

# Polarization Insensitive Compact Wide Stop-band Frequency Selective Surface

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**Abstract**— A compact, polarization insensitive, wide stop band frequency selective surface is presented. The unit cell is designed by modifying the basic square loop FSS. The simulated value of bandwidth for transmission  $< -20$  dB for TE incident wave is 7.7 GHz from 4.71 GHz to 12.41 GHz which is 89.95% corresponding to the center frequency of this range. It has an excellent band stop response for C and X band. The periodicity of the unit cell is the order of  $0.33\lambda_0$  at the center frequency of 8.56 GHz. The total thickness of the proposed structure is 1.6mm ( $0.045\lambda_0$ ). Standard design formulas are used to evaluate the resonance frequencies and calculated values are found to be very close to the simulated ones. The proposed design is polarization insensitive and has good angular stability. An array of the proposed design is fabricated on either side of dielectric substrate FR4. The measured and simulated transmission responses are in good agreement. Proposed design can be used for many potential applications such as electromagnetic shielding, spatial filtering, sub - reflector in antennas and RCS reduction etc.

**Index Terms**— Frequency selective surface, polarization insensitive, compact, wideband, band stop.

## 1 INTRODUCTION

Electromagnetic band gap (EBG) structures [1], partially reflective surfaces (PRSS) [2], and artificial magnetic conductors (AMCs) [3] are extensively investigated for their variety of applications in microwave and millimeter wave regimes. A perfect design of the ground plane beneath the antenna attracts much of the attention due the challenge of improving the various characteristics such as gain, bandwidth and directivity etc. AMCs and PRSSs such as Frequency Selective Surfaces (FSSs) [4-6] are used as the ground plane to improve the aforementioned characteristics of the antenna. FSSs are also used as dichroic sub-reflectors in dual frequency antennas, superstrate in antennas to increase directivity, for radar cross section reduction, as polarizers and spatial filters. They are also used as a special reflector to maintain purity of signal transmitted or received in satellite communication.

FSSs are usually designed to give frequency responses like band stop, band pass, high pass and low pass spatial filter [7]. Their performance depends upon an element type, its shape, size, periodicity, polarization, incident angle and thickness of the dielectric layer [8]. Conventional FSS shapes, such as loop type, center connected and solid interiors are limited in their performance due to narrow transmission bandwidth for

incident waves. Use of multiple FSS layers to achieve wide transmission response is a common approach [9-11]. This makes the structure unsuitable for planar applications due to increase in its overall thickness. However, loop type FSSs are highly investigated due their wideband response. Square Loop type FSSs have been analyzed and synthesized using several techniques [12-14]. A wide stop-band cascaded frequency selective surface by using koch fractal elements is proposed in [15]. In this, wide stop band is achieved by cascading two FSS screens of 1.27mm thick each, with an air gap of 2mm, which increases its overall thickness. Similarly, a wide stop band FSS is presented in [16]. It is a single layer design, but the substrate used is of large thickness (3.2 mm), which limits its use for planar applications. A thin, compact, symmetric and ultra-wide stop band FSS is proposed in [17] but it covers only 3.5 GHz of (-20db transmission) bandwidth in ultra-wide band range. Another wide stop band FSS design has been proposed in [18]. However, it is polarization insensitive but its substrate thickness is large and its -20dB transmission bandwidth is almost nil. A compact, ultra wide band square loop FSS has also been proposed in [18]. It covers 8 GHz of -20db transmission bandwidth, but it lacks in rotational symmetry which makes it sensitive to incident wave polarization and its center frequency varies w.r.t different incident angles.

In this paper, a compact and polarization insensitive FSS, with a wide stop band characteristics has been designed. Periodicity of the unit element is nearly  $0.33\lambda_0$ . The design has rotational symmetry which helps to achieve polarization insensitivity. Thickness of the proposed FSS is  $0.045\lambda_0$  at center frequency of 8.56GHz, which is much smaller than the conventional multilayer FSS. Proposed FSS can be used for bandwidth enhancement of antennas, as reflecting surface and microwave shield for C and X bands. All analysis has been carried out using the Ansoft's HFSS v.14. A prototype of the proposed FSS is fabricated on both sides of dielectric FR4 ( $\epsilon_r = 4.4$ ).

The presented paper is organized as follows: Section II describes the theory of operation and FSS design. Section III outlines the simulation results with parametric analysis of the FSS and in section IV experimental verifications are outlined with a comparison with simulation results. In section V the work is summarized in a brief conclusion.

