

Comparative analysis of normative provisions for seismic design and detailing of reinforced concrete structures

Análise comparativa das considerações normativas para dimensionamento e detalhamento sísmico de estruturas de concreto armado

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Abstract

The main objective of this work is to carry out a comparative analysis between the methods and provisions of the Brazilian code ABNT NBR 15421:2006 and those of the ASCE/SEI 7 and the Eurocode 8, on the seismic design of structures. The similarities and differences between these standards, as far as the application of the Equivalent Lateral Forces method (ELFM) and the Response Spectrum method (RSM) are concerned, will be addressed. The responses will be evaluated for a case study that will be modelled by the SCIA Engineer 17 software. This paper also presents some comments on the detailing of reinforced concrete structures to ensure a good performance under seismic loading, allowing for a more favourable interpretation of the seismic analysis results.

Keywords: seismic analysis, response spectrum, ABNT NBR 15421:2006, Eurocode 8, ASCE/SEI 7.

Resumo

O objetivo principal deste trabalho é fazer uma análise comparativa entre os métodos e considerações da norma brasileira ABNT NBR 15421:2006 e as provisões do ASCE/SEI 7 e do Eurocódigo 8, quanto ao dimensionamento sísmico de estruturas. São verificadas as similaridades e as diferenças entre as instruções normativas, quanto à aplicação do Método das Forças Equivalentes (MFE) e do Espectro de Resposta (MER). Os resultados serão avaliados por meio de um estudo de caso que será processado com auxílio do programa computacional SCIA Engineer 17. O artigo também apresenta alguns comentários sobre o detalhamento de estruturas de concreto armado que visam a garantir um bom desempenho sísmico, possibilitando uma interpretação mais favorável dos resultados sísmicos analisados.

Palavras-chave: análise sísmica, espectro de resposta, ABNT NBR 15421:2006, Eurocódigo 8, ASCE/SEI 7.

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1. Introduction

South America is a region with very heterogeneous degrees of seismicity. The eastern border is inserted in an internal tectonic plate, which guarantees greater stability and consequent reduction in the influence of the seismic activities. On the other hand, the western border has a large seismic activity, for it is located on two plate boundaries. This formation, to a certain extent, justifies the fact that the countries located in the western region of South America have already had norms for seismic design for some decades, while in Brazil, the approval of the ABNT NBR 15421: 2006 [1], that defines the procedures for designing buildings in seismic regions, happened only in 2006.

As it can be seen from Figure 1, the influence of seismic events in Brazil, North America and Europe are considerably different, a fact that is very evident in the assumptions of the seismic standards of each of those regions. Nevertheless, there are many similar considerations that will be explored ahead.

The Brazilian standard presents a mapping of seismic accelerations in the country quite compatible with the study presented in Figure 1, which leads to the understanding that the risk of dramatic seismic damages in Brazil is almost zero. However, more recent studies developed by the University of São Paulo, available at <http://jornal.usp.br/tv-usp/usp-atualiza-mapa-de-risco-de-tremores-de-terra-no-brasil/>, warn for the need to update this mapping. The NBR exempts seismic analysis for areas with design seismic accelerations of less than 0.025 g and requires a fairly simple verification for accelerations between 0.025 g and 0.050 g, while the Eurocode 8 [2] allows for no verification for design accelerations smaller than 0.050g. The American ASCE / SEI 7 [3] standard, unlike the others, uses a response spectrum mapping of accelerations and importance categories to define risk categories for structures, which are defined from "A" to "F", and then exempts seismic analysis for the first defined category (A).

Section 2 presents in general terms the objectives and criteria adopted by the three standards. Considering the great difference in the occurrence and magnitude of the seismic events in Brazil, Europe and the United States, it should be expected that in the international standards there would have, as indeed they have, a considerably greater amount of information, limitations and instructions for the considerations to be made. In this article, the assumptions of the three standards will be presented, so that they can be compared.

Section 3 shows a comparative study between the parameters adopted by ABNT NBR 15421: 2006 [1], ASCE / SEI [3] and Eurocode 8 [2] for the EFM. Similar to section 3, section 4 presents a comparative study between the parameters adopted by the three standards for the RSM.

Then, in section 5, a case study is analyzed by both, the EFM and the RSM, resorting to SCIA Engineer 17 software [4] and using the parameters of each of the three standards. Two situations are considered, one based on rocky terrain and the other on less rigid ground, which allows to illustrate and identify the differences between the results obtained by each method, as well as the variations between the provisions of each standard.

In section 6 some comments are presented regarding the structural detailing that aim at guaranteeing a better seismic performance for the reinforced concrete structures, allowing them to fit into a more favorable design hypothesis.

2. General concept

The objective of ABNT NBR 15421: 2006 [1], ASCE / SEI [3] and EUROCODE 8 [2] is complementary to other reference standards, with regard to the safety requirements of structures in civil construction, when subjected to seismic actions, aiming at preserving human life, reducing the expected damages and guaranteeing that critical buildings remain operational during and after a seismic event. However, NBR only covers the usual structures, built in a conventional way,

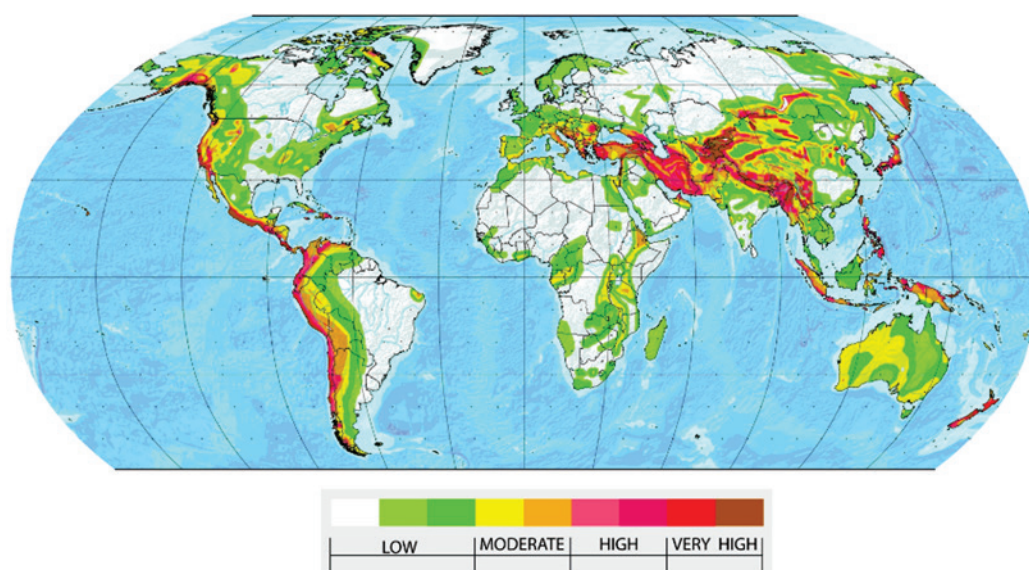


Figure 1

Characteristic horizontal seismic acceleration mapping in the world

Table 1
Importance coefficient

NBR	Category		Nature of occupation	I (NBR)	I (ASCE)	I (EUROCODE)
	ASCE	EUROCODE				
-	I	I	Minor importance building (Agricultural)	-	1	0.65
I	II	II	Common buildings	1	1	1
II	III	III	Relevant buildings (schools, etc.)	1.25	1.25	1.45
III	IV	IV	Essential buildings (hospitals, headquarters, etc.)	1.5	1.5	1.95

