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## Estimation of RC slab-column joints effective strength using neural networks

#### **Abstract**

The nominal strength of slab-column joints made of highstrength concrete (HSC) columns and normal strength concrete (NSC) slabs is of great importance in structural design and construction of concrete buildings. This topic has been intensively studied during the last decades. Different types of column-slab joints have been investigated experimentally providing a basis for developing design provisions. However, available data does not cover all classes of concretes, reinforcements, and possible loading cases for the proper calculation of joint stresses necessary for design purposes. New numerical methods based on modern software seem to be effective and may allow reliable prediction of column-slab joint strength. The current research is focused on analysis of available experimental data on different slab-to-column joints with the aim of predicting the nominal strength of slabcolumn joint. Neural networks technique is proposed herein using MATLAB routines developed to analyze available experimental data. The obtained results allow prediction of the effective strength of column-slab joints with accuracy and good correlation coefficients when compared to regression based models. The proposed method enables the user to predict the effective design of column-slab joints without the need for conservative safety coefficients generally promoted and used by most construction codes.

### **Keywords**

column-slab joint, effective strength, high strength column, normal strength slab, neural network, regression.

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### 1 INTRODUCTION

The use of flat-plate system in tall buildings is rapidly increasing due to its advantages on structural performance and construction process over conventional RC (reinforced concrete) construction [10]. As a result this system has been adopted and widely used for many structures that were recently constructed such as large-scale supermarket, store and underground garage, bridge decks, etc. Using RC flat plate system in the basement and residential floors of tall

buildings is often mandatory to reduce story height and to enable rapid construction. The use of flat plate floors for the basement parking areas also minimizes the amount of excavation so that total construction time and cost can effectively be reduced [19].

Flat plate slab [6] is a very common and competitive structural system, in which columns directly support floor slabs without beams. Such system of construction usually consists of high strength concrete (HSC) columns and normal strength concrete (NSC) slabs or floors. The slabs are laid with NSC mainly for the purpose of achieving the economy and improving the ductile behavior. However, in some cases the presence of intervening weaker concrete slab layer affects the column load carrying capacity. The column strength is reduced as compared to its actual axial compressive strength [22].

Flat-plate systems are popular gravity systems permitting architectural flexibility, more clear space, simple formwork, shorter construction time and simple arrangement of electrical and mechanical systems. Buildings with such systems are technology-friendly and conducive to modern design concepts. Compared to a typical beam-slab system, the flat-plate slab-column system should be able to save structural costs by about 20%. Absence of efficient load transfer mechanism has been one of flat-plate system's weak point that may lead to a brittle punching shear failure at the region of slab-column joint [7, 24]. It was found that the effective moment of inertia concept, together with the Direct Design Method, can be used for computing deflections of irregular flat plate floors [24]. Additionally, the results obtained indicated that at higher load levels, beyond the serviceability limit state, the use of reduced modulus of elasticity will improve the predicted deflections considerably [24]. The problem of brittle punching failure due to the transfer of shearing forces and unbalanced moments at the flat plate-column connection was investigated to study the effects of various interdependent factors that govern the punching shear resistance and behavior of the flat plate-column connections as well as their inclusion in current Codes [7]. It was shown that the problem of displacement-induced unbalanced moment and the accompanying shear forces at flat plate-column connections can be effectively addressed by providing shear reinforcement in slabs.

To understand the load transfer mechanism and predict the effective strength of the joint when two different strengths of concrete are used in columns and slab, several experimental investigations have been conducted [2, 8, 9, 15, 17, 20, 21]. The test results, obtained for slab-column specimens, were analyzed to determine the maximum difference between column and floor concrete strengths that yield no decrease in the column load-carrying capacity and the allowable load-carrying capacity of the column if this difference is exceeded [2].

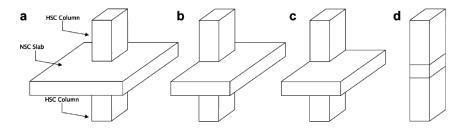
The modern ACI code [1] provisions for estimating the strength of a slab-column joint are based upon the outcomes of this research [2]. It was also shown that the ACI code is unsafe for higher ratios of column to slab concrete strengths [8]. A separate design equation, as a function of column and slab concrete strengths, was proposed that tend to negate the ACI equation for estimating the joint effective strength [8].

Interior column specimens were also tested with and without load acting on a slab [17]. The slab loading on the tested specimens was of service nature and it was applied together with the ultimate axial load that acted on the column portions. It was shown that the slab

loading develop significant tensile strains in the slab's top steel in the slab-column joint region. They recommended that the effective strength of the joint should not only be a function of column and slab concrete strengths but also of the joint aspect ratio (ratio of slab thickness to column dimension, h/c).

One interior slab-column joint was tested with extreme load acting on the slab and service axial load applied on the column [9]. It was reported that the joint strength is highly influenced by the bending action of the slab. It was found that the surrounding slab confinement increased the strength and ductility of the joint [15]. It was also reported that the use of fiber-reinforced concrete in slabs at interior columns increases the strength and stiffness of the joints.

A double headed shear stud rails was used in the surrounding slabs in order to improve the punching shear resistance of the test specimens [20, 21]. The slabs were loaded with ultimate load and columns with service axial load. The effects of surrounding slab confinement, ratio of slab thickness to column dimension (aspect ratio, h/c), intensity of slab load, slab reinforcement ratio, column concrete strength and slab concrete strength were investigated. It was found that the application of slab load reduces the column axial load carrying capacity. It was also observed that the ACI code [1] provisions are unsafe and non-conservative for test specimens with high aspect (h/c) and column to slab concrete strength ratios. The Canadian standard [5] was found safe but conservative for test specimens with low aspect (h/c) ratios. A new design expression, incorporating all of the above-mentioned parameters that is able to predict the joint effective strength more reliably than the ACI code [1] and Canadian standards [5] was proposed. Schematic views of different types of the tested slab-column joints are shown in Fig. 1.