## 2 DESIGN & SIMULATION

The unit cell of the proposed FSS is shown in *Fig. 1(a)*. Initially, a single square loop FSS has been formed and then we modify the design proposed in [18] and made a rotational symmetric structure to achieve polarization insensitivity. It consists of top and bottom metallic layers of a 2-D periodic array, of modified square loop patches as illustrated in *Fig. 1(b)*. The overall size of the single unit cell is  $11.5\text{mm} \times 11.5\text{mm}$ , which is equal to  $0.33\lambda_0$ . The optimized dimensions are  $L = 6\text{mm}$ ,  $L_1 = 4\text{mm}$ ,  $L_2 = 3.5\text{mm}$ ,  $W = 2.5\text{mm}$  and  $W_1 = 1\text{mm}$ . The overall thickness of structure is 1.6 mm. For achieving compactness, the conventional square loop type FSS structure is modified by cutting the slots of the size  $W_1 \times L_1$  symmetrically. The slot cutting increases the current path. The surface current distributions of the conventional and proposed FSSs for their transmission null frequencies are shown in *Fig. 2(a)* and *Fig. 2(b)*, respectively. It is observed that

the cutting of slots results meandering in the path as compared to a normal conventional square loop and the currents has travel longer paths. Due to this increase in current path the proposed FSS exhibits lower resonance frequency in comparison to the conventional square loop as shown in Fig. 3(a). Proposed FSS provides two transmission nulls ' $f_1$ ' and ' $f_2$ ' of 5.0 and 9.67 GHz respectively with -20dB transmission bandwidth of 7.7 GHz. The simulated phase response has also been investigated as represented in Fig. 3(b). The phase changes linearly over the wide stop band exhibited by the proposed FSS. This linearly decreasing phase makes it useful for its potential application in pulsed systems [19].

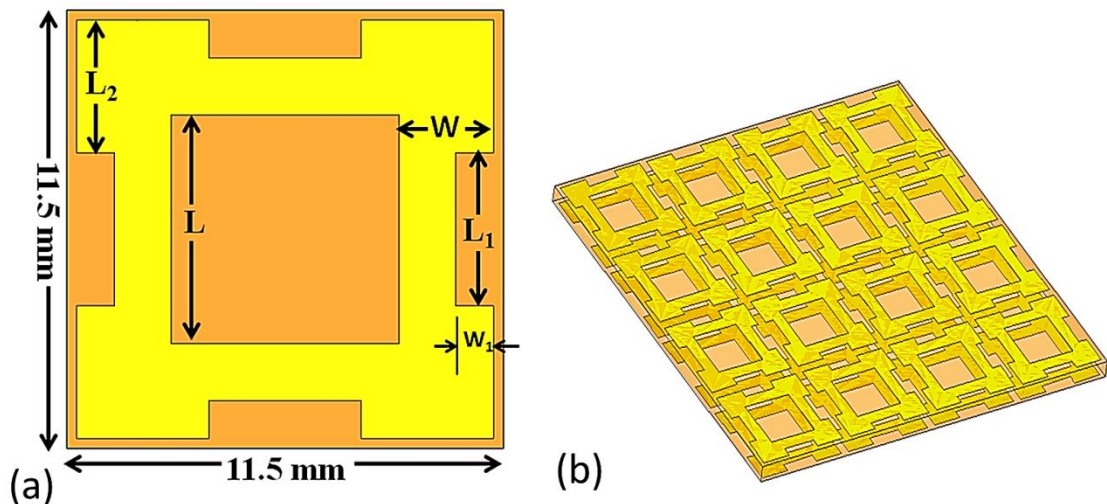


Fig. 1. (a) Unit cell design of the proposed wide stop-band FSS (b) view of the top and bottom metallic layers.