while EUROCODE and ASCE make provisions that are valid for a broader class of constructions, with specific provisions for bridges, viaducts, silos, chimneys, etc. Yet, none of these standards covers the special structures of nuclear power plants, offshore structures and large dams. In this article, the concepts related to reinforced concrete buildings will be primarily addressed.

Regarding the probabilistic considerations of seismic loads, the Brazilian and European standards consider a return period of 475 years (equivalent to a 10% probability of the project earthquake being exceeded in 50 years) for the ultimate limit state and excessive displacements. Additionally, the European standard requires a further analysis regarding damage control, adopting, in this case, a return period of 95 years. The US standard refers to an application, found at <http://earthquake.usgs.gov/designmaps> [6], where the seismic parameters for calibrating the spectrum are available, which in turn adopts a return period of 2475 years, based on a 2% probability of exceeding the project earthquake in 50 years.

The three standards work with the so-called importance coefficient in order to classify the risk and potential damage of the analyzed structures. The importance categories adopted are very similar, however, EUROCODE admits two different sets of coefficients, due to the existence of more than one type of seismic origin in the European region. In this study, it will be considered the set of parameters adopted for what, in EUROCODE 8 [2], is named as "Type 1", because this is the one with the set of parameters that most resembles those considered in the other standards. Table 1 presents the comparison between the aforementioned importance coefficients.

It is not plausible to consider that the structures perform in the elastic regime during a seismic event, therefore, the standards con-

sider response-modification coefficients (reduction of efforts and increase of displacements), which takes into account the nonlinear regime of each structural system. Table 2 shows the coefficients adopted for some of the main conventional structural systems. The coefficients α_u/α_1 are defined in item 6.3.1 of EUROCODE 8 [2], depending on the specific type of the analyzed structure (number of floors, number of frames in plan, bracing, etc.), while the superior limit value of the coefficient is given according to item 6.3.2. It is worth mentioning that international standards indicate a much larger number of structural systems, with a much more detailed description, allowing to select the modification coefficients in a much more precise manner.

Once the seismic forces have been determined, the combination suggested in the standards, which considers simultaneously the dynamic and static actions, can be implemented in order to obtain the structural design forces.

The design methodology of the standards addressed in this article is the so-called Force-Based Design (FBD). Although the trend of some contemporary proposals for designing earthquake resistant structures is to use different methodologies—such as the Performance-Based Design (PBD), which establishes target-displacements defined by a pre-established performance level, these standards have not yet incorporated them with due autonomy. This is, in fact, typical of technical standards in Engineering: between the proposals for the state-of-the-art improvement and its effective incorporation into the text of the standards, there is a great temporal lapse due to the necessary and gradual cultural change that must take place not only in the technical environment, as well as in the productive sector. By the way, as explained by Carvalho in

Table 2
Response-modification factor

Structural systems (frames)	NBR / ASCE		EUROCODE
	Modification factor (R)	Displacement amplification (C_d)	Modification factor and displacement amplification (α)
Concrete frame – usual	3	2.5	3.0 α_u/α_1
Concrete frame – special	8	5.5	4.5 α_u/α_1
Moment-resistant steel frame – usual	3.5	3	3.0 α_u/α_1
Moment-resistant steel frame – special	8	5.5	4.5 α_u/α_1
Braced steel frame – usual	3.25	3.25	3.0 α_u/α_1
Braced steel frame – special	6	5	4.5 α_u/α_1

Table 3
Ground classification

Ground class	V_s (NBR / ASCE)	NSPT (NBR / ASCE)	V_s (EUROCODE)	NSPT (EUROCODE)
	m/s	number	m/s	number
A	$V_s > 1500$	-	$V_s > 800$	-
B	$1500 > V_s > 760$	-	$800 > V_s > 360$	$N > 50$
C	$760 > V_s > 370$	$N > 50$	$360 > V_s > 180$	$50 > N > 15$
D	$370 > V_s > 180$	$50 > N > 15$	$V_s < 180$	$N < 15$
E	$V_s < 180$	$N < 15$		
F (S1 E S2)	Specific evaluation		Specific evaluation	

[2], with reference to EUROCODE 8, "... the use of force-based design is well established and, as mentioned above, is adopted in EN 1998-1 as the reference method, because most of other actions with which structural designers have to cope are forces imposed to the structures. Hence within the overall design process the use of a force-based approach, even for seismic actions, is very practical and attractive. Furthermore, analytical methods for a displacement-based approach in seismic design are not fully developed and not familiar to the ordinary designer". Only in an alternative way, EUROCODE 8 opens the possibility of a non-linear analysis (pushover) according to the "displacement-approach". In addition, although the PBD is mentioned in item 1.3.1.3 of the American Standard ASCE / SEI 7 (2016), the text itself requires that the results obtained be backed up by analyzes made by the force-based approach. Therefore, PBD will not be addressed in this study.

According to Arai [5], the three norms mention the basic principles of an earthquake-resistant project, in which one must seek structural simplicity, uniformity, plant and elevation regularity, bi-directional stiffness, torsional stiffness, diaphragm behavior on various floors and proper foundation.

The Brazilian standard ABNT NBR 15421: 2006 [1] cites five types of geometric irregularities, which are classified as three in the horizontal plane: 1) torsional, 2) discontinuity in force trajectory in the horizontal plane and 3) elements that support the horizontal plane (columns and walls) not parallel to the vertical axis of the structural system; and two vertical geometric irregularities: (4) discontinuity in the vertical stress path; and (5) characterization of a "weak pavement", which has a lateral resistance of less than 65% of the immediately-higher-pavement strength. Generally, the Brazilian standard requires the use of a spatial model when there are irregularities in the plane. For structures with vertical irregularities, the NBR calls for the application of a coefficient called "over-resistance", which acts by increasing the seismic forces on the structure, ensuring that its design generates a structure with a higher resistance. The American ASCE / SEI 7 [3] explores in much more detail possible geometric irregularities in the structures, carefully defining the situations and conditions in which the "over-resistance" coefficients must be applied, among other limitations. Similarly, EUROCODE deals with irregularities in the plan requiring the use of a spatial model and vertical irregularities by reducing the response modification coefficient, which is conceptually equivalent to the use of the over-resistance coefficient adopted in NBR and ASCE.

