE 21 BW is based on the numerical solution of a new formulation of the Boussinesq equations, derived by Madsen et al. (1991) and Madsen and Sorensen (1992). The main limitation of the classical Boussinesq equations lies on the calculation of wave propagation in deep water. However, its enhanced formulation with improved frequency dispersion makes the model appropriate for simulation of wave propagation from deep water through shallow water. A major engineering application of the model is the assessment of disturbance inside harbors aiming to determine its optimum layout.

The model is capable of reproducing the combined effects of most physical processes of interest in shallow water, such as shoaling, refraction, diffraction and reflection of directional, irregular waves of finite amplitude propagating over complex bathymetries (DHI 1998). It can be applied for the determination of the wave-induced hydrodynamics in coastal areas, as well as for the analysis of oscillations caused by regular and

irregular waves in enclosed basins (Hansen et al. 2005). The version employed here does not include realistic approaches for the mechanism of wave breaking. Consequently, the model should not be extended into the surf zone where wave breaking is important, which is not the case in the present investigation. Hansen et al. (2005) and Sorensen et al. (2004) report the results of some models based on the Boussinesq equations that include wave breaking in their calculations.

The main aim of the present study is to evaluate the efficiency of the SWAN model in situations where diffraction is important; therefore, the description of the model MIKE 21 BW is kept to a minimum. Further details of its main features are described in the operation manual (DHI 1998).

MATERIALS AND METHODS

A bathymetric survey was conducted in the Espírito Santo Bay by INPH in 1999 and in 2002 by Argos Hydrographic Services Limited. In the region further away from the coast the bottom topography was determined from the nautical chart DHN 1410, published by the Brazilian Navy Hydrographic Center.

Simulations performed with MIKE 21 BW indicated that the most unfavorable conditions of operation inside the harbor occur when the direction of wave propagation offshore is from 150° (INPH 2003b). This was, therefore, the direction chosen to set up the physical model. Among the data gathered by the Waverider buoy, 4 records were selected with mean wave direction around 150° and significant height of 1.0 m, 1.5 m, 2.0 m and 2.5 m. The main parameters of selected records of the buoy data used as boundary conditions for the physical model and for the numerical models are listed in Table I.

SCALE MODEL EXPERIMENTATION

Physical model tests using spectral patterns of irregular waves were conducted in a wave basin using a 1:50 scale model built in INPH. Hardware includes a wave generator, signal conditioning and transducers. The wave generator digitally controls the paddles, making it possible to generate arbitrary wave profiles. Wave fields are generated by two single-paddle wave generators in accordance to the input parameters shown in Table I.

TABLE I

Measurements made by the Waverider buoy used as boundary conditions for the physical model and for the numerical models. The values listed are Peak Period (Peak Per), Mean Period (Mean Per), Significant Wave Height (Sig Hei) and Mean Direction (Mean Dir), the direction waves are coming from (compass bearing).

Record	Peak Per	Mean Per	Sig Hei	Mean Dir
1	9.1 s	6.1 s	0.99 m	145.5°
2	7.7 s	5.9 s	1.49 m	149.7°
3	8.3 s	5.8 s	2.00 m	154.6°
4	10.5 s	6.4 s	2.51 m	144.2°

A wave gage array of 8 sampling elements was designed to provide estimates of significant wave height within the physical model. The wave gage operates with a submerged, insulated wire rod. The time-varying height of the water surface creates a varying capacitance that is transmitted to a converter yielding an output voltage proportional to the wave height, later scaled up to natural scale (INPH 2003b).

The position of the 8 wave rods relative to the harbor lay out is presented in Figure 2. The measured field data from the physical model and the calculated data from the two wave models can then be compared. Statistical comparisons were performed with the wave rods displaced over two lines. Line 1 consists of the wave rods numbered as 11, 5, 10, 4 and 9. The outer wave rod number 11, in the less sheltered position, is spaced by a distance from the others of, respectively, 50, 90, 130 and 170 m in the real world scale. Line 2 is composed by rods number 6, 7 and 8. The outer one, number 6, is spaced from the other two of 30 and 190 m, respectively.

