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## THE GROWING SPACE UTILIZATION OF MAIN TREE SPECIES IN NORTHERN TURKEY

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### HIGHLIGHTS

Maximum size density relationships varied among tree species.

Size density relationships among species was attributed to their shade tolerance.

Species-specific size density relationships is needed for more appropriate stand development approaches.

### ABSTRACT

Relationships between tree size and density are important to define the growing space utilization in a stand. Although a universal slope for the maximum size-density relationships (MSDRs) has been previously suggested, recent research have highlighted that these relationships are species-specific. Oriental beech (*Fagus orientalis* Lipsky), Trojan fir (*Abies nordmanniana subsp.equi-trojani*), black pine (*Pinus nigra* Arnold) and Scots pine (*Pinus sylvestris* L.) represent different crown architecture, growth rate and shade tolerance; however, MSDRs have not been developed for these tree species in northern Turkey. In this study, average maximum density ( $D_{AM}$ ) slopes for these tree species were determined. Results suggested that MSDRs varied among the species, and that their slope differed from the universal slope of -1.605. The MSDRs described in this study are useful for managing stand density in natural stands of the species analyzed.

## INTRODUCTION

Growth and productivity of an individual tree are generally associated with the available growing space, which can be described in terms of stand density (Krajicek et al., 1961; Zeide, 2005). A general relationship between the number of trees and their average size is often described in forestry, average individual tree size decreases when the number of trees per hectare increases (Zeide 1995). The relationship between tree size and their spatial density (i.e., MSDRs) is crucial to describe stand growing space utilization (Lhotka and Loewenstein, 2008), and it has been a topic of research in forestry throughout the history (Cao et al., 2000). Understanding MSDRs helps silviculturists and forest managers manipulate available growing space, and consequently, enhance tree survival and growth (Lhotka and Loewenstein, 2008). Several stand density measures, including stand basal area ( $\text{m}^2\cdot\text{ha}^{-1}$ ), stand volume ( $\text{m}^3\cdot\text{ha}^{-1}$ ) and number of trees per unit area, have been widely used to help allocating growing space during forestry practices (Kara et al., 2017). However, it has also been recommended that MSDRs should be taken into account in estimating the degree of site occupancy and growing space allocation (Comeau et al., 2010).

The model introduced by Reineke (1933) has been one of the most commonly used methods to assess MSDRs in forestry (Newton 1997; del Rio et al. 2001). MSDRs for a tree species, which are frequently used as indication of competition among trees (Gingrich, 1967), are defined using the average maximum stand density ( $D_{AM}$ ) attainable by the species (Reineke, 1933). Reineke (1933) suggested that the slope of these relationships is universal (i.e., -1.605) across all tree species regardless of site quality. However, several studies have revealed that both slope and intercept are species-specific, and may vary in different regions (Solomon and Zhang, 2002; Pretzsch and Biber, 2005; Weiskittel et al., 2009; Comeau et al., 2010; Reyes-Hernández et al., 2013; Bravo-Oviedo et al., 2018). The slope is important because it explains the self-thinning behavior of a tree species (Lhotka and Loewenstein, 2008). Therefore, some scientists have stated that the use of Reineke's (1933) universal slope for every tree species may cause inaccuracy in estimating and controlling stand density (Bazzaz and Grace, 1997; Pretzsch and Biber, 2005). As a consequence, species-specific local observations regarding the MSDRs have been recommended (Comeau et al., 2010).