Regarding the methods of analysis, the use of RSM or a time-domain analysis for any structural system is allowed in ASCE / SEI

7 [3]. EFM is allowed for all structures in categories B and C and for categories D, E and F when they are:

- i. Risk category I or II, up to two floors;
- ii. Light frame constructions;
- iii. Structures with no geometric irregularities, with fundamental period $< 3.5 T_s$ (where T_s is defined by equation (10));
- iv. Structures up to 50m high, with limitations in geometric irregularities.

It is worth noting that the NBR defines the main method as the EFM, while the EUROCODE defines the RSM as the base method. In addition, EUROCODE advises against the use of EFM when there are vertical irregularities, a consideration that is not made in the NBR.

As for the land classes definitions, the three standards take into account the propagation velocity of the secondary waves (V_s) and the number of blows in the SPT test. EUROCODE gives a much more detailed description of the type of soil formation for each class, however the parameters used in the classification are quite similar. Although the land classes defined in the NBR and the ASCE are identical, the American standard requires the submission of a detailed geotechnical report for categories C, D, E or F, including foundation recommendations to mitigate the risk analysis. Table 3 presents the comparison of the terrain classification.

In EUROCODE 8 [2], as well as in ASCE 7 [3], the elastic spectrum for horizontal earthquake is defined from three control periods and three stages: constant acceleration, constant velocity and constant displacement. Similar to the provisions of ABNT NBR 15421: 2006 [1], the other standards allow a nominal structural damping rate of 5%; however, EUROCODE considers a parameter that allows adjusting the spectrum for situations with different damping rates, other than 5%. It should be noted that the structural damping ratio adopted in a seismic analysis is higher than the 2% value usually used for dynamic analysis of reinforced concrete structures in the elastic regime, since, in a seismic situation, the structures are considered to perform in the elastoplastic regime, and as so, the equivalent structural damping must take into account dissipative inelastic effects. This is done, in a practical way, with an increase in the damping ratio. The NBR basically adopts the same assumptions of the old American UBC standard [7]. Thus, the constant displacement stage is not characterized.

Figure 2 illustrates the spectrum of the analyzed standards, as a function of the parameters that defines them. The parameters for each standard are explained in detail ahead, with the expressions that define the graph curves.

The following expressions define the design spectrum in ABNT NBR 15421: 2006 [1]:

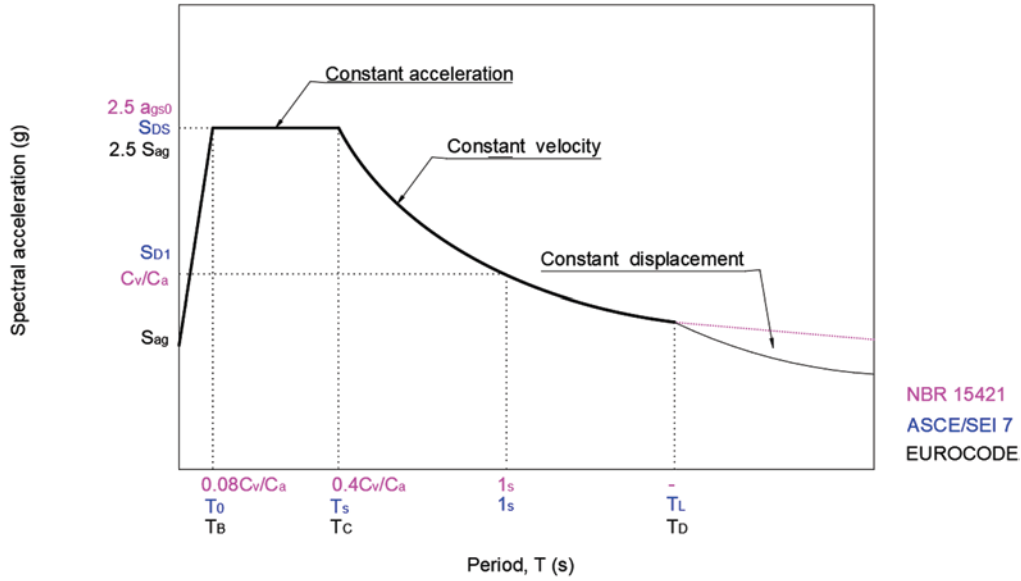


Figure 2
Elastic response spectrum, adapted from Eurocode 8 [2]

$$\text{for } 0 \leq T \leq 0.08 \frac{C_v}{C_a} \quad S_a(T) = a_{gs0} \times \left(18.75 \times T \times \frac{C_v}{C_a} + 1.0 \right) \quad (1)$$

$$\text{for } 0.08 \frac{C_v}{C_a} \leq T \leq 0.4 \frac{C_v}{C_a} \quad S_a(T) = a_{gs0} \times 2.5 \quad (2)$$

$$\text{for } T \geq 0.4 \frac{C_v}{C_a} \quad S_a(T) = \frac{a_{gs1}}{T} \quad (3)$$

where:

$$a_{gs0} = C_a \times a_g$$

$$a_{gs1} = C_v \times a_g$$

The parameters a_{gs0} and a_{gs1} are the spectral accelerations for a period of zero and one seconds, respectively, obtained as a function of the design characteristic acceleration a_g . The parameters C_a and C_v (amplification factors in soil for the respective periods of zero and one seconds) are defined in Table 3 of ABNT NBR 15421: 2006 [1], according to the land class and the characteristic acceleration defined by the seismic zone where the structure is located. The natural period "T" is the period of each mode of vibration of the analyzed structure, in seconds.

ASCE / SEI 7 [3] defines the maximum considered earthquake (MCE) - through the parameters:

$$\begin{aligned} S_{ms} &= F_a \times S_s \\ S_{m1} &= F_v \times S_1 \end{aligned} \quad (4)$$

where:

F_a and F_v are the weighting coefficients in soil, defined in Tables 11.4-1 and 11.4-2 of ASCE/SEI 7 [3], which are presented in Table 5; S_s and S_1 are the spectral acceleration response parameters for the periods of 0.2 and one seconds, respectively, which after being adjusted by the weighting coefficients in the soil, give rise to the parameters S_{ms} and S_{m1} . The S_s and S_1 parameters are provided by the detailed maps, which can be found at <http://earthquake.usgs.gov/designmaps>.