Schematic views of slab-columns connection: (a) interior column (b) edge column (c) corner column (d) sandwich column (following [13]).

In this research the data of previous experimental researchers [2, 8, 9, 15, 17, 20, 21], involving the testing of slab-column connections with HSC columns and NSC slabs has been used. Analysis of the accumulated test data employing the neural network technique has been performed in order to develop a new procedure for predicting the effective strength of the slabcolumn joint. A neural network has the capability of realizing a greater variety of nonlinear relationship of considerable complexity [3, 23]. In neural networking the data is presented to the network in the form of input and output parameters, and the optimum nonlinear relationship is found by minimizing a penalized likelihood.

In fact, the network tests many kinds of relationship in its search for an optimum fit.

As in regression analysis, the results then consist of a specification of the function, which in combination with a series of coefficients (called weights), relates the inputs to the outputs. The search for the optimum representation can be computer intensive, but once the process is completed (that is, the network has been trained), the estimation of outputs is very rapid. This work has been applied to the complex problem of predicting the capacity of an interior slab-column connection.

The present study, applying neural networking, is also aimed at focusing efforts on bringing simplicity and improving the reliability of the proposed estimation procedure. Additionally, the use of test data covering a large range of column and slab concrete strengths, column and slab reinforcement ratios, surrounding slab confinement, and wide range of slab thickness to column dimension ratio (aspect ratio, h/c) greatly enhances the scope of the present study.

### 2 AIMS AND SCOPE OF THE RESEARCH

Despite the availability of large number of models, the problem of column-slab joint effective strength has remained inconclusive. It is felt that this is partly due to the complexity of the phenomenon involved and partly because of the limitations of statistical regression, an analytical tool commonly used by most of the investigators. Neural networks (NN) have advantages over statistical models like their data-driven nature, model-free form of predictions, and tolerance to data errors [11, 12, 16, 18]. The objective of this study is to reanalyze the data considered in earlier studies by employing the NN technique with a view towards finding out if better predictions are possible.

The current research is focused on analysis of available experimental data on different column-slab joints with the aim of predicting the effective column-slab joint strength. For this reason the NN technique was employed. Original MATLAB routines [13] were developed to analyze the available experimental data. NN toolbox is used to analyze the experimental data [14] and predict the effective column-slab joints strength. The prediction should have high accuracy and high correlation coefficients, compared to the regression based models in order to enable using the predicted results in effective design of column-slab joints with no need to conservative safety coefficients presently used in the codes.

### 3 EXISTING MODELS FOR ESTIMATING THE COLUMN-SLAB JOINT EFFECTIVE STRENGTH

A large number of regression models, mostly empirical, based on mechanics of structures and materials are available for the prediction of the effective strength of a column-slab joint [1, 2, 5, 8, 17, 20, 22]. ACI code [1] suggests that there is no reduction in column strength for ratios of column concrete strength to slab concrete strength up to 1.4. For higher ratios, based on the experiments by Bianchini et al. [2], the following expression for predicting the effective strength of the joint was proposed:

$$f'_{ceff} = 0.75 f'_{cc} + 0.35 f'_{cs}; (1)$$

where,  $f'_{cc}$  and  $f'_{cs}$  are strength of column and slab concrete respectively.

Gamble and Klinar [8] proposed the following as a lower bound relationship for estimating the strength of a column-slab joint:

$$f'_{ceff} = 0.47 f'_{cc} + 0.67 f'_{cs}; (2)$$

They reported that the ACI code [1] equation is adequate for column concrete strength to slab concrete strength ratio of 1.4. However, for higher ratios ACI code [1] design provision overestimates the effective strength of the joints and is therefore unsafe.

In existing design provisions to cover the high strength concrete, for higher ratios of column concrete strength to slab concrete strength, the Canadian Standard CSA-A23.3:1994 [5] presents the following design expression:

$$f'_{ceff} = 0.25 f'_{cc} + 1.05 f'_{cs}; (3)$$

The effective strength prediction using CSA A23.3 [5] design provisions appears to be safe but highly conservative.

A striking feature of the test programs conducted by both Bianchini et al. [2] and Gamble and Klinar [8] was the absence of slab load. In fact in a prototype structure, load on the slab will produce significant tensile straining in the top flexural slab reinforcement in the vicinity of the column. It would seem reasonable to assume that such strain will have a detrimental effect on the ability of the surrounding slab to confine the column-slab joint [17]. Ospina and Alexander [17] developed a new design model incorporating the effect of the ratio of slab thickness to column dimension (aspect ratio, h/c). The design equation, proposed for predicting the effective strength of the joint, is given as under:

$$f'_{ceff} = \left(\frac{0.25}{h/c}\right) f'_{cc} + \left(1.4 - \frac{0.35}{h/c}\right) f'_{cs}; \tag{4}$$

Besides the column and slab concrete strengths as well as the aspect ratio (h/c), the effects of surrounding slab confinement and slab reinforcement ratio,  $r_s$ , should also be considered in predicting the effective strength of the joint [20]. Based on the induction of the new parameters, the following predicting equation was devised:

$$f'_{ceff} = 0.35 f'_{cc} + 0.384 \left( \frac{\rho_s + 4.12}{h/c + 1.47} \right) \lambda f'_{cs}; \tag{5}$$