NUMERICAL IMPLEMENTATION

Simulations with the models were performed and the measured directional spectra were taken as input at all boundary grid points. Both models were run in stationary mode on a regular grid in Cartesian coordinates. Comparisons of the measured data from the physical model and the calculated data from SWAN and MIKE 21 BW were performed for the computational grid points that correspond to the wave rods. The re-

flexion coefficient chosen (0.40) for both models is typical for rubble mound breakwaters (DHI 1998). Effects such as wind input, whitecapping, currents and wave-wave interactions (triad or quadruplet) were not included in the present study.

MIKE 21 BW was run with a grid spacing of 8 m with a total of 651 by 1021 points. Sponge and porosity layers were used to model absorption and reflection areas through the computational domain. The area around the Port of CST was set as a porosity layer to model partial reflections around the breakwater, while the remaining area was set as a sponge layer absorbing all incoming wave energy.

SWAN simulations, on the other hand, were computed on a coarser grid of 131 by 205 points (grid spacing of 40 m) to reduce computational time. In the area closer to the port, shown in Figure 2, model estimations were achieved by nesting a finer grid run, with resolution of 8 m, in the coarse grid run. Ilica et al. (2007) present several simulations employing SWAN (with diffraction) to determine the optimum grid size with the lowest error and fewer cycles to achieve a stable solution. In that work, the best results were achieved when the ratio between the wavelength corresponding to the peak period and grid size ($\frac{L_p}{\Delta x}$) was from 10 to 15. For larger grid sizes, fewer cycles were necessary to obtain a stable solution. However, increasing grid size worsens the results around tip of structures such as breakwaters (Enet et al. 2006) and a compromise between grid size and model performance must be sought. In the present work, with a grid resolution of 8 m, the ratio $\frac{L_p}{\Delta x}$ is 16.3, 11.5, 13.4 and 21.4, respectively, for the different simulations shown in Table I.

Wave reflection in SWAN is computed setting the coordinates of obstacle lines and a constant reflection coefficient. The position of the obstacle lines in the surroundings of the Port of CST is also depicted in Figure 2. Additionally, several combinations of the diffraction smoothing parameters SMNUM and SMPAR were tested without significant changes in the results, hence their default values were used.

DESCRIPTION AND RESULTS OF THE SIMULATIONS

One way of assessing the performance of the numerical models is computing the diffracted and reflected waves

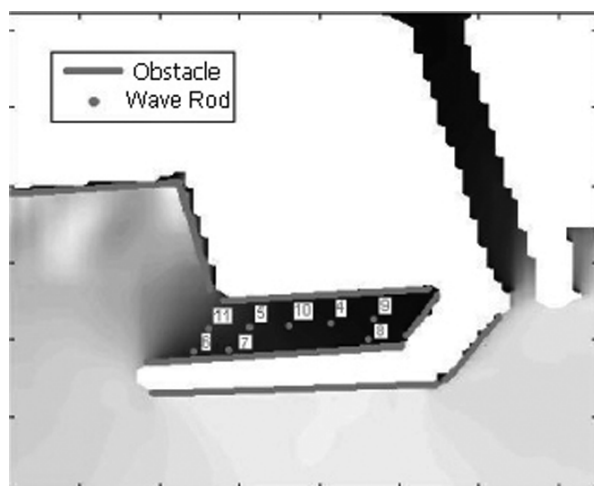


Fig. 2 – Obstacle lines represented by the dark gray lines around the Port of CST, where reflection is computed by the SWAN model. The position of the wave rods in the computational domain is also shown, which are the grid points where significant wave height were estimated by the numerical models. The figure represents the region between latitudes $20^{\circ}15'35''\text{S}$ and $20^{\circ}15'47''\text{S}$ and longitudes $40^{\circ}13'21''\text{W}$ and $40^{\circ}13'01''\text{W}$.

in the harbor and test their results against measurements obtained by the wave rods in the physical model. In order to assure that, different configurations were implemented with the SWAN model. At first, simulations were conducted with diffraction and without reflection (the obstacle lines were not habilitated). In all tests, the model yielded stable solutions after around 10 cycles. A second test was performed without diffraction and with reflection, with stable solutions obtained after around five cycles.

A third configuration, using diffraction and reflection simultaneously, was performed, but the simulations did not converge. After the few initial iterations (from six to nine) the accuracy drops from over 90% of the wet grid points to less than 10% and remains low. However, for each of the four simulations with different incident significant wave heights, the values over the wave rod lines for the iteration obtaining the highest accuracy were compared to the values of the subsequent iterations. The maximum differences, in most of the cases, were less than 1 cm. Therefore, the values of the iteration with the maximum accuracy were used for further comparisons even if the model did not turn out to

converge. The three configurations (with and without diffraction and reflection) were then employed to investigate the importance of diffraction and reflection in SWAN simulations in a harbor.