For the characterization of the design spectrum, the parameters S_{DS} and S_{D1} are defined, respectively, by $\frac{2}{3} \times S_{ms}$ and $\frac{2}{3} \times S_{m1}$, presented in the equation (4).

The following expressions define the design spectrum in ASCE:

$$\text{for } T < T_0 \quad S_a(T) = S_{DS} (0.4 + 0.6 \frac{T}{T_0}) \quad (5)$$

$$\text{for } T_0 \leq T \leq T_S \quad S_a(T) = S_{DS} \quad (6)$$

$$\text{for } T_S \leq T \leq T_L \quad S_a(T) = \frac{S_{D1}}{T} \quad (7)$$

$$\text{for } T \geq T_L \quad S_a(T) = \frac{S_{D1} \times T_L}{T^2} \quad (8)$$

where:

S_a is the spectral acceleration for each defined period T (in s).

$$T_0 = 0.2 \times \frac{S_{D1}}{S_{DS}} \quad (9)$$

$$T_S = \frac{S_{D1}}{S_{DS}} \quad (10)$$

T_L = transition period shown in figures 22-12 to 22-16 of ASCE/SEI 7 [3].

Considering that Europe is a region with more than one seismic origin, EUROCODE defines two typical design spectra, according to Arai [5]: Type 1 for regions of magnitudes greater than 5.5 and Type 2 for regions smaller than 5.5.

The spectrum is then defined by the following expressions:

$$\text{for } 0 \leq T \leq T_B \quad S_{a,d}(T) = a_g \times S \times \left(\frac{2}{3} + \frac{T}{T_B} \times \left(\frac{2.5}{q} - \frac{2}{3} \right) \right) \quad (11)$$

$$\text{for } T_B \leq T \leq T_C \quad S_{a,d}(T) = a_g \times S \times \frac{2.5}{q} \quad (12)$$

$$\text{for } T_C \leq T \leq T_D \quad S_{a,d}(T) = a_g \times S \times \frac{2.5}{q} \times \frac{T_C}{T} \geq 0.2 a_g \quad (13)$$

$$\text{for } T \geq T_D \quad S_{a,d}(T) = a_g \times S \times \frac{2.5}{q} \times \frac{T_C \times T_D}{T^2} \geq 0.2 a_g \quad (14)$$

in which:

$S_{a,d}$ is the ordinate referring to the adopted design acceleration spectrum;

S, T_B, T_C and T_D are defined in Tables 3.2 and 3.3 of Eurocode 8 [2] and presented at Table 4;

a_g is the surface design acceleration, derived from the characteristic acceleration $a_{g,r}$, defined by the seismic zone available in each country's National Annex.

The NBR and the ASCE assume that the responses obtained by the response spectrum should be adjusted by the response-modification factors shown in Table 2. The Eurocode takes into account the response-modification factor (q) already embedded in the expressions (11) to (14). Therefore, the spectrum already provides the compatibilized results.

3. Equivalent lateral forces method

ABNT NBR 15421: 2006 [1] adopts the Equivalent Lateral Forces Method (EFM) as the main analysis procedure and allows its use for all structures to which the standard refers. EUROCODE 8 [2], however, limits its use to structures that are uniform in elevation and have fundamental periods of less than $4 \times T_c$ or $2s$.

The Brazilian standard defines EFM by the following expressions, based on the parameters of the response spectrum and the impor-

tance and response-modification coefficients, defined in section 2 (valid for each direction analyzed):

horizontal force at the base:

$$H = C_s \times W \tag{15}$$

C_s is the coefficient of seismic response, given by:

$$C_s = \frac{2.5 \times \frac{a_{gs0}}{g}}{\frac{R}{T}} \text{ limited to } 0.01 < C_s < \frac{2.5 \times \frac{a_{gs1}}{g}}{T \times \frac{R}{T}} \tag{16}$$

The parameters used are those defined in section 2, where W is the total weight of the structure and T is the fundamental vibration period of the structure in seconds, relative to the first mode of vibration in the direction analyzed, or by the simplification that follows:

$$T = C_t \times h^z \tag{17}$$

where h is the height of the structure in meters above the base, with the parameters " C_t " and " z " defined at Table 5.

The total horizontal force at the base (H) is distributed vertically, between the various elevations " x " of the structure, according to the expression below:

$$F_x = C_{vx} \times H \tag{18}$$

Table 4
Design spectrum parameters

Ground class (V_s)	ASCE/SEI 7										
	Parameter F_a					Parameter F_v					
	S_s					S_1					
	0.25	0.5	0.75	1	> 1.25	0.1	0.2	0.3	0.4	0.5	> 0.6
$V_s > 1500$	0.8	0.8	0.8	0.8	0.8	0.8	0.8	0.8	0.8	0.8	0.8
$V_s > 800$	0.9	0.9	0.9	0.9	0.9	0.8	0.8	0.8	0.8	0.8	0.8
$V_s > 370$	1.3	1.3	1.2	1.2	1.2	1.5	1.5	1.5	1.5	1.5	1.4
$V_s > 180$	1.6	1.4	1.2	1.1	1	2.4	2.2	2	1.9	1.8	1.7
$V_s < 180$	2.4	1.7	1.3	ASCE 11.4.8	ASCE 11.4.8	4.2	ASCE 11.4.8	ASCE 11.4.8	ASCE 11.4.8	ASCE 11.4.8	ASCE 11.4.8

Ground class (V_s)	NBR				EUROCODE							
	C_a		C_v		Type 1				Type 2			
	< 0.1	0.15	< 0.1	0.15	S	T_B	T_C	T_D	S	T_B	T_C	T_D
$V_s > 1500$	0.8	0.8	0.8	0.8	-	-	-	-	-	-	-	-
$V_s > 800$	1	1	1	1	1	0.15	0.4	2	1	0.05	0.25	1.2
$V_s > 370$	1.2	1.2	1.7	1.7	1.2	0.15	0.5	2	1.35	0.05	0.25	1.2
$V_s > 180$	1.6	1.5	2.4	2.2	1.15	0.2	0.6	2	1.5	0.1	0.25	1.2
$V_s < 180$	2.5	1.1	3.5	3.4	1.35	0.2	0.8	2	1.8	0.1	0.3	1.2

Table 5
Coefficients " C_t " and " z "

Structure type	NBR / ASCE		EUROCODE	
	C_t	z	C_t	z
Moment resistant steel frame	0.0724	0.8	0.085	0.75
Concrete frame	0.0466	0.9	0.075	0.75
Braced steel frame	0.0731	0.75	0.075	0.75
Other structures	0.0488	0.75	0.05	0.75

where the coefficient C_{vx} considers the weight and height “x” in relation to the base, for the floor to be loaded.

$$C_{vx} = \frac{W_x h_x^k}{\sum_{i=1}^n W_i h_i^k} \quad (19)$$

where W_x is the effective weight corresponding to the floor of the analyzed “x” elevation, h_x is the distance from the floor in elevation “x” relative to the base; W_i and h_i are analogous to W_x and h_x , yet for elevation “i”; and k is a coefficient relative to the natural period T (in s):
 $k = 1$ for $T < 0.5s$;
 $k = (T + 1.5)/2$ for $0.5s < T < 2.5s$;
 $k = 2$ for $T > 2.5s$.