Recently a mechanics of materials approach, commonly used for composite materials, was applied for the theoretical analysis of the problem [22]. This approach with the use of the available test data lead to a new regression model for calculating the effective strength of the joint. Additionally, it was reported that the new experiments [8, 9, 15, 17, 20, 21] tend to negate the limiting ratio of 1.4 between the two concrete strengths, which ACI [1] allows in Sec. 10.15 of its building code to be used without considering any adverse affects on the axial load carrying capacity of the columns. The effective strength of the joint concrete was found to be proportional to the ratio of product and sum of the two concrete strengths, as given below:

$$f'_{ceff} = 2.25 \left( \frac{f'_{cc} f'_{cs}}{f'_{cc} + f'_{cs}} \right);$$
 (6)

This observation leads to the comparison of column specimens' behavior with that of composite materials. The accumulated test data provides a strong evidence for the applicability of some mechanics principles of composite materials to the sandwiched concrete. Additionally, it is observed that most of the models presented above were developed by different researchers mainly for their own data, except the model proposed by Shah et al. [20], which has used a wide variety of data.

### 4 AVAILABLE EXPERIMENTAL DATA

Table 1 shows the test data of column-slab specimens with HSC columns and NSC slabs [2, 8, 9, 15, 17, 20] with total of 74 data points. The data consists of eight parameters viz. slab thickness, column dimension, column reinforcement, slab reinforcement, slab confinement factor, slab load, concrete strength of slab and column. The range of these parameters for the data is given in Table 2. The data covers all the possible four cases of confinement viz. interior column, edge column, corner column and sandwich column.

All the columns are square in size except two, as mentioned in Table 1, for which equivalent square section has been considered. The experimental value of effective strength of joint, given in the table, has been calculated from:

$$f'_{ceff} = \frac{P_c - f_y A_{st}}{0.85 \left( A_q - A_{st} \right)} \tag{7}$$

where  $P_c$  is the maximum load carried by the column,  $A_{st}$  is the area of longitudinal steel bars in the column,  $A_g$  is the gross cross-sectional area of the column section,  $f_y$  is the yield strength of column reinforcement, and  $f'_{ceff}$  is the effective concrete compressive strength. The effective strength,  $f'_{ceff}$ , is notionally the cylinder strength of some hypothetical concrete that combines the properties of both the column and slab concretes and can be expected to be in between the range of column and slab concrete strengths.

### 5 NEURAL NETWORK MODEL

The manner, in which the data are presented for training, is the most important aspect of the NN method. Often this can be done in more than one way, the best configuration being determined by trial-and-error. It can also be beneficial to examine the input and output patterns or data sets that the network finds difficult to learn. This enables a comparison of the performance of the NN model for these different combinations of data.

In order to map the causal relationship related to the slab-column joint strength, two separate input/output schemes (called Model-A1 and Model-A2) were employed. The first took

Table 1 Details of column-slab specimens.

0,000		h	С	$\rho_c$	$\rho_s$	10	$P_{c}$	$P_{\rm s}$	$p_s$	$f_{ii}'$	$f_{cc}'$	$f_{cs}'$	f, tt
כע	Specimen	(mm)	(mm)	. (%)	. 8	<	(kN)	(kN)	$(kN/m^2)$	(MPa)	(MPa)	(MPa)	(MPa)
	S9013.0	178	279	1.46	0.55	4	3114	0	0	310	51.0	17.1	42.1
	S7513.0	178	279	1.46	0.55	4	3287	0	0	310	51.3	22.2	45.2
	S7513.0	178	279	1.46	0.55	4	2891	0	0	310	43.2	15.9	38.8
	S60I3.0	178	279	1.46	0.55	4	3069	0	0	310	45.3	14.3	41.7
Sianchini et al.	S6012.0	178	279	1.46	0.55	4	3114	0	0	310	45.7	23.7	42.3
	S5012.0	178	279	1.46	0.55	4	2580	0	0	310	40.6	21.3	34.1
	S5012.0	178	279	1.46	0.55	4	2446	0	0	310	34.4	15.2	32.1
	S40I2.0	178	279	1.46	0.55	4	1922	0	0	310	25.9	17.0	24.1
	S4511.5	178	279	1.46	0.55	4	5669	0	0	310	34.3	19.8	35.5
	S3711.5	178	279	1.46	0.55	4	2002	0	0	310	22.6	15.2	25.4
	S3011.5	178	279	1.46	0.55	4	1979	0	0	310	25.6	13.4	25.1
	C	178	254	1.76	0.71	4	3781	0	0	490	89.0	29.7	59.6
	О	178	254	1.76	0.71	4	4670	0	0	490	96.5	30.3	76.5
Gamble and	<sub>ರ</sub>	178	254	1.76	0.71	4	4893	0	0	490	90.3	42.8	90.08
Klinar [8]	Н	178	254	1.76	0.71	4	3336	0	0	490	85.5	17.2	51.7
	X	178	254	1.76	0.97	4	5315	0	0	490	72.4	35.2	88.5
	Г	178	254	1.76	0.71	4	5115	0	0	490	83.4	33.1	84.7
	A1-A	100	200	3.53	0.58	4	3194	0	0	445	105	40	100.31
	A1-B	100	200	3.53	0.65	4	3678	48	25	445	105	40	93.08
	A1-C	100	200	3.53	0.65	4	3498	94	49	445	105	40	87.56
	A2-A	100	200	3.53	0.43	4	3820	0	0	445	112	46	97.43
	A2-B	100	200	3.53	0.65	4	3807	33.2	17	445	112	46	97.03
	A2-C	100	200	3.53	0.65	4	3591	98	45	445	112	46	90.41
	A3-A	150	200	3.53	0.35	4	3437	0	0	445	88	25	85.69
	A3-B	150	200	3.53	0.85	4	3174	100	53	445	68	22	77.63
Jenina and	A3-C	150	200	3.53	0.85	4	2275	157.2	83	445	68	25	50.09
Alexander [17]	A4-A	150	200	3.53	0.35	4	3272	0	0	445	106	23	80.64
anner [11]	A4-B	150	200	3.53	0.85	4	2927	93.2	49	445	106	23	70.07
	A4-C	150	200	3.53	0.85	4	2376	135.2	71	445	106	23	53.19
	B-1	250	250	1.13	0.38	4	4072	173.2	92	445	104	42	71.54
	B-2	250	250	1.13	0.75	4	5359	130	71	445	104	42	96.08
	B-3	250	250	1.13	0.59	4	5078	173.2	92	445	113	44	90.72
	B-4	250	250	1.13	0.44	4	6298	0	0	445	113	44	113.99
	B-5	250	250	1.13	0.38	4	2703	172.2	94	445	95	15	45.44
	B-6	250	250	1.13	0.75	4	3720	130	71	445	92	15	64.83
	$B-7^{b}$	250	175	1.15	0.59	4	2758	173.2	92	445	120	19	47.45
	$B-8^b$	150	175	1.15	0.75	4	4032	130	71	445	120	19	72.25
Jungwirth [9]	J-1	150	200	4.62	1.45	4	3342	639	866	250	80	33	71.7