Figures 3, 4, 5 and 6 show the results for the physical model, for MIKE 21 BW run and for two different runs of the SWAN model (with reflection and with/without diffraction). The figures correspond, respectively, to incident wave heights of 1.0, 1.5, 2.0 and 2.5 m and the two lines where the wave rods were displaced (Fig. 2). It is clear from the figures that higher incident waves correspond to higher energy in the port. The significant wave height measured in the physical model decreases from the outer region (represented by the value 0 on the horizontal axis) towards the sheltered region. Similar results were given by MIKE 21 BW in most of the simulations except in Figure 4b (where significant wave height in rod number 7 is 1 cm higher than in number 6) and in Figure 6b, where significant wave height in rod number 6 is much higher than in number 7 and the curve exhibits an abrupt slope. The same pattern of energy decay towards the inner part of the port is observed with the SWAN estimates but for Figure 6b, where significant wave height in rod number 7 is higher than in number 6.

The plots corresponding to the wave rods over line 1 – Figures 3a, 4a, 5a and 6a – show that the models results are similar, independent of the incident wave height. In general, MIKE 21 BW underestimates the results from the physical model, however comparatively, its values are closer to measurements than SWAN runs. The pattern of the SWAN runs is somehow more erratic, in general underestimating the data derived from the physical model in the sheltered part of the port and overestimating in the outer part. It is also worth mentioning that SWAN predictions with diffraction are higher than without diffraction. In the outer wave rod (number 11), SWAN estimates without diffraction are slightly better than with diffraction.

A similar comparison can be conducted for wave rods over line 2 (Figs. 3b, 4b, 5b and 6b). MIKE 21 BW predictions are better than SWAN estimates, but not as clearly as over line 1. Both models in general underestimate the measurements, except MIKE 21 BW that overestimated the results in the less sheltered area for

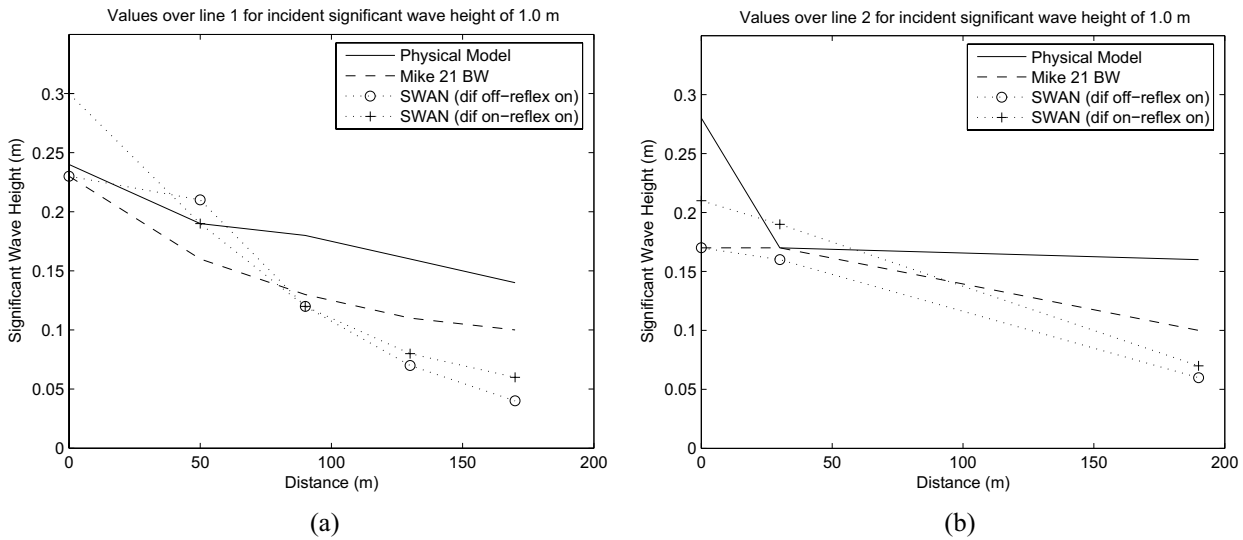


Fig. 3 – Significant wave height measured in the physical model and estimated by the models MIKE 21 BW and SWAN with reflection on for: diffraction off (dif off—reflex on) and diffraction on (dif on—reflex on). For incident significant wave height of 1.0 m (over Line 1 (a) and over Line 2 (b)).