The displacements obtained must be multiplied by the ratio $\frac{C_d}{I}$, in which C_d is given in Table 2 and the coefficient I in Table 1.

The formulation for EFM presented by ASCE / SEI 7 [3] is essentially the same as the one presented in the NBR, with the following particularities:

1. The seismic response coefficient C_s , defined as a function of the parameters presented in section 2, is given by:

$$C_s = \frac{S_{DS}}{\left(\frac{R}{T}\right)} \text{ limited to } \frac{S_{D1}}{T\left(\frac{R}{T}\right)} \text{ for } T < T_L, \text{ or } \frac{S_{D1} \times T_L}{T^2\left(\frac{R}{T}\right)} \text{ for } T > T_L \quad (20)$$

where C_s shall not be less than:

$$\frac{0.5 \times S_1}{\frac{R}{T}} \text{ for seismic zones with } S_1 \geq 0.6g \quad (21)$$

$0.044 \times S_{DS} \times I$ for other cases

2. In addition to the simplification of the fundamental period of the structure presented by NBR, for reinforced concrete structures or moment-resistant steel frames with up to 12 floors and at least three meters between each floor, it is possible to estimate the fundamental period T (s) by:

$$T = 0.1 \times N \quad (22)$$

with N = number of floors above the base.

In any event, the assumed fundamental period shall not exceed the product of equation (17) by the coefficient C_u established in Table 12.8-1 of ASCE / SEI 7 [3].

Eurocode 8 [2] presents a slightly different formulation for the total force in the base which, presented in the notation of this article, is given by:

$$H = S_{a,d}(T) \times W \times \lambda \quad (23)$$

where T is the fundamental period of the structure in seconds; $S_{a,d}$ is the ordinate referring to the design acceleration spectrum adopted, normalized with respect to the acceleration of gravity; W is the total weight of the structure and $\lambda = 0.85$ when $T < T_c$ and the building is more than two-floors high; or $\lambda = 1.0$ in the other cases. In addition to the estimations for the fundamental period (T) defined in the NBR, Eurocode allows the use of the following expression:

$$T = 2 \times \sqrt{d} \quad (24)$$

with d being the lateral displacement at the top of the building, in meters, referring to the forces of gravity acting in the horizontal direction. For the distribution of seismic forces through the height of the structure, Eurocode considers the following formulation:

$$F_x = H \times \frac{s_x \times m_x}{\sum s_i \times m_i} \quad (25)$$

where:

m_x = floor mass at elevation “x”;

m_i = floor mass at elevation “i”.

The parameters s_x and s_i can be taken with respect to a linear distribution in relation to the height of the building, where:

s_x = floor height at elevation “x” with respect to the base;

s_i = floor height at elevation “i” with respect to the base.

Alternatively, one may adopt these parameters with respect to the displacement of the masses in the fundamental mode of vibration of the structure, where:

s_x = relative displacement of the floor at elevation “x”;

s_i = relative displacement of the floor at elevation “i”.

The displacements obtained by this method must be multiplied by the displacement amplification coefficient “q”, shown in Table 2.

Among the “advantages” of the equivalent lateral force method it is frequently cited the ease for application in projects and the low computational cost. One should, however, use this method with caution, since, as shown in section 5, it is based only on the response of the first mode of vibration of the structure; therefore, may not yield good results in cases where higher modes are excited.

4. Response spectrum method

The three analyzed standards define that the analysis by response spectrum is done by modal superposition, with a number of modes analyzed so that at least 90% of the total mass participates in the response. In addition, the standards allow for a modal combination as indicated by the Square Root of the Sum of the Squares (SRSS) method, to be performed whenever the natural frequency of one mode is at least 10% higher than the frequency of the adjacent mode.

According to the expression 3.7 of Eurocode 8 [2], for natural periods of up to 4s, the elastic response spectrum of the displacements (S_{De}) can be obtained directly from the elastic acceleration spectrum (S_e), defined in the item 3.2.2.2 of the Eurocode 8 [2], by means of the following expression:

$$S_{De}(T) = S_e(T) \times \left[\frac{T}{2\pi}\right]^2 \quad (26)$$

For the European standard, the design spectrum ($S_{a,d}$) has the coefficient “q” embedded in the equation, so the obtained stresses are taken with their nominal values, but the displacements obtained by means of $S_{a,d}$ must be multiplied by the parameter “q” to obtain the final displacements. The forces of the spectral analysis obtained by NBR and ASCE should be multiplied by $\frac{I}{R}$, where I and R are given respectively in Table 1 and Table 2. Regarding the displacements, the two standards determine that they must be multiplied by the ratio $\frac{C_d}{R}$, where C_d and R are given in Table 2.

The Brazilian standard allows RSM to reduce the shear stress in the base by up to 15% with respect to the EFM. Hence, if the base shear force obtained by the spectral analysis (H_s), is less than 85% of the base shear force obtained by EFM (H_f), all the forces obtained by the spectral analysis should be adjusted by multiplying it by the ratio $0.85H_f / H_s$. This correction is not needed for the

displacements. The American standard does not allow such reductions in relation to the EFM. Therefore, for the above case, both stresses and displacements would have to be multiplied by the coefficient H_r / H_s . Eurocode does not correct the values obtained through RSM in relation to EFM; therefore, the values obtained from the analysis can be used at once.

5. Discussions and results

For general torsion checks, the three standards specify an accidental eccentricity in relation to the center of mass of the building. This accidental eccentricity is estimated as $5\% \times L_i$, with L_i being the largest linear length in the floor plan, in the direction perpendicular to the seismic action. If an analysis is made considering two orthogonal directions, the accidental eccentricity should only be applied to the one that maximizes the effects, the simultaneous application in both directions being exempted. Thus, the torque applied to each floor is given by the floor lateral force multiplied by the corresponding accidental eccentricity.

To verify the second-order effects, the standards specify a coefficient of stability Θ given by:

$$\theta = \frac{P_x \times \Delta_x}{H_x \times h_x} \quad (27)$$

where:

P_x = service vertical force acting on the floor;

Δ_x = interstory drift;

H_x = shear force acting on the pavement;

h_x = interstory distance.

