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# Alternative Fuels Mixture in Cement Industry Kilns Employing Particle Swarm Optimization Algorithm

*Most of the works accomplished in the optimization area in the cement industry are addressed to solve problems just considering only one variable, forgetting that it includes too many variables and they act at the same time. Among the main variables it can be mentioned the quality of the final product, the environmental ones, the costs along the process and the reduction of the fossil fuels (primary) employed through the use of alternative fuels (secondary), among others. The present work intends to build a mathematical model using optimization tools seeking to improve the cement production process foreseeing what can happen with the clinker and the emissions when the industrial residues co-processing technology is used as alternative or secondary fuel. In the optimization process a new approach called Particle Swarm Optimization (PSO) is employed, which is based on the Cauchy and Gauss distribution considering several process restrictions such as the specific fuel consumption, the cement quality and the environmental impact. The results obtained with PSO were precise and promising and they were compared with the classical Sequential Quadratic Programming (SQP). It was also possible to evaluate the levels of primary fuels substitution through the alternative or secondary ones.*

**Keywords:** portland cement, industrial co-processing residues, particle swarm optimization (PSO), sequential quadratic programming (SQP).

## Introduction

Nowadays, the Portland cement is the main cement type used all over the world and its production is the largest in amount if compared to the other products produced by men (Chatterjee, 1993). The Portland cement is composed of clinker and additions. The clinker is the main component and it is present in all types of Portland cement. The additions can vary from each cement type to another and they mainly define the different cement types. The production process of the Portland cement is presented in Fig.1. The clinker, base component of the Portland cement, is obtained from the grinding, homogenization and subsequent burn in high temperatures (1450°C) inside a rotary cement kiln starting from a powdered mixture called raw, originating from the following raw materials: limestone, clay, sand, iron ore, etc. The main chemical elements that constitute the clinker are the lime (CaO) and the silica (SiO<sub>2</sub>) that react between themselves forming lime silica, which is the main active component of the cement.

However, other materials can be used on the cement Portland production (Peray and Wadell, 1972). In the search for lower production costs, the cement industries have been trying to modernize their industrial plants, through the construction of new industrial units, which incorporate new production technologies. The introduction of secondary materials either as raw materials or in the co-processing, allows sensitive reduction in the final product cost. This fact contributes as a partial solution for the industrial waste disposal problems to a large number of companies. Also, the introduction of secondary materials provides additional revenue for the cement factories, either due to their low acquisition costs, or due to the payment received for the service of thermal waste destruction. However, the introduction of secondary materials must be subject to the desired final product quality, which is the most important control parameter in the cement Portland production. Moreover, when

industrial residues are used as secondary fuels in the rotary kilns, the generated ashes replace some of the components of the raw materials, and therefore these ashes must be made compatible with the remaining raw materials, in order to be absorbed in high percentage in the clinker matrix (Carvalho, 1997).

This work presents a formulation for the mixture optimization of coal, petroleum coke and used tires. This mixture is intended for use in a rotary kiln of clinker production, dry via, with a four stages pre-heater. However, the problem involving mixture of these components is complex. The optimization procedure takes into account process restrictions such as specific heat consumption, cement quality and environmental impact. In this case, the mixture optimization in cement kilns is a problem with nonlinear cost function with linear constraints.

## Nomenclature

- A,B = constants that depend on the clinker composition, dimensionless  
 $c_1, c_2$  = positive constants, dimensionless  
 MS = silica modulus, dimensionless  
 $p_i$  = position of the best objective value on the  $i$ -th particle, dimensionless  
 $p_{ic}$  = raw material and fuel cost, US\$/t  
 $p_E$  = electricity cost, US/MWh  
 S = specific surface, m<sup>2</sup>/g  
 ud, Ud = functions for random numbers generation in range [0,1]  
 $v_i$  = velocity of the  $i$ -th particle, dimensionless  
 w = inertia factor, dimensionless  
 Cauchy = function that generates a random number with Cauchy distribution for the "social" component  
 Gauss = a random number generated with Gauss distribution with average zero and unitary variance