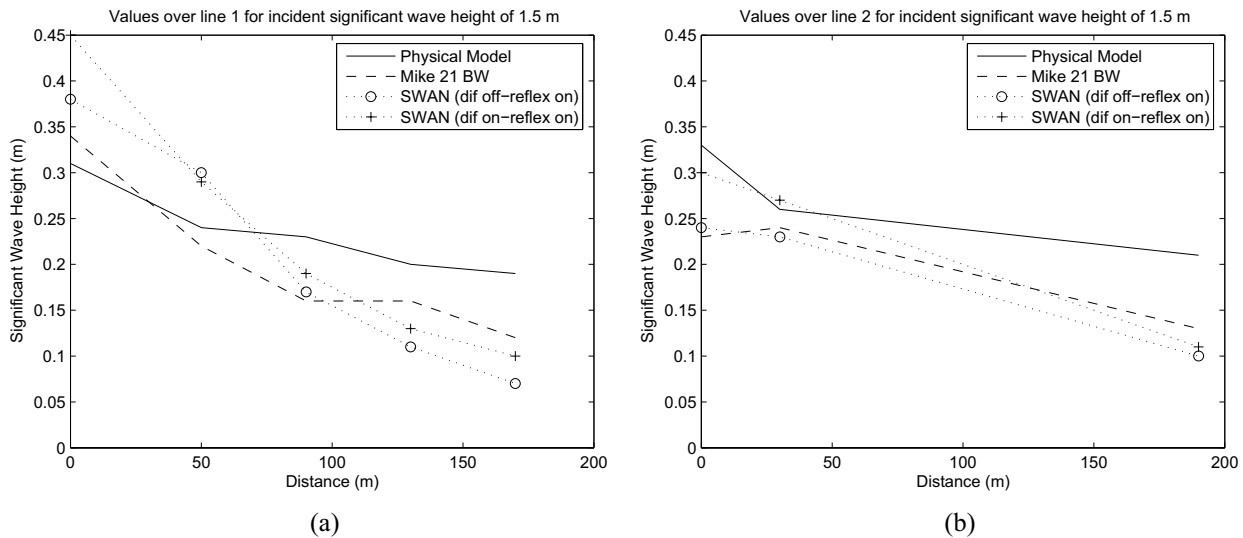


Fig. 4 – Significant wave height measured in the physical model and estimated by the models MIKE 21 BW and SWAN with reflection on for: diffraction off (dif off—reflex on) and diffraction on (dif on—reflex on). For incident significant wave height of 1.5 m (over Line 1 (a) and over Line 2 (b)).

an incident significant wave height of 2.5 m (Fig. 6b). As over line 1, SWAN estimates with diffraction are higher than without diffraction and are closer to the physical model predictions. However, in the more sheltered positions (wave rods number 4 and 9 over line 1 and 1 and 8 over line 2) the difference among SWAN predictions with and without diffraction is small, never more than 6 cm.

Correlation coefficients were obtained between physical model measurements and numerical model estimated data. To increase statistical significance, all values over lines 1 and 2 for the four incident wave heights were taken into account, totalizing 32 points. As Figures 3, 4, 5 and 6 suggest, the highest correlation was achieved by MIKE 21 BW (correlation coefficient $r = 0.95$ and standard deviation $s = 13$ cm). The correlation