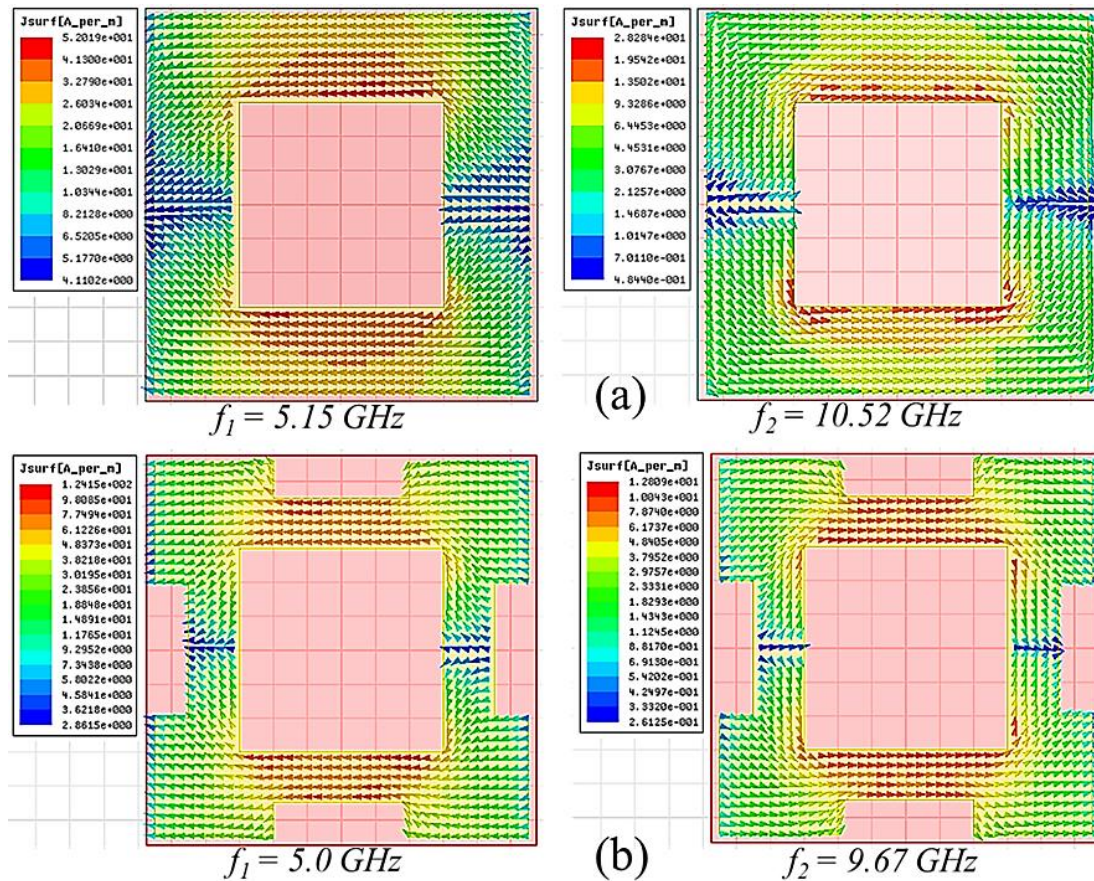


Fig. 2. Surface current distribution of (a) conventional square loop FSS and (b) the proposed FSS structures for their transmission null frequencies.

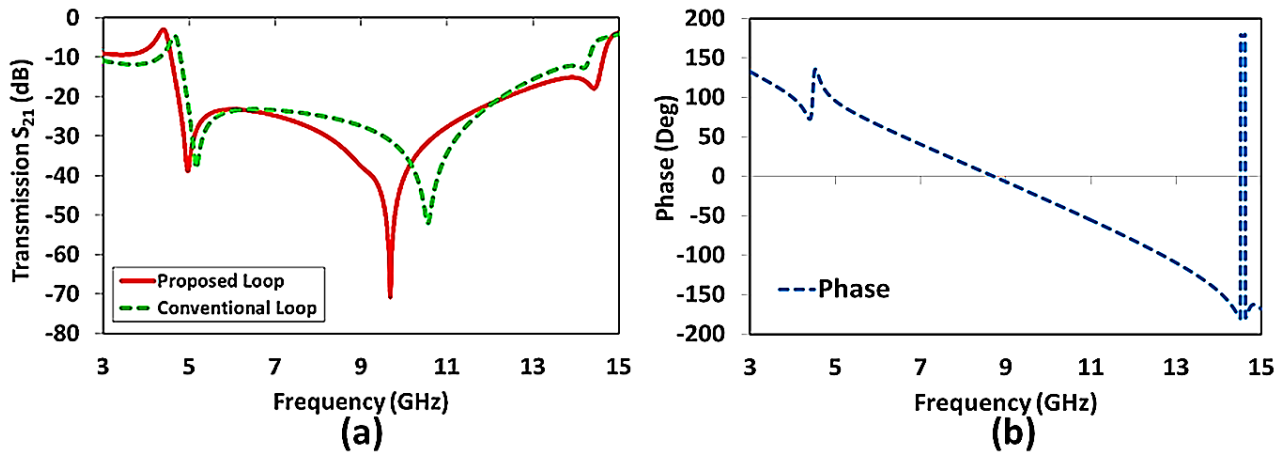


Fig. 3. (a) Comparison of simulated  $S_{21}$  of the proposed FSS with conventional square loop FSS and (b) simulated phase response.

The simulated polarization response of the proposed FSS is shown in Fig. 4(a). As the polarization angle varies the electric field (E) and magnetic field (H) makes an angle ‘ $\phi$ ’ with the X-axis and Y-axis, respectively, but the direction of propagation is maintained along Z-axis. The proposed structure exhibits polarization insensitivity as for the variations of angle ‘ $\phi$ ’ from  $0^{\circ}$  to  $90^{\circ}$  the transmission response remains same and both the resonant frequencies remains constant. The performance of the proposed FSS has also been investigated for oblique angles as shown in Fig. 4(b). The resonant frequencies almost remain same for



varying angles of incident wave from  $0^0$  to  $60^0$ . Therefore, the overall bandwidth almost remains unaffected with the change in angles and the structure shows good performance for high incident angles such as  $60^0$ .