## Subscripts

- $x_i$  = position of the particle

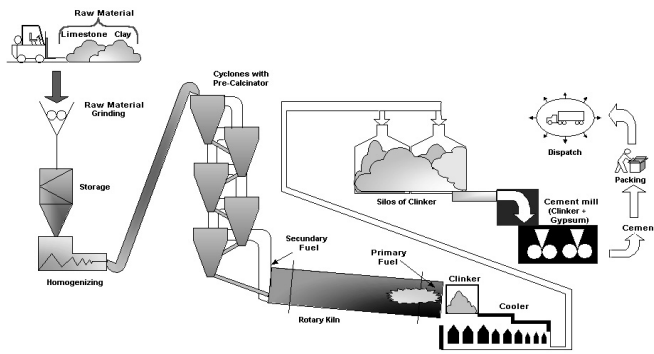


Figure 1. Stages of the Portland cement process production

**Fuels in the Cement Industry**

Due to the high heat consumption in the process, the cement industry always worried about using fuels of low cost, but without losing the quality of the final product. One of the alternatives found to obtain the economy of the energy resources was the co-processing of industrial wastes, also denominated alternative or secondary fuels (Hansen, 2003). The process consists basically in the replacement of a part of the traditional fuel for residues generated by other industries such as useless tires, waste oils and sludge of hazardous and industrial waste treatment, among others (Kleppinger, 1993). In Brazil, the cement industries are using the petcoke as main fuel due to its low cost jointly with the industrial residues (alternative fuels), Fig. 2.

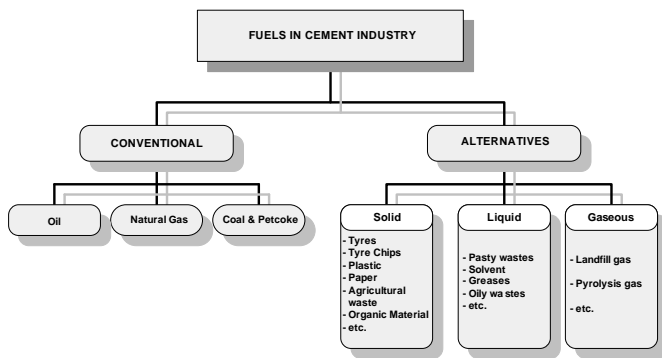


Figure 2. Fuels employed in cement industries.

**Grinding in the Cement Industry**

As described previously, the composed cements contain other added constituents that should be mixed in the phase of clinker grinding. In this case, the grinded product should be inside a certain granulometry limit in such a way to create better conditions for the hardening process (Duda, 1977). Approximately 30% of the energy required to produce a ton of cement is consumed in the grinding. This is a significant percentage of the total cement cost. The energy consumed in the mills is in the range of 16,5 - 63,5 kWh/t with an average of 36 kWh/t (Tokyay, 1999). There is a relationship between the required energy in the grinding phase and the specific surface (Tokyay, 1999). The larger the thinness of the cement (granulometry) is, the bigger will be the specific surface, and as a consequence, there will be a larger consumption of energy (Fig. 3) (Zhang and Napier-Munn, 1995).

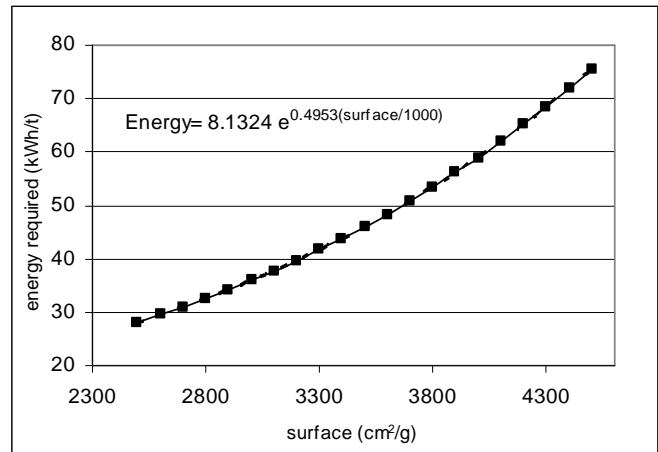


Figure 3. Energy required rate versus specific surface (Tokyay, 1999).