Oriental beech (*Fagus orientalis* Lipsky), Trojan fir (*Abies nordmanniana* subsp. *equi-trojani*), black pine (*Pinus nigra* Arnold) and Scots pine (*Pinus sylvestris* L.) are

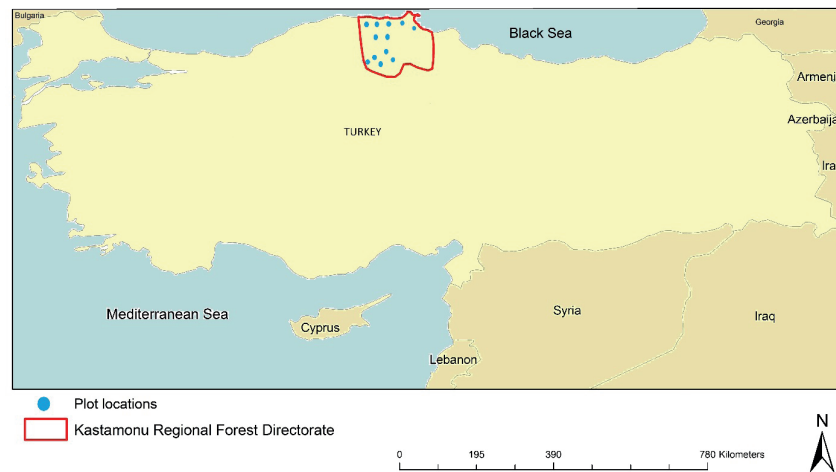
four of the main tree species in Turkey, and native to the northern part of the country. These tree species have economic and ecological importance in Turkish forestry since they provide high-quality timber and represent rich biodiversity (Ertekin and Özel, 2010; Sevik, 2012; Atik, 2013). Approximately 8,800,000 ha are occupied by these tree species, which roughly represents 40% of the total forested land in Turkey (General Directorate of Forestry, 2014). Oriental beech, Trojan fir, black pine and Scots pine have been usually managed using similar silvicultural prescriptions in Turkey, especially using shelter-wood method. However, it has been stated that they represent different crown architecture, growth rate and shade tolerance (Odabaşı et al., 2004). It is unknown whether the MSDRs differ among these tree species.

Several studies have explored the MSDRs for different tree species around the world (Cao et al., 2000; Lhotka and Loewenstein, 2008; Comeau et al., 2010), but, to our knowledge, these relationships have not been studied for the main tree species in northern Turkey. For example; Hynynen (1993) developed MSDRs for Scots pine forests in Finland, but, he stated that this MSDRs may vary for Scots pine stands in different regions. For these reasons, the objectives of this study are to (i) determine the relationships between tree size and stand density for Oriental beech, Trojan fir, black pine and Scots pine trees, and (ii) compare the  $D_{AM}$  slopes among the species, (iii) compare their  $D_{AM}$  slopes with the Reineke's (1933) universal slope of -1.605.

## MATERIAL AND METHODS

The  $D_{AM}$ , in which trees have minimum necessary growing space to survive, has to be estimated from fully-stocked stands (Gingrich, 1967), which are undisturbed stands that are at or near maximum density for their age. To determine the  $D_{AM}$  for Oriental beech, Trojan fir, black pine and Scots pine forests, a database from the Regional Forest Directorate in Kastamonu, Turkey was used (Figure 1). The database was generated from the temporary inventory plots in the region for years 2008 through 2011. Plot sizes are 400 or 600  $\text{m}^2$  depending on the stand density (i.e., larger plots were used to measure stands with less tree density). In the plots, diameter at breast height (DBH) of all trees taller than 1.3 m in height were recorded for each plot. For each species in the database, plots from pure stands in which target species' basal area was  $\geq 90\%$  were selected. Table 1 shows the number of plots selected, and their descriptive statistics by species.

We identified stands that were fully-stocked with the following approach. First, quadratic mean diameter (QMD) and number of trees per hectare ( $N_T$ ) were calculated for each plot (Table 1).



**FIGURE 1** Plot locations and boundary of Kastamonu Regional Forest Directorate in Turkey. Plots are located in Ayancık, Azdavay, Cide, İnebolu, Küre, Sinop, Türkeli, Araç, İhsangazi, Karadere, Samatlar regions.