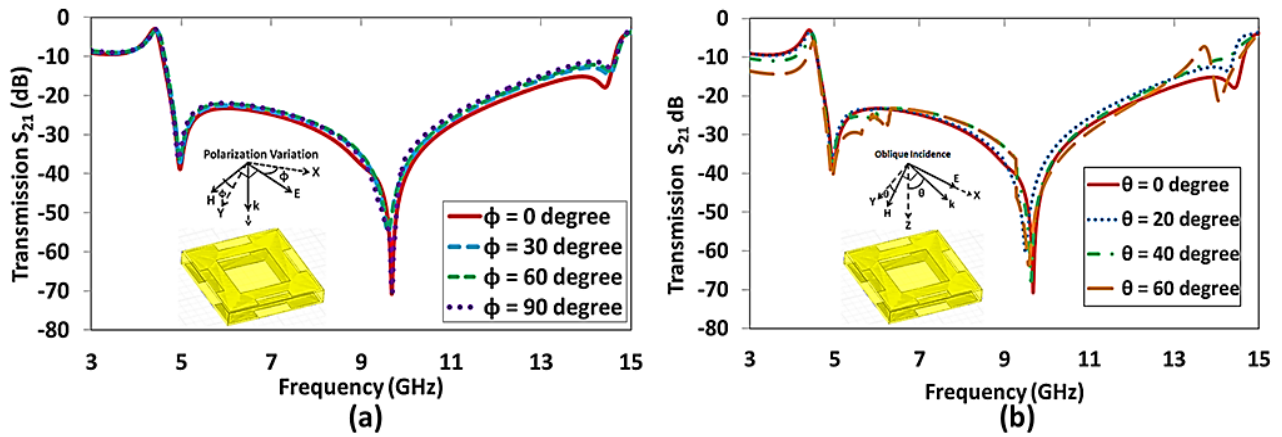


Fig. 4. Simulated response (a) for different polarization angles and (b) for different oblique incidence angles

As the bandwidth of the loop type FSS is mainly dependent upon its width and the cutting of slots, reduces the width ( $W$ ) of the proposed square loop which further decreases the bandwidth. To solve this problem, the dimensions of  $W_1$  and  $L_1$  are critically optimized to maintain the effective width nearly constant.

### 3 EQUIVALENT CIRCUIT ANALYSIS

The equivalent circuit method is used to understand the basic theory of operation of the proposed design. Equivalent circuit is shown in Fig. 5. The Impedance of the dielectric material is calculated as  $Z_D = Z_0/\sqrt{\epsilon_r}$  ( $Z_0$  is free space impedance i.e.  $377\Omega$ ). Loop type FSS patch is modeled by the parallel combination of  $L_F$  and  $C_F$ . From the simplified equivalent circuit of square loop FSS suggested in [20] the values of inductance ( $L_D$ ) and capacitance ( $C_D$ ) of dielectric substrate as well as of the conventional square loop are calculated using the following equations:

$$L_D = \mu_0 \mu_r h \quad (1)$$

$$C_D = (\epsilon_0 \epsilon_r h)/2 \quad (2)$$

$$\frac{X_{LF}}{Z_0} = \frac{d}{p} F_1(p, W, \lambda) \quad (3)$$

$$\frac{B_{CF}}{Y_0} = 4 \frac{d}{p} F_2(p, g, \lambda) \quad (4)$$

$$F_1(p, W, \lambda) = \frac{p}{\lambda} \left[ \ln \left( \operatorname{cosec} \frac{\pi W}{2p} \right) + G_1(p, W, \lambda) \right] \quad (5)$$

$$F_2(p, g, \lambda) = \frac{p}{\lambda} \left[ \ln \left( \operatorname{cosec} \frac{\pi g}{2p} \right) + G_2(p, g, \lambda) \right] \quad (6)$$

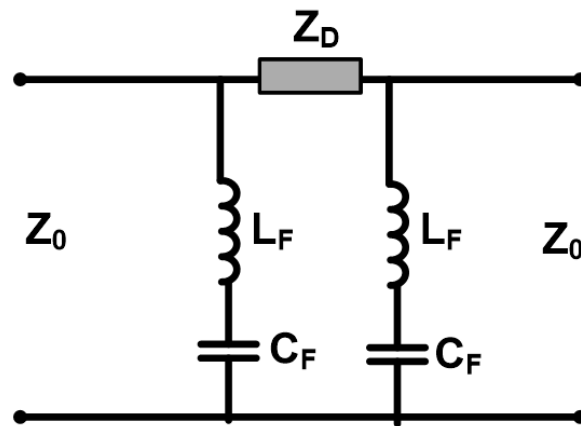


Fig. 5. Equivalent circuit of the proposed FSS.

Where  $\mu_0$  is the permeability of the free space,  $\mu_r$  is the relative permeability of dielectric substrate, ‘h’ is the height of the dielectric substrate,  $\epsilon_0$  is the permittivity of free space,  $\epsilon_r$  is the relative permittivity of the dielectric, ‘p’ is the periodicity, ‘W’ is the width of the loop, ‘g’ is the gap between two unit elements and ‘d’ is the dimension of square loop.  $G_1(p, W, \lambda)$  and  $G_2(p, g, \lambda)$  are correction factors. From the equations, (1) to (6) the values of the lumped parameters are calculated and given in Table I.

TABLE I CALCULATED VALUES OF LUMPED PARAMETERS.