**Model Description and Methodology**

**Optimization Problem Description**

The modeling will use optimization algorithms, of which objective is to assure a better stability of the kiln operation, energy consumption reduction and environmental impact minimization. The following aspects will be modeled:

- a) The effects that the use of alternative fuels can cause:
  - in the clinker quality, through the material and fuel chemical composition;
  - in the environment, through the raw material and fuel emissions of CO<sub>2</sub> and SO<sub>2</sub>;
  - in the clinker production cost, considering the raw material and fuels costs; obtaining as result a optimum composition of raw material and fuels for the clinker production.
- b) The cost and electric power consumption requested in the grinding process for the Portland cement production (Tokyay, 1998). The grinded product should be inside a certain granulometry limit in such a way to create better conditions for the hardening process (Duda, 1977). The equation that represents the electric power requested in the grinding process should be expressed in function of the specific surface and the mixture control modules.

To accomplish the modeling it is necessary to know the input parameters data (raw materials, fuels, raw materials costs, etc), and these should be addressed in function of the proposed objective getting as results the costs optimization, environmental impact minimization, among others. In the work of Carpio et al. (2005) a flowchart is presented, which shows the procedure that will be necessary to accomplish to model the proposed system (Fig. 4).

**Building the Model of the Mixture of the Raw Materials and Fuels**

In order to build the optimization model it is necessary to obtain data as well as to identify the more important decision variables that represent the mixture. These can be obtained starting from the raw material and fuels chemical composition (to see Tab. 1 and Tab. 2).

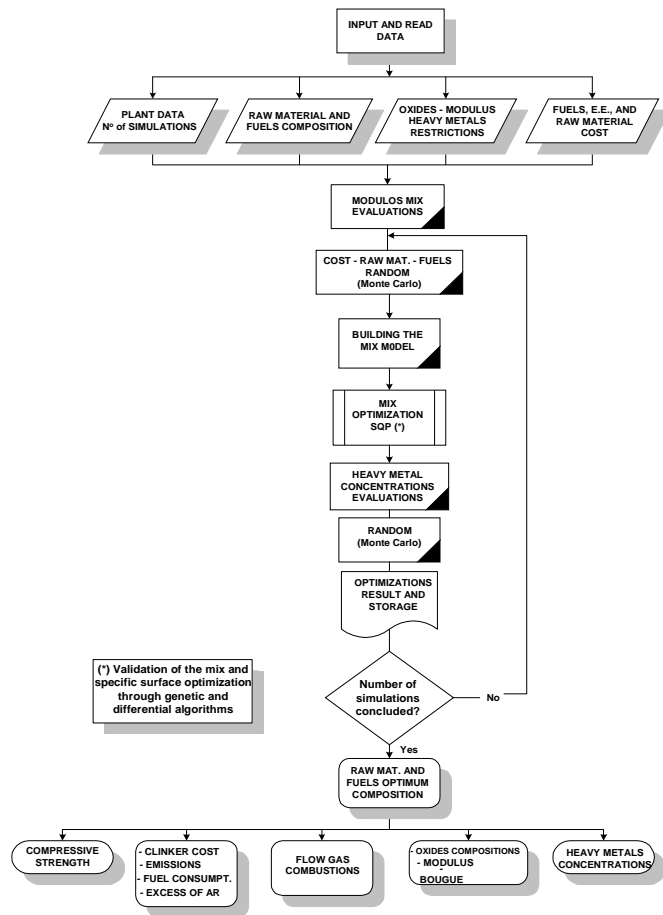


Figure 4. Flowchart when the industrial wastes co-processing is employed (Carpio, 2005).

The mixture optimization should consider the stable operation of the rotative kiln, the quality of the clinker produced, the minimum cost of the used composition and the electric power; all these variables are considered in the nonlinear model proposed through the following objective function, Eq.(1).

$$C = \sum_{i=1}^n p_{iC} \cdot X_i + p_E \cdot A \cdot \exp^{(B \cdot S)} \quad (1)$$

The objective function (C) of the model should try to obtain a minimum cost in the clinker production, considering the raw materials costs as well as the consumption of the energy required for grinding.

The first term (linear) represents the raw materials and fuels (primary and alternative) costs used in the clinker production ( $p_i$ , is the raw materials and fuels costs  $i = 1, 2, \dots, n$ , that participate in the burn with their respective percentages  $X_1, X_2, \dots, X_n$ ).