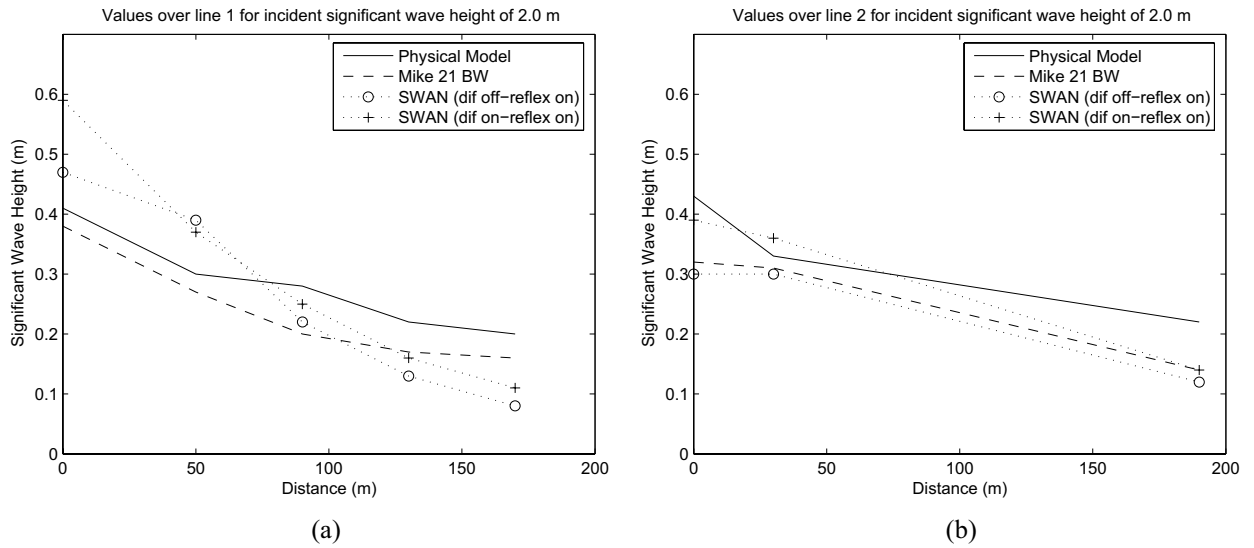


Fig. 5 – Significant wave height measured in the physical model and estimated by the models MIKE 21 BW and SWAN with reflection on for: diffraction off (dif off—reflex on) and diffraction on (dif on—reflex on). For incident significant wave height of 2.0 m (over Line 1 (a) and over Line 2 (b)).

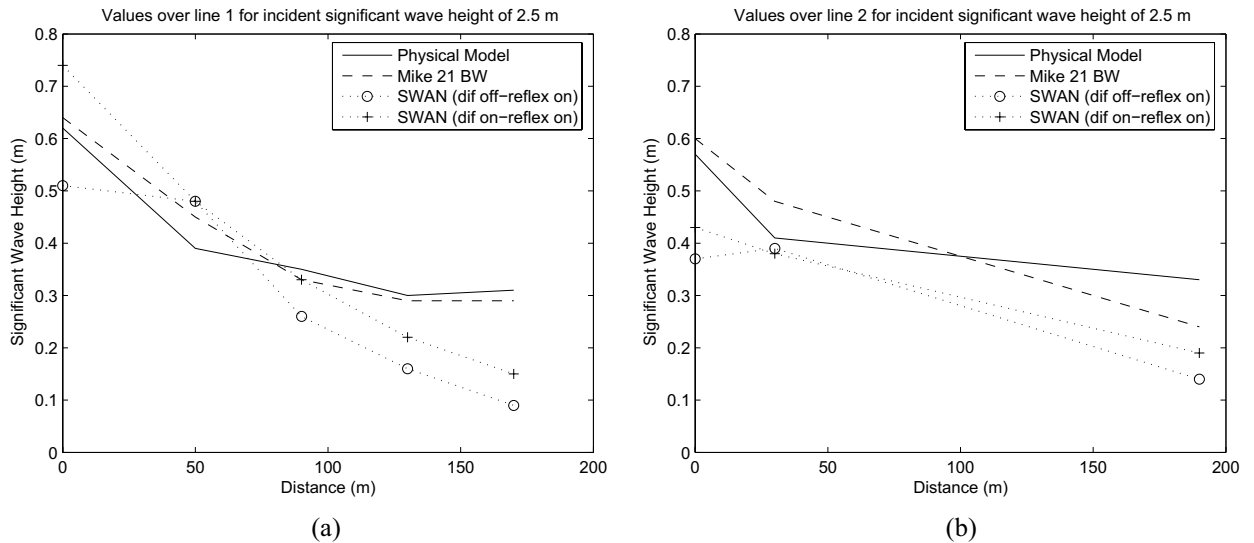


Fig. 6 – Significant wave height measured in the physical model and estimated by the models MIKE 21 BW and SWAN with reflection on for: diffraction off (dif off—reflex on) and diffraction on (dif on—reflex on). For incident significant wave height of 2.5 m (over Line 1 (a) and over Line 2 (b)).

with SWAN runs is slightly lower, $r = 0.86$ and 0.80 and $s = 13$ and 12 cm, respectively, for configuration with and without diffraction. As a matter of comparison, the correlation coefficient between SWAN with and without diffraction is 0.96 with standard deviation of 13 cm.