S. No.	Parameter	Calculated Value
1	$L_D$	2.011nH
2	$C_D$	0.031pF
3	L	2.610nH
4	C	0.130pF

The simulated value of first resonance frequency ( $f_1$ ) is 5.0 GHz. The first and second resonance frequencies are calculated by using methods as suggested in [18]. The first resonance frequency ( $f_1$ ) is calculated as:

$$f_1 = \frac{1}{2\pi \sqrt{(L_D + \frac{L_F}{2})(C_D + 2C_F)}} \quad (7)$$

$L_D$  and  $C_D$  are the inductance and capacitance of the dielectric substrate respectively. The calculated value of first resonance frequency ‘ $f_1$ ’ is 5.12 GHz which is very close to the simulated value. The second resonance frequency ‘ $f_2$ ’ of the proposed FSS design depends upon ‘W’, ‘ $L_1$ ’ and ‘ $W_1$ ’. The second resonance frequency has been evaluated by formulation of an equation through the use of curve fitting as:

$$f_2 = a(e^{bW}) \quad (8)$$

Where

$$a = 2.1233 - 0.3291W_1 \tag{9}$$

$$b = 0.6469 + 0.0059L_1 \tag{10}$$

The values of ‘W’, ‘W<sub>1</sub>’ and ‘L<sub>1</sub>’ are in mm. The simulated and calculated values are compared as listed in Table II, Table III and Table IV. It is observed that for the optimized dimensions of W, W<sub>1</sub> and L<sub>1</sub> the percentage errors in between the simulated and calculated values are quite less which shows the good convergence of the fitted equation.

TABLE II COMPARISON OF DIFFERENT VALUES OF W (L<sub>1</sub> =4 mm, W<sub>1</sub> =1 mm).

S. No.	W (mm)	Simulated f <sub>2</sub>	Calculated f <sub>2</sub>	%Error
1	2.00	7.08	6.89	2.68
2	2.25	8.09	8.11	0.25
3	2.50	9.67	9.59	0.83
4	2.75	11.56	11.34	1.90

TABLE III COMPARISON OF DIFFERENT VALUES OF W<sub>1</sub> (L<sub>1</sub> = 4 mm, W =2.5 mm).

S. No.	W <sub>1</sub> (mm)	Simulated f <sub>2</sub>	Calculated f <sub>2</sub>	%Error
1	0.5	9.98	10.47	4.90
2	1.0	9.67	9.59	0.93
3	1.5	9.25	8.71	5.83
4	2.0	8.30	7.84	5.54

TABLE IV COMPARISON OF DIFFERENT VALUES OF L<sub>1</sub> (W<sub>1</sub> = 1 mm, W =2.5 mm).

S. No.	L <sub>1</sub> (mm)	Simulated f <sub>2</sub>	Calculated f <sub>2</sub>	%Error
1	2	9.25	9.31	0.64
2	3	9.33	9.45	1.28
3	4	9.67	9.59	0.83
4	5	9.83	9.73	1.01

#### 4 PARAMETRIC ANALYSIS

In order to get better physical insight and to investigate the contribution of different geometric dimensions in wideband response the parametric analysis of the proposed FSS has been done. The simulated transmission response for different value of ‘W’ is shown in Fig. 6(a). It is observed that as the width (W) increases second resonant frequency greatly affected and shifts towards higher value thereby enhances the bandwidth. The maximum bandwidth achieved is 9.32 GHz for ‘W’ equals to 2.75 mm from 4.79 to 14.11 GHz, which is 98.62% corresponding to the center frequency of this range. However, the increase in width (W) above 2.50 mm (optimized value) results increase in bandwidth, but it shifts the second resonant frequency to a higher value which further disturbs the compactness of the proposed design. Transmission response for different values of the slot width (W<sub>1</sub>) is shown in Fig. 6(b). It is observed that as the slot width increases second resonant frequency shifts towards lower value due to increase in effective inductance and causes the decrease in -20dB bandwidth. The optimized value of W<sub>1</sub> is 1 mm. The effect of slot length (L<sub>1</sub>) on the transmission response is shown in Fig. 6(c). It can be observed that as the slot length increases, there is no

variation in first resonance frequency but the second resonance frequency increases slightly which further increases the bandwidth and the optimized value of  $L_1$  is found to be 4 mm.