The second term (nonlinear) represents electricity cost ( $p_E$ ) and the energy consumption required in kWh/t for the grinding process of a certain specific surface (S is the area of the specific surface in  $cm^2/g$ , A and B are constants that depend on the clinker composition). Based on Tab.1 and Tab. 2 values and on the Eq. (1), an objective function was set up, which represents costs minimization problem, considering the operational and environmental costs presented as it follows:

Table 1. Meal raw materials chemical composition (% in weight) (Carpio, 2005)

Material	Notation	CaO	SiO <sub>2</sub>	Al <sub>2</sub> O <sub>3</sub>	Fe <sub>2</sub> O <sub>3</sub>	MgO	SO <sub>3</sub>	Na <sub>2</sub> O	K <sub>2</sub> O
Limestone	X <sub>1</sub>	50.66	5.04	1.19	0.67	0.78	0.1	0.1	0.3
Clay	X <sub>2</sub>	1.23	61.62	16.59	9.01		0.3	0.3	5
Sand	X <sub>3</sub>	1.13	93.00	2.87	1.20	0.10	0.5	0.5	1
Iron ore	X <sub>4</sub>	0.71	7.60	1.13	82.97	-	-	-	-

Table 2. Fuels composition employed as primary and secondary (ABCP, 2002)

Component	Mineral Coal % weight	Petcoke % weight	Tires uses % weight
Notation	X <sub>5</sub>	X <sub>6</sub>	X <sub>7</sub>
C	63.9	80 – 100	72.15
H	3.6	3.5	6.74
S	4.6	0.5 – 7.0	1.23
O	0.9		9.67
N	1.8	1.5	0,36
Cl	-		0.149
Zinc	0.04	1 – 85 ppm	
Cadmium	0.001	1 ppm	0.0006
Lead	0.027	1 – 10 ppm	0.0065
Thallium	0.0004	1 – 80 ppm	0.00001
Arsenic	0.00017	0.1 – 10 ppm	
LHV [kJ/kg]	25.392	32.447	32.100

$$\text{Min } \text{Cost}_1 X_1 + \text{Cost}_2 X_2 + \text{Cost}_3 X_3 + \text{Cost}_4 X_4 + \text{Cost}_5 X_5 + \text{Cost}_6 X_6 - \text{Cost}_7 X_7 + \text{Cost}_{EE} \cdot \{(5,76(\text{MS}) - 5,82) \cdot e^{-(0,2(\text{MS}) + 0,98)^{0,5}}\} \quad (2)$$

$$\text{where } \text{MS} = \frac{5.04 X_1 + 61.62 X_2 + 93 X_3 + 7.6 X_4 + 9.32 X_5 + 1.93 X_7}{1.86 X_1 + 25.6 X_2 + 4.07 X_3 + 84.1 X_4 + 12.29 X_5 + 0.92 X_7}$$

Subject to:

$$50.60 X_1 + 1.23 X_2 + 1.13 X_3 + 0.71 X_4 + 1.03 X_5 + 0.93 X_7 \geq 63.76 \quad (3)$$

$$50.60 X_1 + 1.23 X_2 + 1.13 X_3 + 0.71 X_4 + 1.03 X_5 + 0.93 X_7 \leq 70.14 \quad (4)$$

$$5.04 X_1 + 61.62 X_2 + 93 X_3 + 7.6 X_4 + 9.32 X_5 + 1.93 X_7 \geq 19.71 \quad (5)$$

$$5.04 X_1 + 61.62 X_2 + 93 X_3 + 7.6 X_4 + 9.32 X_5 + 1.93 X_7 \leq 24.25 \quad (6)$$

$$1.19 X_1 + 16.59 X_2 + 2.87 X_3 + 1.13 X_4 + 5.08 X_5 + 0.79 X_7 \geq 3.76 \quad (7)$$

$$1.19 X_1 + 16.59 X_2 + 2.87 X_3 + 1.13 X_4 + 5.08 X_5 + 0.79 X_7 \leq 6.78 \quad (8)$$

$$0.67 X_1 + 9.01 X_2 + 1.2 X_3 + 82.97 X_4 + 7.21 X_5 + 0.13 X_7 \geq 1.29 \quad (9)$$