Additional tests, shown in Figure 7, were conducted without reflection and with diffraction for incident sig-

nificant wave height of 1.0 m. The values calculated by SWAN are much lower than those generated by the physical model, especially over line 2. At wave rod number 8, the most sheltered position over line 2, the wave height is zero, which makes clear the relative importance of reflection in the harbor. Similar results were obtained for the other incident wave heights, not shown here.

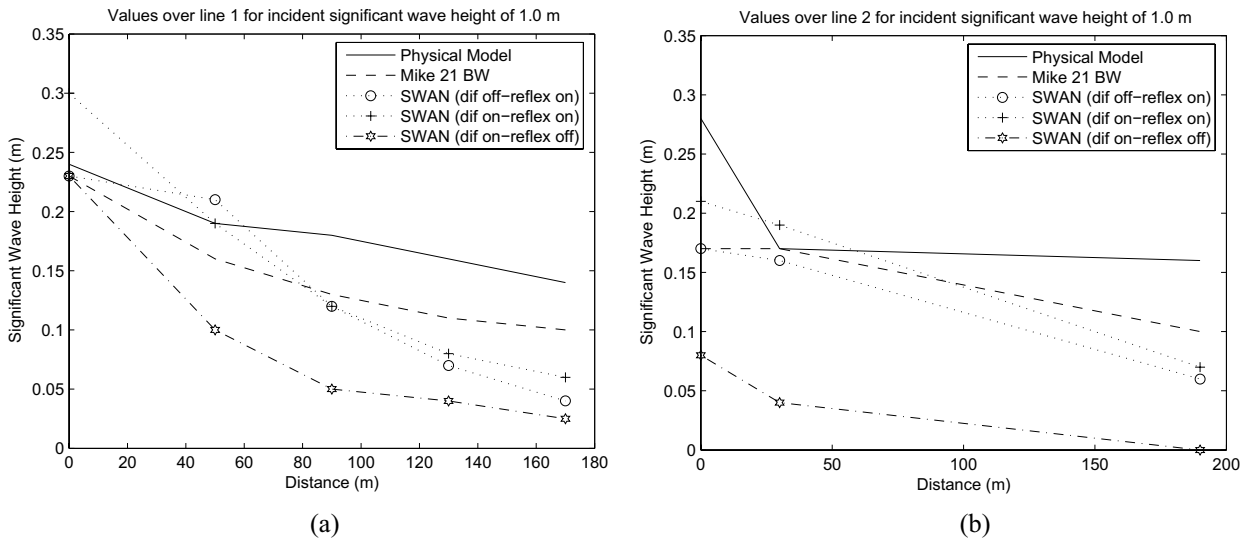


Fig. 7 – Significant wave height measured in the physical model and estimated by the models MIKE 21 BW and SWAN with reflection on for: diffraction off (dif off—reflex on) and diffraction on (dif on—reflex on). The values for reflection off and diffraction on (dif on—reflex off) are also shown. For incident significant wave height of 1.0 m; over Line 1 (a) and over Line 2 (b).

Due to the lack of convergence when SWAN was run with diffraction and with reflection, the choice seems to be either with diffraction and without reflection or without diffraction and with reflection. The results indicate that taking reflection into consideration has a greater relative importance for prediction of wave energy in the harbor. The mean differences between SWAN estimates without diffraction and with reflection and the physical model measurements are, respectively, of 6, 8, 9 and 13 cm for incident wave heights of 1.0, 1.5, 2.0 and 2.5 m. These values correspond to 6, 5.3, 4.5 and 5.2% of the incident significant wave height. Moreover, it is worth to stress that smaller differences were obtained when the model was tested with both diffraction and reflection, although it did not turn out to converge.

SUMMARY AND CONCLUSIONS

Analysis of wave interaction with breakwaters in general are performed using numerical models or small scale physical models. In the present study, both approaches were employed to assess practical limitations regarding the applicability of the combined effect of diffraction and reflection in the SWAN model computing waves in a harbor. In addition, the results of a phase-resolving model were also available, together with measurements made by a Waverider buoy. The validation tests revealed

that SWAN did not converge when set up with reflection and diffraction simultaneously, becoming unstable, revealing limitations to the use of diffraction in the model.