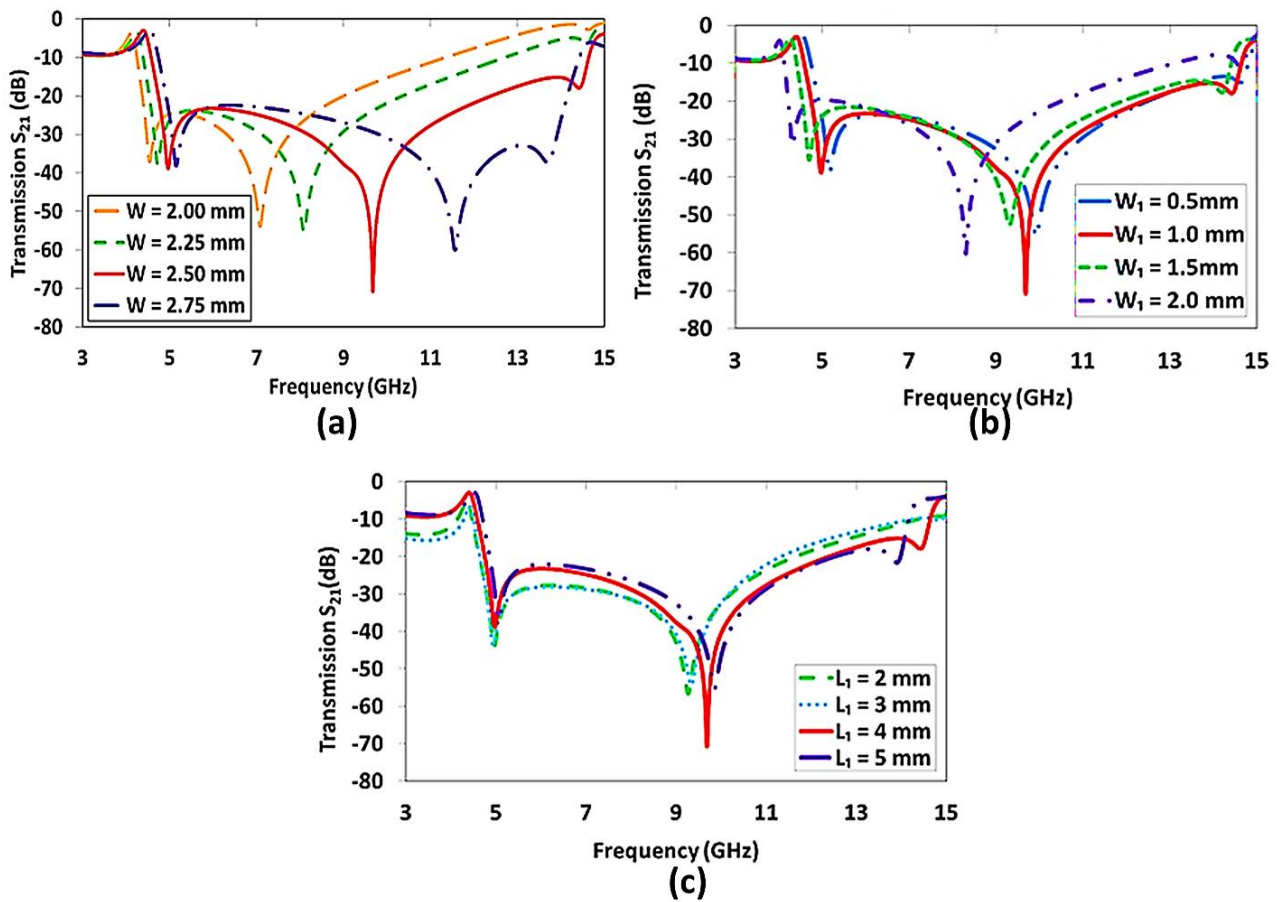


Fig. 6. Simulated response of the proposed FSS (a) for different values of width ‘W’ (b) for different values of width ‘ $W_1$ ’ and (c) for different values of width ‘ $L_1$ ’

## 5 EXPERIMENTAL VERIFICATIONS

In order to experimentally measure the performance of the proposed wideband FSS structure an array of  $17 \times 17$  elements has been fabricated as shown in Fig. 7(a). For the measurements of transmission response ( $S_{21}$ ) two double ridge ultra-wide band horn antennas (1 to 18GHz), connected to Agilent’s Vector Network Analyzer (VNA) model N5222A are used. One of the horn antennas is used as a transmitter and the other as a receiver. At first, in order to calibrate the test setup  $S_{21}$  is measured by placing the two antennas in front of each other at a distance of nearly 1.2 meters. Then measurement of  $S_{21}$  was performed by placing fabricated prototype of FSS in between the two horn antennas as shown in Fig. 7(b). The difference between the two measured results gives rise to actual transmission response of the fabricated FSS structure. The measured and simulated transmission responses for normal incidence are shown in Fig. 8. It is observed that measured response follows the simulated response quite well.