$$0.67 X_1 + 9.01 X_2 + 1.2 X_3 + 82.97 X_4 + 7.21 X_5 + 0.13 X_7 \leq 4.64 \quad (10)$$

$$0.78 X_1 + 0.10 X_3 + 0.44 X_5 + 0.12 X_7 \leq 6.5 \quad (11)$$

$$0.762 X_1 + 2.74 X_2 + 83.64 X_3 - 185.83 X_4 - 18.96 X_5 - 0.186 X_7 \geq 0 \quad (12)$$

$$-0.018 X_1 + 7.5 X_2 - 82.011 X_3 + 219.47 X_4 + 23.88 X_5 + 0.554 X_7 \geq 0 \quad (13)$$

$$0.319X_1 + 4.877X_2 + 1.31X_3 - 106.73X_4 - 4.29X_5 + 0.621X_7 \geq 0 \quad (14)$$

$$0.619X_1 + 7.737X_2 + 0.37X_3 + 222.88X_4 + 14.387X_5 - 0.439X_7 \geq 0 \quad (15)$$

$$38.24X_1 - 155.67X_2 - 173.6X_3 - 164.34X_4 - 37.86X_5 - 4.2X_7 \geq 0 \quad (16)$$

$$-35.48X_1 + 190.65X_2 + 212.43X_3 + 201.0X_4 + 46.51X_5 + 5.34X_7 \geq 0 \quad (17)$$

$$25392X_1 + 34436X_6 + 32100X_7 = 3600 \quad (18)$$

$$0.046X_5 + 0.07X_6 + 0.0123X_7 \leq 0.05 \quad (19)$$

$$0.1X_1 + 3X_2 + 0.5X_3 \geq 0.20 \quad (20)$$

$$0.1X_1 + 3X_2 + 0.5X_3 \leq 2.07 \quad (21)$$

$$0.1X_1 + 0.3X_2 + 0.5X_3 \geq 0.03 \quad (22)$$

$$0.1X_1 + 0.3X_2 + 0.5X_3 \leq 0.33 \quad (23)$$

$$0.3X_1 + 5X_2 + X_3 \geq 0.31 \quad (24)$$

$$0.3X_1 + 5X_2 + X_3 \leq 1.76 \quad (25)$$

$$A_5X_5 + A_6X_6 + A_7X_7 \leq 0.10 \quad (26)$$

$$B_5X_5 + B_6X_6 + B_7X_7 \leq 0.35 \quad (27)$$

$$C_6X_6 \leq 0.05 \quad (28)$$

$$D_5X_5 + D_6X_6 + D_7X_7 \leq 0.10 \quad (29)$$

The Equations from 3 to 10 represent the operational restrictions, where the amount of CaO should stay between 62 and 67% Eq.(3) and Eq.(4), SiO<sub>2</sub> between 19 and 25% Eq.5 and Eq.(6), Al<sub>2</sub>O<sub>3</sub> between 2 and 9% Eq.(7) and Eq.(8) and Fe<sub>2</sub>O<sub>3</sub> between 1 and 5% Eq.(9) and Eq.(10). The maximum amount of magnesium should be limited in 6.5% Eq.(11). Equations (12) to (17) are the restrictions of the mixture control modules regarding to the clinker quality (Carpio et al., 2004). The total fuels feeding should assist the heat specific consumption presented in Eq. (18). The restriction regarding to the sulfur is presented in Eq. (19). Equations (20) and (21) represent the limits for the trioxide of sulfur (SO<sub>3</sub>) contained in the raw material. The restrictions of the Equations (22) to (25) are referred to the alkalis in the raw material. The more volatile and dangerous heavy metals, such as the cadmium, lead, mercury and thallium, are controlled by the restrictions of the Equations (26) to (29). More details about the restrictions can be found in Carpio (2005).

### Particle Swarm Optimization Method (PSO)

PSO is an approach of collective intelligence (swarm intelligence) and it was developed initially by Kennedy and Eberhart (Kennedy and Eberhart, 1995; Eberhart and Kennedy, 1995; Kennedy et al., 2004) based on the studies of the social-biologist Edward Osborne Wilson. The proposal of PSO algorithm was put forward by several scientists who developed computational simulations of the movement of organisms such as birds flocks and fish schools. Such simulations were heavily based on manipulating the distances between the individuals, i.e., the swarm behavior

synchrony is seen as an effort to keep an optimal distance between them.