**TABLE 1** Summary of data from all the inventory plots that were available for this study by species.

Species	n	Variables	Min.	Max.	Mean	SD
<i>Fagus orientalis</i> Lipsky	430	NT	100	2550	830	460.5
		QMD (cm)	10	67.0	24	9.4
<i>Abies nordmanniana</i>	422	NT	100	1650	604	235.4
		QMD (cm)	12.9	51.6	29	5.7
<i>Pinus nigra</i> Arnold	358	NT	75	2550	711	363.8
		QMD (cm)	10.6	52.9	25	6.9
<i>Pinus sylvestris</i> L.	321	NT	50	2275	693	373.4
		QMD (cm)	9.2	49.5	24	8.8

where n is number of plots, and NT= total density (trees ha<sup>-1</sup>).

Further, stand density index - SDI (Reineke, 1933) was calculated with [1], where  $N_T$  is the number of trees per hectare, and QMD is the quadratic mean diameter. Then, the relative stand density -RSD for each plot was calculated with [2] (Drew and Flewelling, 1979).

$$SDI = N_T \cdot \left( \frac{QMD}{25} \right)^{1.605} \quad [1]$$

$$RSD = \frac{SDI_{obs}}{\text{Maximum stand density index attained}} \quad [2]$$

Plots with a relative stand density higher than 0.7 were selected for further analysis, as suggested by Solomon and Zhang (2002). Another reason for choosing the relative stand density higher than 0.7 is to obtain adequate number of plots to define the ( $D_{AM}$ ) (Solomon and Zhang, 2002). Following the selection of fully-stocked plots for each species,  $D_{AM}$  patterns for Oriental beech, Trojan fir, black pine and Scots pine were quantified using Reineke's (1933) model (3). It should be noted that the regression models were fit using only the plots that were fully-stocked, where  $b_0$  and  $b_1$  are the model coefficients.

$$\log_c(N_T) = b_0 - b_1 \cdot \log_c(QMD) \quad [3]$$

As the final step,  $N_T$  and their associated QMD obtained from fully-stocked plots were plotted on a log-log scale to estimate the coefficients of the  $D_{AM}$  models for Oriental beech, Trojan fir, black pine and Scots pine forests. In order to fit the  $D_{AM}$  models, ordinary least square (OLS) regression and reduced major axis (RMA) regression (VanderSchaaf and Burkhart, 2007; Lhotka and Loewenstein, 2008; Comeau et al. 2010) have been commonly used. However, in recent research, it has been suggested that these regression methods may produce inappropriate slopes of  $D_{AM}$  (Zhang et al., 2005). Zhang et al. (2013) stated that quantile regression (QR) gives less biased and more efficient estimates than OLS and RMA when fitting MSDRs. For this reason, QR was used to fit the  $D_{AM}$  models. In order to compare the  $D_{AM}$  slopes of each species with the Reineke's (1933) universal slope of -1.605, a t test was used as suggested by Lhotka and Loewenstein (2008). The "rq" function and "lm" function for fitting the  $D_{AM}$  models and comparing the  $D_{AM}$  slopes of the species, respectively, were utilized in R-Statistical software (R Development Core Team, 2010).

## RESULTS AND DISCUSSION

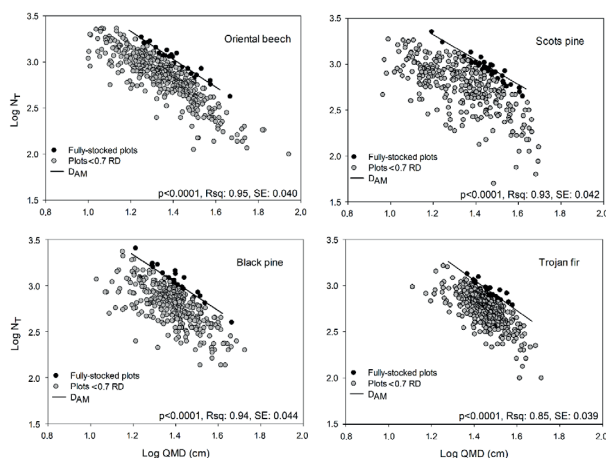
The number of fully-stocked stands varied from 25 to 36 among the species analyzed (Table 2). It should be noted that the study plots are located in different stands. In previous studies, the number of fully-stocked plots used to define the  $D_{AM}$  for different tree species ranged from 9 to 50 plots (Solomon and Zhang, 2002; Pretzsch and Biber, 2005; Lhotka and Loewenstein, 2008; Comeau et al., 2010; Larsen et al., 2010). Thus, in this study, the number of plots used to determine the  $D_{AM}$  fall within the normal range for all tree species. The maximum stand density indexes for the fully-stocked plots were 1390, 1472, 1445 and 1413 for Oriental beech, Trojan fir, black pine and Scots pine, respectively.