The three standards state that for Θ values less than 0.1, no second order effects need to be considered. For values of Θ greater than 0.1 but less than the Θ_{max} accepted, displacements and stresses will be multiplied by the ratio $\frac{1}{1-\theta}$, Θ_{max} being defined by:

$$\text{NBR and ASCE: } \theta_{max} = \frac{0.5}{Cd} \leq 0.25;$$

Eurocode: $\theta_{max} = 0.2$.

CASE STUDY

In order to comparatively analyze the provisions of the three standards, a three-floor conventional reinforced concrete model building, similar to that used by Lima and Santos [8] was adopted. The 3D model along with the axis directions considered in the analysis are shown in Figure 3. It should be noted that in Figure 3, the elevation coordinate has been defined as "z", differently from what has been used in equations (18), (19), (25) and (27), in which it has been termed "x".

This building was subdivided into two groups of analysis, in which the first one considers a conventional reinforcement detail (DC) and the other a specific reinforcement earthquake-resistant detail (DS). The building has columns with a 50 x 40 cm² section, beams with an 80 x 30 cm² section and slabs of 11cm thickness, built with an $f_{ck} = 30$ MPa concrete.

As seismic characteristics, an acceleration zone $a_g = 0.10g$ was considered. For the application of the American standard, the city of Saint Louis, Oakville, in the United States was adopted which, according to the Unified Hazard Tool available at

<http://earthquake.usgs.gov/designmaps>, features a characteristic spectral acceleration (PGA) of 0.10g for a return period of 475 years, making this location compatible with the seismic characteristics considered for the other two standards. It is worth remembering though, that for the application of this standard's equations, the parameters for a return period of 2475 years, obtained on February 22, 2018 from the same website of the American government, had to be applied.

The analyses were computed for loadings in the parallel direction to the "x" axis, for two types of foundations, one in sand with average SPT $N = 30$ and another in bedrock with class of terrain "A", as presented in Table 3.

Eurocode provisions were taken for a Type 1 earthquake spectrum.

5.1 Lateral equivalent force method analysis

For the model building, the weight of each floor was approximately and uniformly determined as:

Permanent load per floor: 1740 kN;

Total permanent load: $3 \times 1740 = 5220$ kN.

With the aid of the expressions presented in this study for the three standards, the parameters for the analysis, presented in Table 6, were obtained.

For the total shear forces at the base (H) obtained in each analysis, the equivalent vertical distributions were computed. Table 7 shows the calculated distribution for DC cases. The same procedure was adopted to obtain the distribution of the DS cases.

With the equivalent lateral forces calculated, an elastic analysis model was generated with the aid of SCIA Engineer 17 [4], from which the displacements and stresses in the structural elements were obtained, which are presented in Table 9 and in Table 10.

5.2 Response spectrum analysis

For the response spectrum analysis, the same base parameters presented in the previous subsection were used to generate the acceleration spectra and, consequently, the displacement spectra.

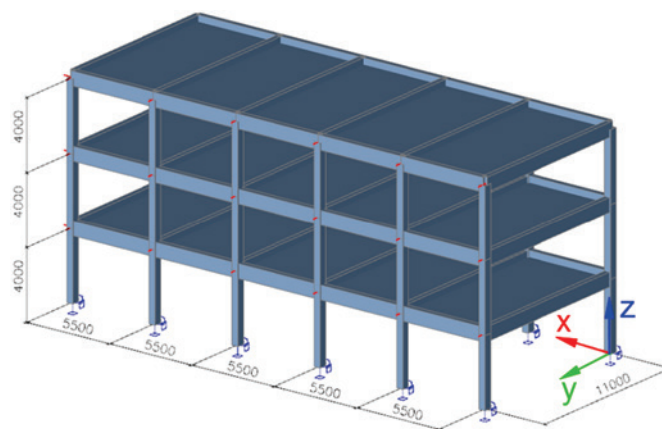


Figure 3
Reference building

Source: author

Table 6
Reference building parameters

NBR													
Soil class	R	I	T (s)	W (kN)	k	α_g	C_a	C_v	α_{gs0}	α_{gs1}	C_s	C_s max	H (kN)
(DC) Rigid soil	3	1	0.436	5220	1	0.1	1.6	2.4	0.16	0.24	0.133	0.183	696
(DC) Rock	3	1	0.436	5220	1	0.1	1	1	0.1	0.1	0.083	0.076	399
(DS) Rigid soil	8	1	0.436	5220	1	0.1	1.6	2.4	0.16	0.24	0.050	0.069	261
(DS) Rock	8	1	0.436	5220	1	0.1	1	1	0.1	0.1	0.031	0.029	150

ASCE - Saint Louis (Oakville)													
Soil class	R	I	T (s)	W (kN)	k	F_a	F_v	T_o	T_s	C_s	C_s min	C_s max	H (kN)
(DC) Rigid soil	3	1	0.436	5220	1	1.44	2.25	0.12	0.60	0.14	0.02	0.20	756
(DC) Rock	3	1	0.436	5220	1	0.90	0.80	0.07	0.34	0.091	0.01	0.071	368
(DS) Rigid soil	8	1	0.436	5220	1	1.44	2.25	0.12	0.60	0.05	0.02	0.07	284
(DS) Rock	8	1	0.436	5220	1	0.90	0.80	0.07	0.34	0.034	0.01	0.026	138

EUROCODE (Type 1)													
Soil class	q	I	T(s)	W (kN)	λ	α_g	S	T_b	T_c	T_d	S_d	H (kN)	
(DC) Rigid soil	3.6	1	0.484	5220	1	0.1	1.15	0.2	0.6	2	0.08	417	
(DC) Rock	3.6	1	0.484	5220	1	0.1	1	0.15	0.4	2	0.06	300	
(DS) Rigid soil	5.4	1	0.484	5220	1	0.1	1.15	0.2	0.6	2	0.05	278	
(DS) Rock	5.4	1	0.484	5220	1	0.1	1	0.15	0.4	2	0.04	200	

These spectra were inserted in SCIA Engineer 17 [4], from which the displacements and the stresses for the comparative analysis were obtained.

Figure 4 compares the spectra generated by each standard for each of the two foundation types assumed.

Ten modes of vibration were considered to perform the spectral analysis. Table 8, which presents the first six modes of the analyzed model, shows that the use of only three modes would be enough to reach 90% of mass translation in the analyzed direction (x), nonetheless, the software's standard was used.

5.3 Results

The comparative results of the analysis performed for the model building, through SCIA Engineer, are presented below, already considering the adjustments made by the response-modification coefficients ("R" and "q"), as well as the displacements coefficients ("C_d" and "q").