In theory, at least, individuals of a swarm may benefit from the prior discoveries and experiences of all the members of a swarm when foraging. The fundamental point of developing PSO is a hypothesis in which the exchange of information among creatures of the same species offers some sort of evolutionary advantage.

PSO presents characteristics similar to the evolutionary computation techniques (Goldberg, 1989), which are based on a population of solutions. However, PSO is motivated by the simulation of social behavior and cooperation among agents instead of the most capable individual's survival as in the evolutionary algorithms. In PSO, each candidate solution (denominated particle) has an associated velocity. The velocity is adjusted through an updating equation that considers the experience of the corresponding particle and the experience of the other present particles in the population.

The concept of PSO consists of, to each iterative step, changing the velocity of each particle towards the *pbest* (personal best) and *gbest* (global best) locations. The velocity of the search procedure is pondered through a generated term in a random way linked in a separate way of the *pbest* and of the *gbest* locations.

The procedure for PSO implementation is governed by the following stages:

(i) begin a population (matrix) of particles, with positions and velocity in a space problem of *n* dimensional, randomly with uniform distribution.

(ii) for each particle, evaluate the fitness function (objective function);

(iii) compare the evaluation of the particle aptitude function with the *pbest* of the particle. If the average value is better than the *pbest*, then the *pbest* value becomes the value of the aptitude function and the *pbest* location becomes the same of the current location in the *n* dimensional space;

(iv) compare the aptitude function evaluation with the best previous value of the population aptitude. If the current value is better than the *gbest*, update the *gbest* value for the index and current particle value;

(v) modify the velocity and the position of the particle in agreement with the equations (Shi and Eberhart, 1998; Kennedy et al., 2001):

$$v_i = w \cdot v_i + c_1 \cdot ud \cdot (p_i - x_i) + c_2 \cdot Ud \cdot (p_g - x_i) \quad (30)$$

$$x_i = (x_i + \Delta t \cdot v_i) \quad (31)$$

where  $\Delta t$  is 1.

(vi) go to the stage (ii) until a stop criterion is found. It is usually used a pre-defined error or a maximum number of iterations (generations).

The used notations are:  $x_i = [x_{i1}, x_{i2}, \dots, x_{in}]^T$  which stores the *i*-th position of the particle,  $v_i = [v_{i1}, v_{i2}, \dots, v_{in}]^T$  which stores the *i*-th velocity of the particle and  $p_i = [p_{i1}, p_{i2}, \dots, p_{in}]^T$  which represents the position of the best fitness value of the *i*-th particle. The index *g* represents the index of the best value among all of the particles of the group. The variable *w* is the inertia factor, *c*<sub>1</sub> and *c*<sub>2</sub> are the cognitive and social components, respectively, which are the acceleration constants responsible for varying the particle speed towards *pbest* and *gbest*, respectively; *ud* and *Ud* are two functions for random numbers generation with uniform distribution in the interval [0,1], respectively. The particles velocity of each dimension is limited to a maximum value of velocity, *V*<sub>max</sub>.

The first part in the Eq. 30 is a term of the particle moment. The weighted inertia *w* represents the particle moment degree. The second part consists of the "cognitive" part, which represents the

independent "knowledge" of the particle. The third part is the "social" one, which represents the co-operation among the particles.

The  $c_1$  and  $c_2$  represent the weighted of the "cognition" and "social" parts that influence each particle toward  $p_{best}$  and  $g_{best}$ . These constants are usually adjusted by try and error heuristics attempts. The population size is also selected depending on the dimension of the approached problem.

In classical PSO approaches, a uniform probability distribution is used to generate random numbers to update the velocity equation. However, the use of other probability distributions may improve the ability to fine-tune or even escape from local optima. In the meantime, it has been proposed that the Gaussian and/or Cauchy probability distributions be used to generate random numbers to update the velocity equation (Miranda and Fonseca, 2002; Wei et al., 2002; Secrest et al., 2003; Stacey et al., 2003; Esquivel and Coello, 2003; Higashi and Iba, 2003; Coelho and Krohling, 2005; Ting et al., 2006; Krohling and Coelho, 2006, Coelho and Alotto, 2008; Coelho and Lee, 2008).