(Continued on next page)

Table 1 (continued)

<sup>a</sup> Slab confinement factor,		et al. [2]	Bianchini					(	et al [2]	Bianchini						Klinar [8]	Gamble and						(c) (d)	et al [2]	Bianchini						Citati Co ar. [20]	Shah et al [90]			[15]	Mcharg et al.	Office	Source
ment factor, $? = {}^{b}$ Rec	S37C1.5	S50C2.0	S60S2.4	S75S3.0	S30C1.5	S37C1.5	S45C1.5	S40C2.0	S50C2.0	S60C2.0	S60C3.0	S75C3.0	S90C3.0	J	П	Ŧ	Ħ	В	Α	S30E1.5	S37E1.5	S45E1.5	S40E2.0	S50E2.0	S60E2.0	S60E3.0	S75E3.0	S90F3.0	ICSD-1	ICSC-1	ICSA-4	ICSA-3		ICSA-1ICSA-2	NB	NU	оресписи	Specimen
= 4 for in ctangula	178	178	178	178	178	178	178	178	178	178	178	178	178	178	127	178	178	178	178	178	178	178	178	178	178	178	178	178	240	180	120	120	120	120	150	150	(mm)	h
4 for interior column, tangular column of 17	279	279	279	279	279	279	279	279	279	279	279	279	279	254	254	254	254	254	254	279	279	279	279	279	279	279	$\frac{1}{279}$	279	200	200	200	200	200	200	225	225	(mm)	c
olumn, 1 of 175	1.46	1.46	1.46	1.46	1.46	1.46	1.46	1.46	1.46	1.46	1.46	1.46	1.46	1.76	1.76	1.76	1.76	1.76	1.76	1.46	1.46	1.46	1.46	1.46	1.46	1.46	1.46	1.46	2.00	2.00	2.00	2.00	2.00	2.00	1.40	1.40	(%)	$\rho_c$
$= 3 \text{ for } 5 \times 250 \text{m}$	0	0	0	0	0.54	0.54	0.54	0.54	0.54	0.54	0.54	0.54	0.54	0.89	0.94	0.89	0.89	0.89	0.89	0.55	0.55	0.55	0.55	0.55	0.55	0.55	0.55	0.55	0.43	0.36	1.00	0.53	1.00	0.53	1.41	1.41	(%)	$\rho_s$
edge m (E	0	0	0	0	2	2	2	2	2	2	2	2	2	ယ	ယ	ယ	ယ	ယ	ω	ယ	ယ	ω	ယ	ယ	ယ	ယ	ယ	اند	4	4	4	4	4	4	4	4	>	$\lambda a$
3 for edge column, 250mm (Equivalent	1735	1850	1672	1846	1334	1779	1957	1632	2002	2446	1712	2295	2135	4448	2891	3002	4226	3225	3336	1543	1779	1984	1615	2015	2589	1966	2375	2526	2713	2821	3191	2729	3180	2858	3254	3008	(kN)	$P_c$
$n_{r} = 2$ that $n_{r$	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0		871	624	459	300	442	348	0	0	(kN)	$P_s$
?=4 for interior column, $=3$ for edge column, $=2$ for corner column, <sup>b</sup> Rectangular column of 175×250mm (Equivalent square considered) [1]	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1361	975	717	469	691	544	0	0	$(kN/m^2)$	$p_s$
•	310	310	310	310	310	310	310	310	310	310	310	310	310	486	486	486	486	486	486	310	310	310	310	310	310	310	310	310	545	545	545	545	545	545	486	486	(MPa)	$f'_u$
= 0 for sa	20.8	35.9	35.5	36.8	16.5	22.6	27.5	24.2	38.2	45.7	37.1	51.2	52.0	79.3	92.4	97.9	90.3	86.9	86.2	15.8	20.8	23.8	23.2	35.3	45.1	35.8	46.9	52.5	79	82	84	70	83	85	81.8	81.8	(MPa)	$f_{cc}'$
0 for sandwich column	13.5	15.0	13.5	15.0	10.6	15.9	18.8	10.4	17.6	24.8		18.6	17.0	36.5	30.3	15.9	45.5	25.5	28.3	10.1	13.7	17.7	9.6	16.2	23.9	11.9	16.4	16.8	32.0	28.0	29.0	28.0	30.0	32.0	30.0	30.0	(MPa)	$f_{cs}'$
olumn	21.1	23.1	20.1	22.4	15.2	21.9	24.8	19.6	25.3	32.2	20.8	29.9	27.4	72.3	68.2	45.5	68.2	49.6	51.7	18.3	22.0	25.2	19.4	25.4	34.3	24.6	30.9	33.4	68.0	71.0	83.0	69.0	82.0	73.0	68.6	62.8	(MPa)	$f'_{coff}$