**TABLE 2** Descriptive statistics of the fully-stocked stands selected to develop the average maximum stand density (DAM) equations.

Species	nf	Variables	Min.	Max.	Mean	SD
Fagus orientalis L.	25	NT	425	1875	1122	377
		QMD (cm)	17.7	46.4	26	6.9
Abies nordmanniana	31	NT	617	1350	859	183
		QMD (cm)	23.3	37.9	30	3.5
Pinus nigra Arnold	26	NT	400	2550	1189	424
		QMD (cm)	16.2	45.9	26	5.8
Pinus sylvestris L.	36	NT	450	2275	930	340
		QMD (cm)	15.5	41.6	29	5.6

Where nf is number of fully-stocked plots, NT is the number of trees per hectare, SD is standard deviation.

The data utilized to fit the  $D_{AM}$  models for Oriental beech, Trojan fir, black pine and Scots pine are illustrated in Figure 2. As stated before, the relationship between number of trees per unit area and QMD is linear on logarithmic scale as we observed in this study (Figure 2). Stands with a relative density lower than 0.7 appear to be more dispersed for black pine and Scots pine than for the other two species (Figure 2). We believe that this might be the result of their growth behavior, since black pine and Scots pine forests are more shade-intolerant tree species than Oriental beech and Trojan fir. Another reason might be that, the possibility of obtaining pure black pine and Scots pine stands with lower density is higher in northern Turkey (Odabaşı et al., 2004). Although the relationship between number of trees per unit area and QMD is commonly reported with a straight line on logarithmic scale, it should be noted that the shape of the self-thinning line displays a curvilinear trend (Tang et al., 1994; Charru et al., 2012; Fonseca et al., 2017). Zeide (1987) stated that a deviance from the straight line should occur at both ends is expected.

**FIGURE 2** Average maximum stand density (DAM) relationships for each species. NT, QMD, RD and SE refer to trees per hectare, quadratic mean diameter (cm), relative density, and standard error, respectively.

The  $D_{AM}$  model parameters for each species are summarized in Table 3. For black pine and Trojan fir, the slopes were -1.649 and -1.626, respectively, which are steeper than the value -1.605 proposed by Reineke (1933). The slopes for Oriental beech and Scots pine were -1.499 and -1.447, respectively, which are smoother than the Reineke's (1933) universal slope (Table 3). As mentioned before, Reineke (1933) stated that the slope of MSDRs are universal (i.e., -1.605), which means it is species-independent. However, several studies have rejected the idea that the slope and intercept of these models are species independent, and they stated that many factors can influence MSDRs (Solomon and Zhang, 2002; Prethz and Biber, 2005; Weiskittel et al., 2009; Comeau et al., 2010; Reyes-Hernández et al., 2013; Bravo-Oviedo et al., 2018). Our findings also agree with the statement that the slope of size-density models is species-specific (Table 3). In this study, the slopes for Oriental beech, Trojan fir, black pine and Scots pine MSDRs were significantly different from Reineke's (1933) universal slope of -1.605 ( $\alpha=0.05$ ). The self-thinning in a stand can be explained with the slope of size-density models created for that species (Lhotka and Loewenstein, 2008). The use of a universal slope may result in unsuitable formulation of thinning regimes (Pretzsch and Biber, 2005).