Previous studies have questioned the need to compute wave diffraction in the lee of a breakwater for broad directional spread (as in, for example, Briggs et al. 1995). There is a direct relation between directional spread and wave diffraction. For short crested, irregular waves, with broad directional spread, more energy will be diffracted into the lee of the breakwater than for an equivalent monochromatic, long crested wave. Therefore, several computations were made with and without diffraction. The simulations confirmed that for irregular, short crested waves, the difference in the results with and without diffraction is small and the effect of directional spreading reduces the importance of diffraction. However, the model with the diffraction option enabled predicts the wave heights slightly better than the model without diffraction – although it did not turn out to converge – meaning a gain in the model results with the new phase-decoupled refraction-diffraction approximation.

On the other hand, reflection in a harbor can be of prime importance as the simulations have shown. When a wave hits a vertical wall, most of its energy will reflect from the wall. When it penetrates a harbor entrance, the energy can propagate further into the harbor creating

undesirable oscillations. In the SWAN runs with diffraction and without reflection effects, the values computed were much smaller than the physical model data and, in some situations, the significant wave height in the most sheltered positions was zero. The results indicate that reflection has, comparatively, a greater importance.

With the configurations presented here in, SWAN achieves convergence only when it is not set up to compute diffraction and reflection simultaneously. The best or most probable explanation, according to Holthuijsen (2007), is that the diffraction option should not be used in front of reflecting obstacles, as in the present case. In such situations, stationary waves can occur and phase information is necessary, which is not available. Therefore, in conditions usually found in harbors with broad directional spread, short crested irregular waves, SWAN 40.51 should be implemented without diffraction and with reflection to assure that it will achieve convergence. Naturally, phase resolving models are more appropriate in such situations, however, the rms difference between SWAN estimates without diffraction and with reflection and the physical model data is 10 cm and the mean difference is around 5% of the incident significant wave height. Since SWAN is currently under continuous development, it is expected that such limitations, i.e. the problem of convergence, will be eliminated in future versions of the model.

RESUMO

O modelo de ondas SWAN é amplamente empregado em simulações na região costeira e o presente trabalho investiga sua aplicação dentro de um porto. A última versão disponibilizada para a comunidade – SWAN 40.51 – inclui uma aproximação para computar a difração, embora, até o momento, poucos trabalhos abordando este tema foram publicados. O desempenho do modelo é estudado em um porto onde os fenômenos de reflexão e difração são importantes. Para avaliar suas estimativas, um modelo do tipo Boussinesq também é empregado, juntamente com medições realizadas em um modelo em escala reduzida da área atrás do quebramar. Para ondas irregulares, com cristas curtas e espalhamento direcional mais amplo, a importância da difração é relativamente menor. Contudo, o modelo SWAN não alcança convergência quando programado para estimar difração e reflexão simultaneamente. Conclui-se que, para situações normalmente encontradas em portos, com

ondas irregulares próximas a obstáculos refletivos, o modelo deve ser empregado sem a opção de difração.

Palavras-chave: ondas geradas pelo vento, modelo de geração e propagação de ondas SWAN, reflexão de ondas, difração de ondas, transformação de ondas em um porto.

REFERENCES

- BERKHOFF JCW. 1972. Computation of combined refraction-diffraction. In: Proceedings 13th Int. Conf. Coastal Eng., ASCE, Vancouver, p. 471–490.
- BOUIJ N, RIS R AND HOLTHUIJSEN L. 1999. A third generation wave model for coastal regions – 1. Model description and validation. *J Geophys Res* 104(C4): 7649–7666.
- BRIGGS MJ, THOMPSON EF AND VINCENT CL. 1995. Wave diffraction around breakwater. *J Waterw Port Coast Ocean Eng* 121: 23–35.
- CHELTON DB, RIES J, HAINES BJ, FU LL AND CALLAHAN P. 2001. Satellite altimetry. In: FU LL AND CAZANAVE A (Eds), *Satellite altimetry and earth sciences*. Academic Press, 463 p.
- CHO YS, YOON S, LEE JI AND YOON TH. 2001. A concept of beach protection with submerged breakwaters. *J Coastal Res* 34: 671–678.
- DHI. 1998. MIKE 21 – User guide and reference manual, release 2.7. Technical report, Danish Hydraulic Institute. Denmark, 98 p.
- DINGEMANS MW. 1997. Water wave propagation over uneven bottoms: Part 1 – linear wave propagation. World Scientific, London.
- ENET F, NAHON A, VAN VLEDDER G AND HURDLE D. 2006. Evaluation of diffraction behind a semi-infinite breakwater in the SWAN Wave Model. In Proceedings of Ninth International Symposium on Ocean Wave Measurement and Analysis – WAVES06.
- HANSEN KH, KERPER DR, SORENSEN OR AND KIRKEGAARD DJ. 2005. Simulation of long wave agitation in ports and harbours using a time-domain Boussinesq model. In Proceedings of Fifth International Symposium on Ocean Wave Measurement and Analysis – WAVES 2005. Madrid, Spain.
- HOLTHUIJSEN LH. 2007. *Waves in Oceanic and Coastal Waters*. Cambridge University Press, Great Britain, 387 p.
- HOLTHUIJSEN LH, HERMAN A AND BOUIJ N. 2003. Phase-decoupled refraction-diffraction for spectral wave models. *Coastal Eng* 49: 291–305.