S. no.	Parameter	Range
Basic p	parameters	
1	Slab thickness, $h$ (mm)	100 - 250
2	Column dimension, $c$ (mm)	200 - 279
3	Column steel, $\rho_c$ (%)	1.13 - 4.62
4	Slab steel, $\rho_s$ (%)	0.00 - 1.81
5	Slab confinement factor, $\lambda$	0-4
6	Slab load per unit area, $p_s$ (kN/m <sup>2</sup> )	0 - 1361
7	Column concrete strength, $f'_{cc}$ (MPa)	15.8 - 120.0
8	Slab concrete strength, $f'_{cs}$ (MPa)	8.8 - 46.0
Additi	onal non-dimensional parameters	
1	h/c	0.5-1.2
2	$p_s/f_{cs}'$	0 - 0.0425
3	$f_{cc}^{\prime}/f_{cs}^{\prime}$	1.35 - 6.33

Table 2 Range of parameters for the data of slab-column connections (74 data points).

the input of raw causal parameters while the second utilized their non-dimensional groupings. This was done in order to check if the use of the grouped variables produced better results. The Model-A1 thus takes the input in the form of causative factors namely,  $h, c, \rho_c, \rho_s, \lambda, p_s$  $f_{cc}^{\prime}$  and  $f_{cs}^{\prime}$  yields the output, the joint-effective strength,  $f_{ceff}^{\prime}$ :

Model-A1: 
$$f'_{ceff} = f(h, c, \rho_c, \rho_s, \lambda, p_s, f'_{cc}, f'_{cs});$$
 (8)

The matrix of dimensions for the variables involved is:

The columns of the above matrix correspond to the variables in the order in which they appear in Eq. (8) and the rows of the matrix correspond to the three fundamental dimensions viz. M (mass), L (Length) and T (Time). Though the number of fundamental dimensions involved in the model is three but the rank of the above dimensional matrix is 2, thus according to the Buckingham-PI theorem [4], the number of dimensionless parameters required for modeling would be 9-2=7. The independent PI terms obtained from the nullity theorem are: h/c,  $\rho_c$ ,  $\rho_s$ ,  $\lambda$ ,  $p_s/f'_{cs}$ , and  $f'_{cc}/f'_{cs}$  and the corresponding dimensionless output  $f'_{ceff}/f'_{cc}$ . The Model A-2 employing these dimensionless variables is thus given by:

Model-A2: 
$$\frac{f'_{ceff}}{f'_{cc}} = g\left(\frac{h}{c}, \rho_c, \rho_s, \lambda, \frac{p_s}{f'_{cs}}, \frac{f'_{cc}}{f'_{cs}}\right); \tag{9}$$

The current study used the data described above (74 data points) for the prediction of joint effective strength. The training of the above two models was done using 67% of the data (49 data points) selected randomly. Validation and testing of the proposed models was made with the help of the remaining 33% of observations (25 data points), which were not involved in the derivation of the model.

Three neuron models namely, 'tansig', 'logsig' and 'purelin', have been used in the architecture of the network with the back propagation algorithm implemented in originally developed MATLAB routines. In the back propagation algorithm, the feed-forward (FFBP), cascade-forward (CFBP) and Elman back propagation (EBP) type network were considered [3, 11, 12, 16, 18, 23]. Each input is weighted with an appropriate weight and the sum of the weighted inputs and the bias forms the input to the transfer function. A transfer function (also known as the network function) is a mathematical representation, in terms of spatial or temporal frequency, of the relation between the input and output of a (linear time-invariant) system. With optical imaging devices, for example, it is the Fourier transform of the point spread function (hence a function of spatial frequency) i.e. the intensity distribution caused by a point object in the field of view.

The transfer function is commonly used in analysis of single-input single-output (SISO) filters. It is mainly used in signal processing, communication theory, and control theory. The term is often used exclusively to refer to linear time-invariant systems (LTI). Most real systems have non-linear input/output characteristics, but when operated within nominal (not "over-driven") parameters they behave close enough to linear LTI systems. The neurons employed use the following differentiable transfer function to generate their output:

$$y_j = f \cdot \left(\sum_i W_{ij} x_i + \phi_j\right) = \frac{1}{1 + e^{-(\sum_i W_{ij} x_i + \phi_j)}};$$
 (10)

Linear transfer function:

$$y_j = f \cdot \left(\sum_i W_{ij} x_i + \phi_j\right) = \sum_i W_{ij} x_i + \phi_j; \tag{11}$$

Tan-sigmoid transfer function:

$$y_j = f \cdot \left(\sum_i W_{ij} x_i + \phi_j\right) = \frac{2}{1 + e^{-2(\sum_i W_{ij} x_i + \phi_j)}} - 1; \tag{12}$$

The weight, w, and biases, f, of these equations are determined to minimize the energy function. The optimal architecture was determined by varying the number of hidden neurons. The optimal configuration was based upon minimizing the difference between the neural network predicted value and the desired output. In general, as the number of neurons in the layer is increased, the prediction capability of the network increases in beginning and then becomes stationary.

The performance of all NN model configurations was based on the mean percent error (MPE), mean absolute deviation (MAD), root mean square error (RMSE), correlation coefficient (CC), and coefficient of determination,  $R^2$ , of the linear regression line between the predicted values from the neural network model and the desired outputs. Training of NN

models was stopped when either the acceptable level of error was achieved or when the number of iterations exceeded a prescribed maximum. The neural network model configuration that minimized the MAE and RMSE and optimized the  $R^2$  was selected as the optimum and the whole analysis was repeated several times.