The  $D_{AM}$  trends across a range of QMD for Oriental beech, Trojan fir, black pine and Scots pine are illustrated in Figure 3, showing variation for the selected species (Figure 3). When comparing the four species analyzed, the slopes of  $D_{AM}$  are statistically significant across all species ( $\alpha=0.05$ ) (Figure 3); but, there was not statistically significant differences between black pine and Trojan fir ( $\alpha=0.05$ ) (Figure 3).

Black pine had the steepest slope of the three species analyzed (Table 3). Comparisons among species included in this study highlighted that the slopes of  $D_{AM}$  vary among tree species of northern Turkey. It has been suggested that differences of slopes among species can be attributed to their shade tolerance (Pretzsch and Biber, 2005). Oriental beech and Trojan fir are known to be shade tolerant tree species, while black pine and Scots pine are considered semi-tolerant and intolerant to shade, respectively (Odabaşı et al., 2004). Pretzsch and Biber (2005) argue that shade-tolerant species present a steeper slope, but, in this study, black pine has the steepest slope although it is considered a semi-tolerant species (Odabaşı et al., 2004). This can be attributed to black pine's tolerance to shade at young ages. It has been suggested that black pine is more tolerant to shade when young, and they become more intolerant of shade with

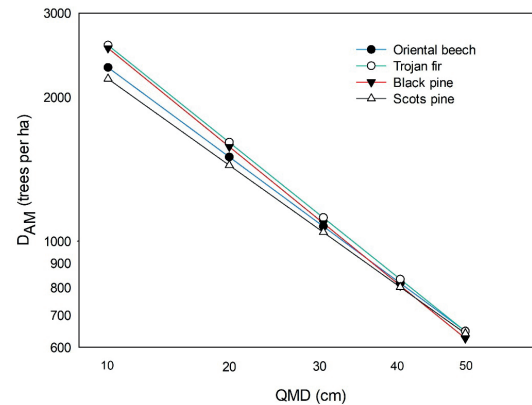
**TABLE 3** Model coefficients for average maximum stand density ( $D_{AM}$ ) equations using fully-stocked plots.  $b_0$  and  $b_1$  are model coefficients, and SE is standard error of estimates.

Species	$b_0$				$b_1$			
	Lower	Estimate	Upper	SE	Lower	Estimate	Upper	SE
<i>F. orientalis</i> L.	4.907	5.127	5.220	0.102	-1.563	-1.499	-1.343	0.072
<i>A. nordmanniana</i>	4.738	5.323	5.628	0.208	-1.832	-1.626	-1.234	0.140
<i>P. nigra</i> Arnold.	5.264	5.344	5.684	0.135	-1.857	-1.649	-1.593	0.096
<i>P. sylvestris</i> L.	4.911	5.042	5.266	0.116	-1.598	-1.447	-1.341	0.079

increasing age (Odabaşı et al., 2004). Another reason for the differences of  $D_{AM}$  among the tree species can be associated with their foliage type, since Vospernik and Sterba (2014) found out that differences between broadleaf and conifer species exist in terms of  $D_{AM}$ .

It should be noted differences of  $D_{AM}$  among the tree species is also variable for small and large stand QMDs (Figure 3), this is, for small stand QMD (i.e., 10 cm), a black pine tree occupies less growing space (i.e., higher  $D_{AM}$ ) while a Scots pine tree occupies more growing space for the same QMD (Figure 3). This indicates that black pine is able to “pack” relatively more trees of a small QMD in the same available growing space. In another words, young black pine trees contributes less crown area and species composition than other tree species as suggested by Hasenauer (1997). However, the amount of growing space occupied by each tree species seems to be similar for large stand QMDs suggesting that the tree species occupy similar amount of growing space when stand QMD is larger than 40 cm (Figure 3).