The values presented in Table 9 and Table 10 do not consider the forces and displacements compatibility for the RSM in relation to the EFM yet, as suggested in section 4. After this compatibilization has been carried out, the RSM responses are adjusted to the values presented in Table 11.

In this case study, when considering a conventional reinforcement

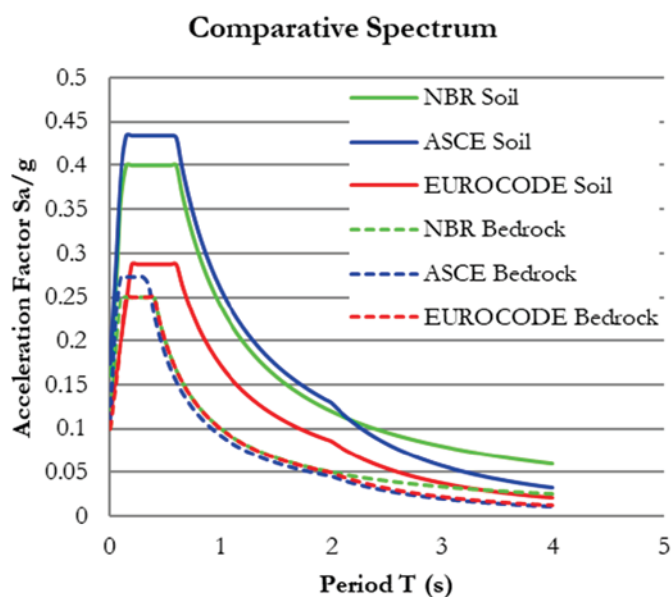


Figure 4
Spectra comparison

Source: author

Table 7
Distributed forces (rigid soil – DC)

Floor	h_x (m)	W_x (kN)	NBR		ASCE		EUROCODE		
			F_x (kN)	H_x (kN)	F_x (kN)	H_x (kN)	F_x (kN)	H_x (kN)	
Rigid soil	3	12	1740	348	348	378	378	208	208
	2	8	1740	232	580	252	630	139	347
	1	4	1740	116	696	126	756	69	417
Rock	3	12	1740	200	200	184	184	150	150
	2	8	1740	133	333	123	307	100	250
	1	4	1740	67	399	61	368	50	300

detail, one can perceive that the force-weighting coefficients, suggested by Eurocode, are more favorable than those presented by the NBR, in addition to the European spectrum being much milder. These aspects, in the analyzed case, lead to considerably smaller shear forces according to the European standard than those obtained by an equivalent analysis according to NBR. The American standard, on the other hand, has weighting coefficients similar to those of the NBR, but uses a slightly heavier response spectrum. Nevertheless, in compliance with the limitations of “ C_s ” imposed by the ASCE, presented in equations (20) and (21), which make the responses slightly different from those of a direct application of the American standard spectrum, the results are quite close to those

obtained by NBR for the EFM. However, with respect to RSM, the deviations between NBR and ASCE are much more pronounced, due to the American standard requirement that the RSM results be “scaled” to 100% of the shear base force obtained by the EFM. For the specific earthquake-resistant reinforcement detail shown in this example, the deviations between the NBR and the ASCE are very similar to those obtained for a conventional detailing. However, the deviations obtained with respect to the Eurocode acquire a very different proportion, since the relationships between the weighting coefficients for each type of detail are significantly different. Particularly for this study, regardless of the adopted standard, it is very clear that the adoption of an earthquake-resistant detail sub-

Table 8

Modal participation factors

Mode	Circular frequency(ω) [rad/s]	Period [s]	Cyclic frequency [Hz]	Mass share of each mode relative to the total					
				% translation axis x	% translation axis y	% translation axis z	% rotation axis x	% rotation axis y	% rotation axis z
1	119.322	0.5266	18.991	0.8815	0.0000	0.0000	0.0000	0.1152	0.0000
2	322.666	0.1947	51.354	0.0000	0.0000	0.0000	0.0000	0.0000	0.8464
3	349.009	0.1800	55.546	0.0871	0.0000	0.0000	0.0000	0.7666	0.0000
4	533.548	0.1178	84.917	0.0162	0.0000	0.0000	0.0000	0.0434	0.0000
5	983.627	0.0639	156.549	0.0000	0.0000	0.0000	0.0000	0.0000	0.1022
6	1.570.494	0.0400	249.952	0.0000	0.0000	0.0000	0.0000	0.0000	0.0245
Summation				0.9847	0.0000	0.0000	0.0000	0.9252	0.9730

Table 9

Analysis results – DC

	NBR EFM		NBR RSM		ASCE EFM		ASCE RSM		EUROCODE EFM		EUROCODE RSM	
	Soil	Rock	Soil	Rock	Soil	Rock	Soil	Rock	Soil	Rock	Soil	Rock
Disp. (mm)	33.50	19.25	28.50	13.50	36.50	17.75	31.00	12.50	28.80	20.88	24.48	16.20
H base (kN)	62	36	55	27	67	33	60	25	37	27	33	22
Displacement deviation with respect to NBR					9.0%	-7.8%	8.8%	-7.4%	-14.0%	8.5%	-14.1%	20.0%
Shear force deviation with respect to NBR					8.6%	-7.7%	8.8%	-7.2%	-39.9%	-24.7%	-39.9%	-15.5%

Table 10

Analysis results – DS

	NBR EFM		NBR RSM		ASCE EFM		ASCE RSM		EUROCODE EFM		EUROCODE RSM	
	Soil	Rock	Soil	Rock	Soil	Rock	Soil	Rock	Soil	Rock	Soil	Rock
Disp. (mm)	27.50	15.95	23.65	11.55	30.25	14.85	25.85	10.45	29.16	21.06	24.84	16.20
H base (kN)	23	15	21	13	25	15	23	13	25	19	22	16
Displacement deviation with respect to NBR					10.0%	-6.9%	9.3%	-9.5%	6.0%	32.0%	5.0%	40.3%
Shear force deviation in respect to NBR					8.5%	-4.1%	7.1%	-3.5%	6.4%	20.8%	5.3%	22.5%

Table 11

Compatibilized results RSM

	DC						DS					
	NBR		ASCE		EUROCODE		NBR		ASCE		EUROCODE	
	Soil	Rock	Soil	Rock	Soil	Rock	Soil	Rock	Soil	Rock	Soil	Rock
Disp. (mm)	28.5	13.5	34.6	16.7	24.5	16.2	23.7	11.6	28.7	12.1	24.8	16.2
H base (kN)	55	30	67	33	33	22	21	13	25	15	23	16
Displacement deviation			22%	24%	-14%	20%	-	-	21%	5%	5%	40%
Shear force deviation			21%	9%	-40%	-26%	-	-	19%	12%	5%	22%

stantially reduces the forces to be resisted at the base and consequently in the earthquake-resistant structural elements, although the displacements do not undergo such significant changes. The results also show that the foundation is a very influential variable in the responses of a seismic analysis, including the drifts obtained in the comparative analysis.