### SENSITIVITY ANALYSIS

Sensitivity tests were conducted to determine the relative significance of each of the independent parameters (input neurons) on the joint effective strength (output) in both of the models given by Eqs. (8) and (9). In the sensitivity analysis, each input neuron was in turn eliminated from the model and its influence on prediction of effective strength of the joint was evaluated in terms of the MPE, MAD, RMSE, CC and  $R^2$  criteria. The effect of elimination of two and more independent variables on the effective strength of joint has also been studied. The network architecture of the problem considered in the present sensitivity analysis consists of one hidden layer with 12 neurons and the value of epochs has been taken as 100.

Sensitivity analysis of Model A-1 with feed-forward back propagation for different sets of input vari-

Input variables	MPE	MAD	RMSE	CC	$R^2$
All (Eq. (8))	1.30	7.90	6.69	0.97	0.94
No $h$	5.93	8.58	8.35	0.96	0.90
No $c$	-2.05	9.19	7.29	0.97	0.92
No $\rho_c$	1.68	9.89	7.59	0.96	0.92
No $\rho_s$	3.06	5.99	6.45	0.97	0.94
No $\lambda$	6.63	13.70	8.15	0.95	0.91
No $p_s$	2.42	7.05	7.21	0.96	0.93
No $f'_{cc}$	3.89	10.00	7.80	0.96	0.91
No $f'_{cs}$	-0.38	11.42	7.71	0.96	0.92
No $\rho_c$ , $\rho_s$	1.66	8.27	6.36	0.97	0.94
No $\lambda$ , $\rho_c$	3.18	11.29	8.38	0.95	0.90
No $\lambda$ , $\rho_c$ , $\rho_s$	5.20	12.86	8.62	0.95	0.89
No $\lambda$ , $\rho_c$ , $p_s$	4.22	11.23	7.59	0.96	0.92
Only $f'_{cc}$ , $f'_{cs}$ , $h$ , $c$	3.87	12.14	8.42	0.95	0.90
Only $f'_{cc}$ , $f'_{cs}$	3.76	14.94	9.12	0.94	0.88

Note: MPE, mean percent error; MAD, mean absolute deviation; RMSE, root mean square error; CC, correlation coefficient;  $R^2$ , coefficient of determination.

The results in Table 3 show that for Model-A1, slab thickness, h, slab confinement factor,  $\lambda$ , column concrete strength,  $f'_{cc}$ , slab concrete strength,  $f'_{cc}$ , and column steel,  $\rho_c$ , are the five most significant parameters for the prediction of effective strength of the joint. The variables in the order of decreasing level of sensitivity for Model-A1 are: h,  $\lambda$ ,  $f'_{cc}$ ,  $f'_{cs}$ ,  $\rho_c$ , c,  $p_s$  and  $\rho_s$ . It is thus seen that the last three parameters have least significant effect when taken independently. The influence of the removal of two and more independent parameters at a

time has also been studied for some of the pairs. Some of the pairs considered for removal represent the existing models. The sensitivity analysis by eliminating all except  $f'_{cc}$  and  $f'_{cs}$  represents models given by Eqs. (1) to (3) and (6). It is observed to have significant effect as it reduces the value of  $R^2$  from 0.94 to 0.88. Thus the models of Bianchini et al. [2], Gamble and Klinar [8], Canadian Standards [5] and Shah and Ribakov [22] have ignored some useful parameters. The elimination of all except  $f'_{cc}$ ,  $f'_{cs}$ , h and c representing the model given by Eq. (4), is also observed to have significant effect as it reduces the value of  $R^2$  from 0.94 to 0.90. The model given by Eq. (5) is simulated by eliminating  $\lambda$ ,  $\rho_c$  and  $\rho_s$  in Table 3, which reduces the value of  $R^2$  from 0.94 to 0.92.

Similarly, Table 4 gives the results of sensitivity analysis for Model-A2. It is apparent that,  $f'_{cc}/f'_{cs}$  and l have the most significant effect on normalized effective strength and all other dimensionless variables, namely  $\rho_c$ , h/c,  $\rho_s$ , and  $p_s/f'_{cs}$  have the least significant effect. A comparison with the sensitivity analysis of Model-A1, shows that though the h/c ratio has little influence on the effective strength of the joint but the slab thickness taken independently has significant effect. The results presented in Tables 3 and 4 indicate that the models incorporating only limited number of the available parameters like  $f'_{cc}/f'_{cs}$ , and h/c are not good enough for achieving the desired accuracy and reliability in predicting the joint effective strength. Eq. (8) was devised using many of the non-dimensional variables and thus resulted in relatively better values of the coefficient of determination and correlation coefficients ( $R^2$  and CC). These findings are consistent with existing understanding of the relative importance of the various parameters on joint effective strength.

Table 4 Sensitivity analysis of Model A-2 with feed-forward back propagation.

Input variables	MPE	MAD	RMSE	CC	$R^2$
All (Eq. (9))	5.29	9.42	0.10	0.84	0.65
No $h/c$	3.30	9.77	0.10	0.83	0.67
No $\rho_c$	3.94	10.13	0.10	0.82	0.66
No $\rho_s$	3.55	8.67	0.09	0.87	0.74
No $\lambda$	2.69	11.14	0.12	0.76	0.55
No $p_s/f'_{cs}$	2.18	8.58	0.10	0.84	0.69
No $f'_{cc}/f'_{cs}$	1.01	14.64	0.14	0.60	0.33
No $\rho_c$ , $\rho_s$	2.05	9.31	0.10	0.83	0.68
Only $f'_{cc}/f'_{cs}$ , $h/c$ , $\rho_s$	5.09	12.85	0.13	0.70	0.45
Only $f'_{cc}/f'_{cs}$ , $h/c$	4.95	13.72	0.12	0.73	0.52

The Model-A1 using the raw variables is found to be better than the Model-A2 involving non-dimensional parameters. The study of sensitivity of Model-A1 gives the impression that elimination of some of the variables has only marginal influence on the resulting joint effective strength. However considering the limitations and uncertainties in the data, a full-fledged network involving all input variables would be desirable.