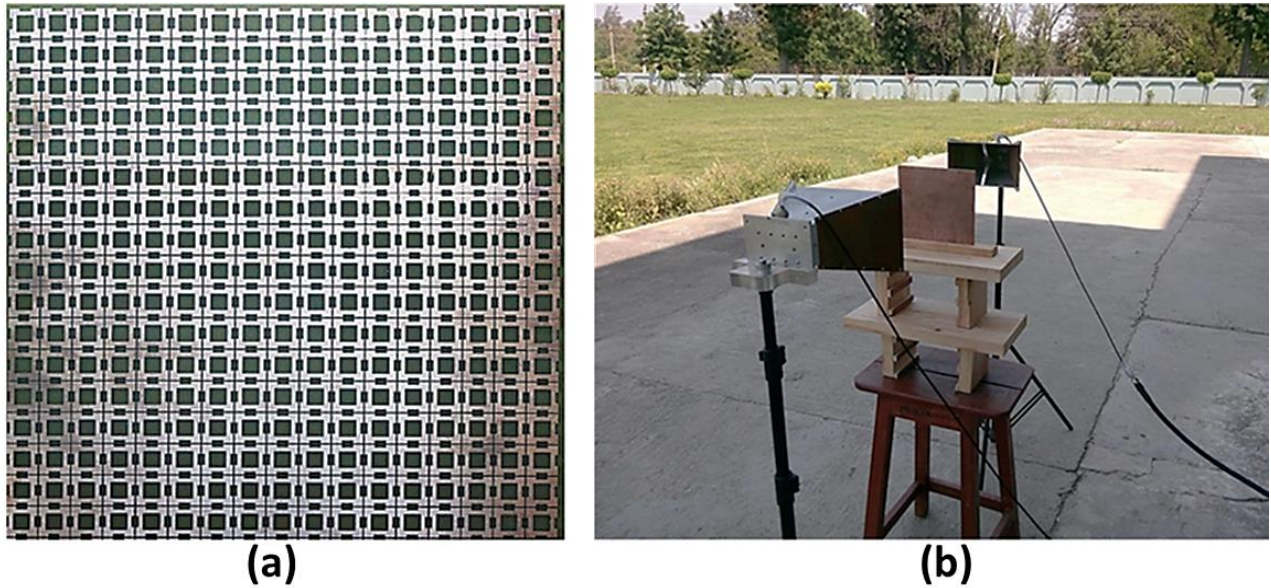


Fig. 7. (a) Fabricated prototype of the proposed FSS and (b) measurement setup.

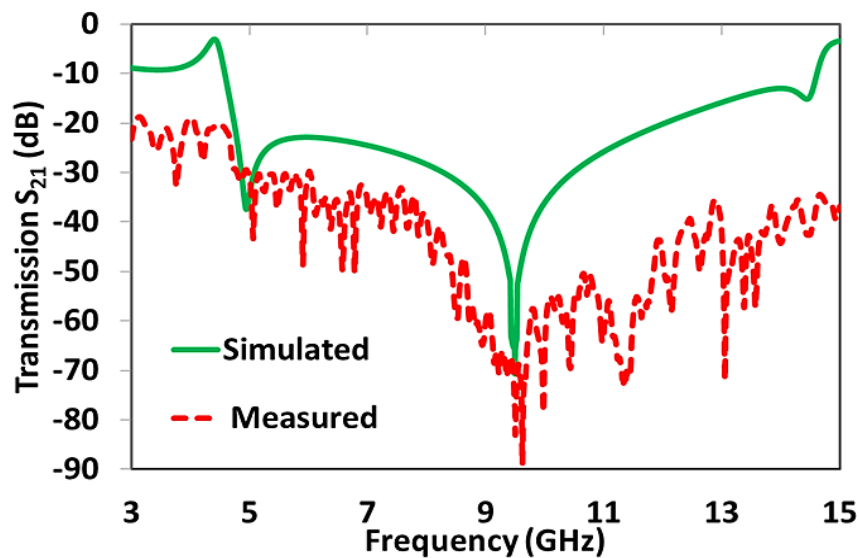


Fig. 8. Comparison of measured and simulated transmission response ( $S_{21}$ ) under normal incidence.

The polarization insensitivity of the fabricated design is tested by measuring its transmission response for different azimuthal angles ( $\phi$ ) as shown in Fig. 9. In order to measure polarization response, the fabricated structure is rotated about its axis from  $0^{\circ}$  to  $90^{\circ}$  in the steps of  $30^{\circ}$ . It is observed that similar to simulated response the measured transmission response remains same for all polarization angles ( $\phi$ ), which proves polarization insensitivity of the proposed FSS structure. Fabricated prototype is also tested experimentally for oblique incidences by rotating transmitting antenna around the circumference of a circle whose radius is equal to the distance at which near field effects are observed to be minimum. The experimental results for different oblique incidence angles are shown in Fig. 10. It is observed from simulated and measured results that second resonance frequency almost remains unvarying even for large angles of incidence.

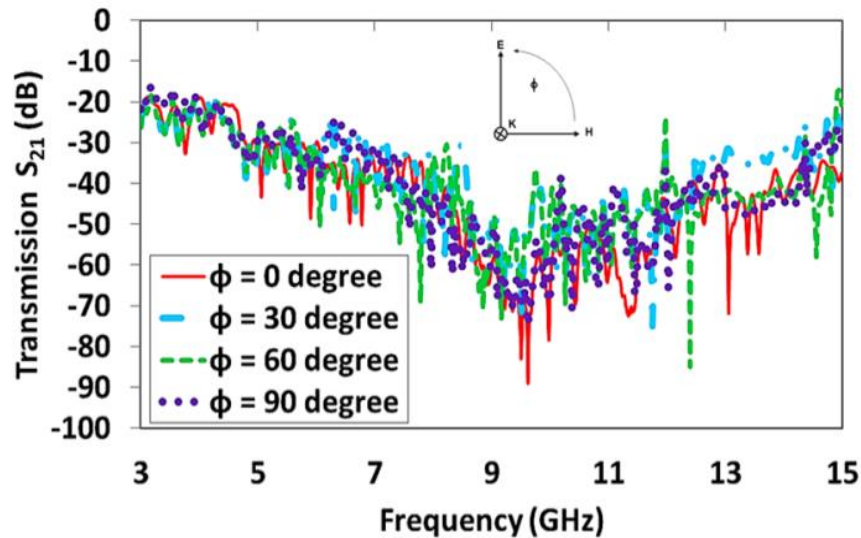


Fig. 9. Measured transmission response ( $S_{21}$ ) for different polarization angles under normal incidence.