It has been previously suggested that tree age and site characteristics have negligible effects on slope and intercept of MSDRs (Lhotka and Loewenstein, 2008); however, recent studies have indicated that these relationships may vary depending on regions for a given species (Pretzsch, 2002; Comeau et al., 2010). Our findings also support this statement. Pretzsch and Biber (2005) examined MSDRs for Scots pine forests in Germany, finding that the slope of  $D_{AM}$  was -1.593 which is steeper than the value that what we obtained in our study for the same species (i.e., -1.447). The same authors reported a slope of -1.789 for beech in Germany, which is also steeper than the slope for Oriental beech (-1.626) that we obtained. Moreover, the intercepts for Scots pine and Oriental beech obtained in this study are considerably lower than that observed by Pretzsch and Biber (2005) suggesting the intercept of  $D_{AM}$  is also region specific. This indicates that much smaller basal areas and therefore less dense stands are observed for the same species in Turkey. These support the fact that the slope of the MSDRs might be region specific. As a consequence, results from this study are valid for the species analyzed and constrained within the region where the data were obtained, since it has been also suggested that environment characteristics

**FIGURE 3** Trend of average maximum density ( $D_{AM}$ ) across a range of quadratic mean diameter (QMD) (cm).

may influence the MSDRs for a tree species (Bi, 2001; Weiskittel et al., 2009; Comeau et al., 2010).

In addition to the effects of region on the slope and intercept of MSDRs, recent studies have revealed that many other factors can influence the MSDRs (Weiskittel et al., 2009; Comeau et al., 2010; Reyes-Hernández et al., 2013; Bravo-Oviedo et al., 2018). Weiskittel et al. (2009) found that site index, stand origin and site aspect influenced the slope of MSDRs for Douglas-fir (*Pseudotsuga menziesii* var. *menziesii* [Mirb.] Franco), western hemlock (*Tsuga heterophylla*), and red alder (*Alnus rubra* Bong.). In another study, Reyes-Hernandez et al. (2013) observed MSDRs of pure and mixed stands of trembling aspen (*Populus tremuloides* Michx.) and white spruce (*Picea glauca* (Moench) Voss.) in Canada, and stated that MSDRs can be affected by site quality, stand composition and soil nutrients. Shade tolerance and drought tolerance of tree species are also known to have significant influence on the slope of MSDRs (Pretzsch and Biber, 2005; Bravo-Oviedo et al., 2018).

On the other hand, relationships reported here for pure stands, should not be used and applied in mixed stands, or be cautiously applied if needed. In addition to pure Oriental beech, Trojan fir, black pine and Scots pine forests mixtures of the same species are common in northern Turkey (Odabaşı et al., 2004). In this regard, Lhotka and Loewenstein (2008) suggested that a mixed stand can be treated as a single-species stand if the species are functionally similar, but also that, relative density metrics



are needed when the mixtures contain dissimilar species. Therefore, the application of MSDRs reported here will depend on the specific mixture of species that is found.

Weller (1990) suggested two different thinning lines; static and dynamic thinning lines. The static thinning line is defined using observations from many different stands of a species regardless of age and other factors, while the dynamic thinning line is determined using observations in an individual crowded stand (Weller, 1990; Reyes-Hernandez et al., 2013). Some factors such as site quality, climate, and stand composition can influence dynamic thinning line, but, static thinning line is proposed to be constant for all stands of a given species (VanderSchaaf and Burkhart, 2007). In this study, the analysis of MSDRs have been based on the a static thinning line, thus, determination of dynamic thinning lines for the species examined are recommended in future studies.

## CONCLUSION

Four economically important tree species of northern Turkey were compared in terms of their growing space utilization. Our results suggest that the MSDRs vary among tree species, and that the slope of these relationships is different from the universal slope of -1.605 suggested by Reineke (1933). Findings of this study highlighted the necessity of developing species-specific size density relationships for more appropriate stand development approaches. These results should not be utilized for the subject species located in other regions, since environment and other factors may influence MSDRs. The  $D_{AM}$  models reported here can be utilized to create stand density management tools, such as stocking charts and density management diagrams. Due to the importance of MSDRs for mixed stands, we recommend the development of  $D_{AM}$  models for mixed stands of Oriental beech, Trojan fir, black pine and Scots.

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