### ANALYSIS AND INTERPRETATION OF TEST RESULTS

The preprocessing of the network training set was performed by normalizing the inputs and targets so that they have means of zero and standard deviations of 1. Similarly, all weights and bias values were initialized to random numbers. While the numbers of input and output nodes are fixed, the hidden nodes in the case of FFBP were subjected to trials and the one producing the most accurate results (in terms of the CC) was selected. The optimization of the training procedure automatically fixes the hidden nodes in the case of the CFBP. The training of these networks was stopped after reaching the minimum mean square error between the network yield and true output over all the training patterns.

The information on number of nodes required to achieve minimum error taken in the case of each training scheme used (i.e. FFBP, CFBP and EBP) is shown in Table 5 for Model-A1 and A2. As a matter of general information, which is not of real significance in this study, it can be seen that the cascade correlation algorithm, designed for efficient training, trained the network with fewer epochs than the FFBP network.

The network architecture of the two models, given by Eqs. (8) and (9), is given in Figs. 2 and 3 respectively for BP training scheme. The error estimation parameters, on the basis of which the performance of a model is assessed, are given in Tables 3 and 4. Training and validation results for the two models are shown in Figs. 4 and 5. The trained values of connecting weights and bias for the two models are given in Tables 6 and 7 obtained from FFBP training scheme.

Model	Algorithm –	Netw	ork configu	ration	Learning	Momentum
Model	Aigoriumi –	I	H	O	rate	function
	FFBP	8	20	1	0.5	0.7
Model A-1	CFBP	8	25	1	0.5	0.7
Wiodel A-1	RBF	8	80	1	0.5	0.7
	EBP	8	20	1	0.5	0.7
	FFBP	6	14	1	0.5	0.7
Model-A2	CFBP	6	16	1	0.5	0.7
Model-A2	RBF	6	60	1	0.5	0.7
	EBP	6	20	1	0.5	0.7

Table 5 Network architecture.

Note: I, H, O indicate number of input, hidden, and output nodes, respectively; FFBP, feed-forward back propagation; CFBP, cascade-forward back propagation; RBF, radial basis function; EBP, Elman back propagation network.

The histograms of error in the prediction of the joint effective strength for Model-A1, which is found to be better than Model-A2, are plotted in Fig. 6. The percentage error in the prediction of the joint effective strength for different data sets is plotted in Fig. 7 for Model-A1. The predicted value of the effective strength of joint has been plotted against its observed value in Fig. 8 for the Model-A1.

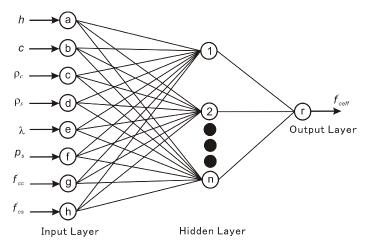


Figure 2 Model-A1: use of raw variables.

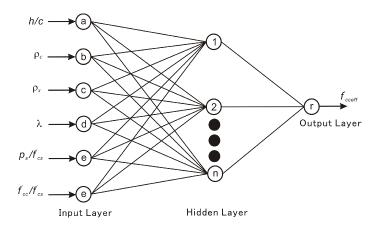


Figure 3 Model-A2: use of non-dimensional variables.

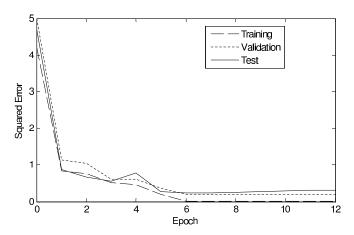


Figure 4 Epochs versus squared error of raw variables (Model - A1) by back propagation.

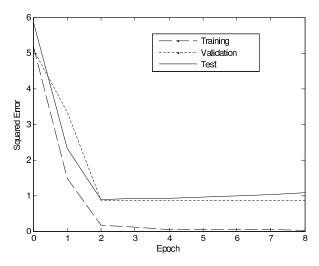


Figure 5 Epochs versus squared error of grouped variables (Model - A2) by back propagation.

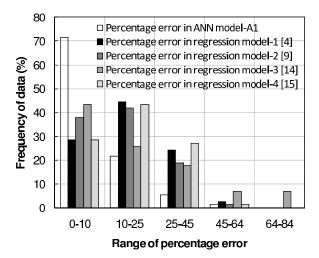


Figure 6 Histogram of percentage error for Model-A1.

It also shows that the use of raw variables as input (i.e. Model-A1) may be more beneficial than that of the non-dimensional grouped variables (i.e. Model-A2), provided an appropriate training scheme is chosen. The most suitable network, FFBP Model-A1, has the highest CC=0.97 and  $R^2=0.94$ ; and lowest MPE=1.30, MAD=7.90, and RMSE=6.69. All the ANN models featured small RMSE during training; however, the value was slightly higher during validation. The models showed consistently good correlation throughout the training and testing. In conclusion the network configuration (FFBP Model-A1) along with corresponding weight and bias matrix given in Table 6 is recommended for general use in order to predict the effective strength of the joint.

The mean error in the prediction of the joint effective strength by various regression models

Table 6 Connection weights and biases for Model-A1 (refer to Fig. 2) (output bias = 0.6582).