- ILICA S, VAN DER WESTHUYSEN A, ROELVINK J AND CHADWICK A. 2007. Multidirectional wave transformation around detached breakwaters. *Coastal Eng* 54: 775–789.
- INPH. 2003a. The evolution of wave generation systems in INPH. Technical report, Brazilian Waterways Research Institute (INPH). In Portuguese, 53 p.
- INPH. 2003b. Mathematical modeling of wave propagation around and inside the Port of CST. Technical report, Brazilian Waterways Research Institute (INPH). In Portuguese, 27 p.
- LOSADA MA, DALRYMPLE RA AND VIDAL C. 1990. Water waves in the vicinity of breakwaters. *J Coastal Res* 7: 119–137.
- MADSEN P AND SORENSEN O. 1992. A new form of the Boussinesq equations with improved linear dispersion characteristics. Part 2. A slowly-varying bathymetry. *Coastal Eng* 18: 183–204.
- MADSEN P, MURRAY I AND SORENSEN O. 1991. A new form of the Boussinesq equations with improved linear dispersion characteristics. *Coastal Eng* 15: 371–388.
- OCAMPO-TORRES FJ. 2001. On the homogeneity of the wave field in coastal areas as determined from ERS-2 and RADARSAT Synthetic Aperture Radar images of the ocean surface. *Sci Mar* 65(S1): 215–228.
- ROBINSON IS. 2004. *Measuring the Oceans from Space*. Springer-Praxis Books, Great Britain, 669 p.
- ROUSSEAU S AND FORGET P. 2001. Ocean wave mapping from ERS SAR images in the presence of swell and wind waves. *Sci Mar* 68(1): 1–5.
- SORENSEN OR, SCHAFFER HA AND SORENSEN LS. 2004. Boussinesq-type modelling using an unstructured finite element technique. *Coastal Eng* 50: 181–198.
- SWAN TEAM. 2006. *Swan User Manual version 40.51*. Department of Civil Engineering and Geosciences, Delft University of Technology, Delft, The Netherlands, 111 p.
- TOLMAN H. 1991. A third-generation model for wind waves on slowly varying, unsteady and inhomogeneous depths and currents. *J Phys Oceanogr* 21: 782–797.
- TUCKER MJ AND PITT EG. 2001. *Waves in Ocean Engineering*. Elsevier Engineering Book Series, Great Britain, 521 p.
- VIOLANTE-CARVALHO N AND ROBINSON IS. 2004. On the retrieval of two dimensional directional wave spectra from spaceborne Synthetic Aperture Radar (SAR) images. *Sci Mar* 68(3): 317–330.
- VIOLANTE-CARVALHO N, ROBINSON IS AND SCHULZ-STELLENFLETH J. 2005. Assessment of ERS Synthetic Aperture Radar wave spectra retrieved from the MPI scheme through intercomparisons of one year of directional buoy measurements. *J Geophys Res* 110(C07019).
- WAMDI GROUP. 1988. The WAM model. A third generation ocean wave prediction model. *J Phys Oceanogr* 18: 1775–1810.
- YOUNG IR. 1999. *Wind Generated Ocean Waves*. Elsevier, 288 p.
- ZIJLEMA M AND VAN DER WESTHUYSEN AJ. 2005. On convergence behaviour and numerical accuracy in stationary SWAN simulations of nearshore wind wave spectra. *Coastal Eng* 52(3): 237–256.