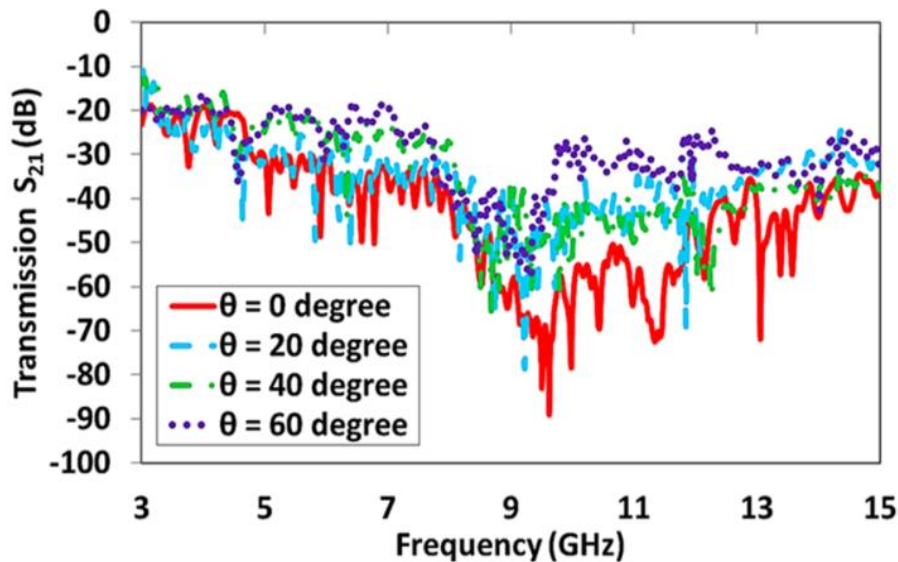


Fig. 10. Measured transmission response ( $S_{21}$ ) for different incident angles under TE polarization.

## 6 CONCLUSIONS

A compact, polarization insensitive, wide stop band frequency selective surface has been presented. The unit cell of the proposed design consists of a modified square loop FSS printed on either side of FR4 substrate. Overall thickness and periodicity of the design is 1.6mm ( $0.045\lambda_0$ ) and 11.5 mm ( $0.33 \lambda_0$ ) respectively. The proposed FSS has wide stop band (transmission response  $< -20$ dB) of 7.7 GHz, which covers both C and X band. Equivalent circuit of the proposed design is presented and resonance frequencies are calculated to validate their values in comparison to simulated ones. The performance of the proposed FSS design is investigated for its various dimensional parameters to find best optimal solution. The fabricated prototype is experimentally tested for normal as well as for oblique angles of incidence wave.

Measured results are observed in agreement with the simulated results. The unit cell size, thickness and other features of the proposed FSS have been compared with the previously reported wide stop-band FSS designs in Table V. It is observed that the proposed FSS is compact and provides large percentage bandwidth as compared to [15, 16]. However, the designs presented in [18] and [21] exhibits more percentage bandwidth but the proposed design is polarization insensitive as compared to [18] and is more compact in size as compared to [21]. These features make it suitable for various potential applications such as RCS reduction, pulsed systems, electromagnetic shielding, spatial filtering, sub-reflector in antennas etc.

TABLE V COMPARISON OF THE PROPOSED FSS WITH PREVIOUSLY PRESENTED DESIGNS.

FSSs	Center Frequency (GHz)	Unit Cell Size (mm)	Thickness (mm)	-20 dB Stop band Bandwidth (GHz)	Metallic Layers used	Polarization Insensitive
[15]	~8.5	9.0 (0.30 $\lambda_0$ )	3.27 (0.92 $\lambda_0$ )	~5.0 (~60%)	Multilayer	Yes
[16]	10.25	12.0 (0.041 $\lambda_0$ )	3.20 (0.11 $\lambda_0$ )	7.50 (73.17%)	Dual Layer	Yes
[18]	6.87	16.0 (0.37 $\lambda_0$ )	1.80 (0.041 $\lambda_0$ )	8.0 (116%)	Dual Layer	No
[21]	7.63	14.0 (0.36 $\lambda_0$ )	1.60 (0.041 $\lambda_0$ )	7.53 (98.62%)	Dual Layer	Yes
<b>Proposed FSS</b>	8.56	11.5 (0.33 $\lambda_0$ )	1.60 (0.045 $\lambda_0$ )	7.70 (89.95%)	Dual Layer	Yes

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