No. of neurons			Inp	out weigl	nts			Output weights	Input
neurons	h	c	$ ho_c$	λ	$p_s$	$f'_{cc}$	$f'_{cs}$	(r)	blases
1	0.707	0.512	0.992	-0.833	0.322	-0.724	-1.508	0.971	2.053
2	-0.511	0.269	0.629	1.086	0.205	-0.493	-2.484	1.303	1.962
3	-1.050	-0.199	-0.685	0.693	1.299	-1.322	-0.503	-1.017	2.290
4	-0.003	1.462	0.906	1.946	-0.618	-0.419	0.789	0.339	-1.496
5	0.260	0.328	1.568	-0.953	-1.109	0.767	0.529	-0.181	-1.576
6	0.033	-0.828	-1.114	-1.016	0.865	-2.501	-0.966	-0.237	1.426
7	-0.009	-5E-04	0.468	-0.472	1.072	-1.301	1.202	-1.052	1.019
8	0.006	-0.889	-0.556	-0.488	1.151	0.123	0.501	0.159	-0.976
9	1.032	-0.303	-0.452	-1.037	0.150	-1.025	0.473	-0.053	1.495
10	-0.466	-1.140	-1.530	-0.622	-0.423	0.768	2.033	0.311	-0.425
11	-0.652	-0.353	0.816	-0.531	1.931	0.047	0.990	0.575	1.188
12	-0.187	0.593	1.491	-0.028	-0.480	0.689	-1.413	-2.172	1.190

Table 7 Connection weights and biases for Model-A2 (refer to Fig. 3) (output bias = 0.3827).

No. of neurons		]	Input we	ights		Output weights	Input
neurons	h/c	$ ho_c$	λ	$100p_s/f'_{cs}$	$f'_{cc}/f'_{cs}$	(r)	Diases
1	-0.358	0.873	0.054	-1.530	-0.677	-1.273	-0.656
2	-0.897	1.106	-1.173	0.457	2.095	-1.362	1.469
3	0.307	0.079	-0.130	-0.746	1.184	0.056	1.203
4	-1.123	0.873	-0.415	-0.250	1.280	-1.033	1.268
5	0.586	-1.484	1.539	1.056	-0.689	-0.672	-1.694
6	-0.440	1.529	-1.071	-1.262	0.387	1.127	1.104
7	-0.089	-1.457	0.405	1.167	0.261	-0.694	-1.907
8	-2.337	3.203	-0.080	-0.505	0.930	-0.764	-0.994
9	-0.582	0.355	-1.046	-2.088	0.518	1.152	-0.482
10	-0.503	-1.154	-0.370	1.367	-2.367	0.372	-0.455
11	-1.871	0.039	0.849	0.565	-2.235	1.081	-0.925
12	-0.596	-0.743	-0.664	1.480	-2.479	-0.774	2.246

(Eq. (1-6)) may be compared with the performance of neural network Model-A1 where the mean error is only 7.4%. On the other hand the mean errors calculated using regression models by Shah and Ribakov [22], Ospina and Alexander [17], ACI [1], and CSA [5] are 18.31, 15.69, 20, and 18.37%, respectively. The histogram of percentage error of a neural network model in comparison with the corresponding histograms for the earlier regression based models [1, 5, 17, 22] given by Eq. (1-6) is shown in Fig. 6. It is observed from this figure that for 72% of the data the percentage error is less than 10% for the neural network model, whereas the percentage error in the regression based models [1, 5, 17, 22] in the same percentage of data is about 25%. Similarly, for 93% of the test data the percentage error for the neural network Model-A1 obtained is less than 25%, while for almost the same percentage of data the regression based models [1, 5, 17, 22] are showing the percentage error as 36%. This clearly indicates the supremacy of the neural network model over the regression models.

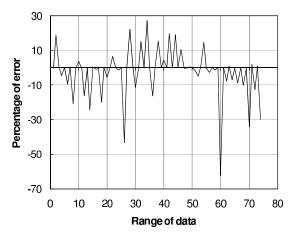


Figure 7 Percentage error in prediction of effective strength by Model-A1 for individual data points.

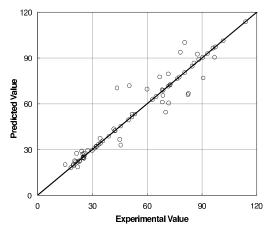


Figure 8 Observed versus predicted effective strength.

### 8 CONCLUSIONS

A generalized model for predicting the slab-column joint effective strength using neural network (NN) has been developed. The network predictions were generally more satisfactory than those given by traditional regression equations because of low errors and high correlation coefficients. Predictions based on raw data  $(h, c, \rho_c, \rho_s, \lambda, p_s, f'_{cc})$  and  $f'_{cs}$  were better than those based on the grouped dimensionless form of the data  $(h/c, \rho_c, \rho_s, \lambda, p_s/f'_{cs})$ , and  $f'_{cc}/f'_{cs}$ .

The NN with one hidden layer was selected as the optimum network to predict the effective strength of joint. The network configuration of Model-A1 with feed-forward back propagation is recommended for general use in order to predict the effective strength of joint.

Sensitivity analysis was performed in order to determine the relative significance of each of the independent parameters (input neurons) on the joint effective strength (output) in both of the NN models that were used in the frame of this study. On the basis of this analysis it was observed that the slab confinement factor, the slab thickness, and the column concrete strength are the three most significant parameters for the prediction of effective strength of the joint. From the study of sensitivity of the two models as well as keeping in view the variability in the outcome resulting from application of different analytical schemes, it is felt that the network which requires all input quantities may be followed for generality. Results of this study demonstrate that the NN model is far better than the regression one because it more precisely determines the effective strength of a column-slab joint and is, therefore, recommended for general use in order to predict the effective strength of the joint.

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