The PSO approach proposed in this work, denominated of PSO-CG, seeks to modify the equation (30) of the conventional PSO for:

$$v_i = w \cdot v_i + c_1 \cdot \text{Cauchy}(p_i - x_i) + c_2 \cdot \text{Gauss}(p_g - x_i) \quad (32)$$

where Cauchy is a function that generates a random number with Cauchy distribution for the "social" component and Gauss generates a random number with Gauss distribution with average zero and unitary variance for the "cognitive" component of PSO.

The use of Cauchy distribution in PSO can be useful to avoid local minima when the search space is small, while the Gauss (normal) distribution (truncated in [0,1] in this paper) can supply a faster convergence in local searches when the search space is big (Chellapilla, 1998).

## Results and Analysis

### Simulation Results

The results for the optimization nonlinear evaluation using conventional PSO, PSO-CG and Sequential Quadratic Programming (SQP) are summarized in Table 3 (run 30 experiments with each optimization technique). In this case, the required chemical composition is sought for a cement type produced in a rotative kiln, dry via, with heat specific consumption of 3600 clinker kJ/kg.

Table 3. Equation 2 (30 experiments) objective function optimization results

Optimization method	Best	Worst	Average	Standard deviation	Time*
SQP	4.761624	4.761624	4.761624	0.000000	0.023
PSO	4.731781	10.66206	6.177593	2.329706	14.33
PSO-CG	4.713311	5.477078	4.713310	0.316630	22.84

\* time (in seconds) to run each experiment in a PC computer (1,09 GHz AMD 4, 124 MB RAM with Matlab 6.5)

Table 4. Optimization model results employing PSO-CG

Objective Function C = US\$4.713311/ton	Oxides compositions in Clinker (%)	Modulus	Specific heat consumption = 3600 (kJ/kg clk*)
Compositions (kg/kg Clk*)			Consumption of fuels (kg/tonclk*)
$X_1 = 1.2175$	CaO = 62.07		
$X_2 = 0.2007$	SiO <sub>2</sub> = 20.13	MS = 2.50	Petroleum Coke = 74.1
$X_3 = 0.0161$	Al <sub>2</sub> O <sub>3</sub> = 5.22	MA = 1.82	Used tires = 28.0
$X_4 = 0.0000$	Fe <sub>2</sub> O <sub>3</sub> = 2.86	MH = 2.20	* Clk: Clinker
$X_5 = 0.0000$	MgO = 0.95		
$X_6 = 0.0741$			
$X_7 = 0.0280$			

Table 3 presents the medium, minimum, maximum and the standard deviation values results. The parameters of PSO and PSO-CG used a population of 30 particles;  $c_1 = c_2 = 2.05$ ; initial weighted  $w$  of 0.729 with linear decline up to 0.400; search space of the variables to be optimized in the interval  $0 < X_n < 3$ , where  $n=1, \dots, 7$ ;  $V_{max}$ : 20% of the search space of each variable; and maximum number of generations (stop criterion): 500 generations. SQP uses a Hessian matrix approach (of the function Lagrange) and it uses a Quasi-Newton's method and line search for minimization of the cost function (Fletcher, 1987; Nash and Sofer, 1996; Boggs and Tolle, 2000).

It is noticed that the obtained results using PSO-CG and SQP is quite close, with a little advantage of PSO-CG in terms of answer quality. However, SQP, in spite of not finding the optimum value, is faster in terms of computational cost and with smaller standard deviation than PSO and PSO-CG.

## Conclusion and References

Through the optimization model presented, it is possible to foresee the raw composition when it is decided to burn residues as secondary fuels in cement industries rotary kilns. It is also possible to calculate the substitution levels of the primary fuel by alternative fuel derived from industrial wastes, being considered the acceptable pollutant emissions levels (sulfur for example). This model was shown satisfactory based on the presented results, either for keeping the values of chemical composition inside the quality parameters or finding smaller production costs. Regarding the optimization procedure, the results with PSO-CG and SQP were precise and promising. The disadvantage of PSO-CG in relation to SQP was the largest computational cost for the convergence.

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