6. Special detailing for reinforced concrete structures

The earthquake-resistant detailing aims at ensuring structural deformability and ductility, since the plastic loading capacity of a structural system, within the scope of the Force Based Design (FBD), is superior to its resistance in the elastic regime. As presented in Fanella [18], the performance of the earthquake-resistant details, specified in the standards, was empirically guided and observed by elements in real situations. In other words, with empirical support, the standards state that the use of the specific patterns of detail suggested ensures that the structure will perform in a more ductile way when subjected to seismic loading, thus allowing for the adoption of more favorable response-modification coefficients. ABNT NBR 15421: 2006 [1] does not clarify in any way what are the criteria adopted for a structure to be considered as specially earthquake-resistant detailed. ASCE / SEI 7 [3] together with ACI 318 [9] and Eurocode 8 [2] present a number of additional considerations that must be followed to ensure adequate seismic performance for the structures. Some of these considerations are presented in what follows.

The elements, whenever possible, should be governed by bending, rather than by shear; the pillars must be stronger than the beams; and the joint regions between elements must have superior resistance to the elements themselves. It is also necessary to consider overloads, load inversion and impact.

The minimum required strength for the concrete is $f_{ck} = 20$ MPa, though some standards suggest that, for buildings with more than four floors, a $f_{ck} > 25$ MPa should be adopted; therefore, it should be ideally adopted f_{ck} higher than 25 MPa for any structure with special earthquake-resistance reinforcement detail.

For elements designed for pure bending (beams) where normal stress does not exceed $0.1 f_{ck}$, the following conditions must be met:

- $b > 0.3D$, where (b) and (D) are respectively the smallest and largest cross-sectional dimension;
- $b > 0.25cm$ (to ensure internal concrete confinement);
- $D < 25\%$ of span (to avoid wall-beam behavior);
- $b < 3C_2$ or $b < C_2 + 1.5C_1$ (where C_1 and C_2 are the longitudinal and transversal dimensions of the pillars, respectively);

$$■ A_{s,min} = 0.25 \frac{\sqrt{f_{ck}}}{f_{yk}} \times b \times D \geq 1.4 \frac{b \times D}{f_{yk}} \quad \text{where } b \text{ and } D$$

are given in centimeters; f_{ck} and f_{yk} in MPa (for the model building of this study the minimum reinforcement would be approximately twice the one adopted according to NBR 6118);

- Reinforcement ration $< 2.5\%$;
- $A_{s,inf}$ anchored at the bearing $> 0.5A_{s,sup}$ anchored at the bearing;
- Reinforcement in any region of the beam ($A_{s,min}$) shall not be less than 25% of the largest portion of required reinforcement ($A_{s,maior}$), according to the expression: $A_{s,min} > 25\% A_{s,maior}$.

For transverse reinforcement, the following minimum criteria must be adopted:

- Lap splice involved by stirrups of maximum spacing: $\frac{d}{4}$ or 10 cm (smallest value);
- Longitudinal rebar without a stirrup corner protection at a maximum distance of 15 cm from a protected rebar;
- Stirrups with 45° internal hooks and a straight end greater than: $6\Phi_t$ or 8 cm (the largest value), in which Φ_t is the stirrup diameter;
- In elements where the total normal stress is less than $0.05 f_{ck}$ and the portion of the shear stress derived from the seismic load is greater than 50% of the remainder shear force on the element, the element shall be designed by taking the shear portion absorbed by complementary mechanics to the truss model (V_c) equal to zero;
- The lap splices shall not be placed in regions of probable longitudinal reinforcement yield, that is to say, lap splices shall be avoided in the midspan or in regions as close to pillar intersections as twice the height of the beam, where plastic hinges are more likely to occur.
- The maximum spacing of the stirrups shall be: $\frac{1}{4}D$, $6\Phi_L$ or $\left(10 + \frac{35 - S_t}{3}\right)$ (in cm), where S_t is the transverse spacing of the stirrup section and Φ_L the longitudinal reinforcement diameter;
- The stirrups must be closed loops or at most, a "U" shaped stirrup with a hat complement, with a 45° internal hook at every connection;
- The first stirrup shall be at no more than 5cm from the face of the support.

For elements designed for compound bending (pillars) where the normal stress is greater than $0.1 f_{ck}$, the following conditions must be met:

- $b > 0.4D$ where (b) and (D) are respectively the smallest and largest cross-sectional dimension;
- $b > 30$ cm;
- The sum of the minimum moment applied to a pillar node shall be greater than 6/5 of the sum of the resistant moments of the beams composing the node (if this condition is not satisfied, the stiffness of the element shall be neglected in the seismic analysis);
- Amount of reinforcement adopted so that $1\% < A_s < 6\%$;
- Lap splice mandatorily at the element's midspan;
- Minimum stirrups diameters 10 mm;
- Hooks with a straight end greater than $6\Phi_t$ or 8cm (the greater value);
- Longitudinal rebar without a stirrup corner protection at a maximum distance of 15 cm from a protected rebar;
- Every other rebar must be protected by a stirrup corner;
- The cross sectional spacing of the stirrup shall be inferior to 35 cm;
- Reinforcement cover inferior to 10cm (when this criterion cannot be met, additional stirrups with no more than 30 cm spacing distance must be placed for cover protection);
- The pillar anchoring reinforcement must be integrally protected by the transversal reinforcement;
- Shear design considering $V_c = 0$ at regions with the following distances from the support: $2 \times$ greatest transversal dimension;

$$\frac{1}{6} \text{ span};$$

or 45 cm.

- The maximum spacing of the stirrups shall be: $\frac{1}{4}D$, $6\Phi_L$ or $\left(10 + \frac{35 - S_t}{3}\right)$ (in cm), where S_t is the transverse spacing of the stirrup section.

For corner joints:

- Admit yield stress = $1.25 f_{yk}$ (to ensure that the reinforcement will yield and form a plastic hinge);
- The anchoring must be extended to the end face of the column;
- Good adhesion anchorage = $2 \times ldh$, bad adhesion anchorage = $3.5 \times ldh$; where ldh is the anchoring length required for a hooked bar;
- Anchorage outside the containment should be multiplied by a factor of 1.6;
- For beams that end in columns, column dimension $> 20\Phi_L$ of beam;
- Pillar's transverse reinforcement must be placed across the entire node;
- Additionally, when the beam section is greater than the pillar's, the beam's transversal reinforcement must be placed across the entire node as well;
- Node shear stress must be inferior to (kN):

for nodes confined in all directions: $1.7\sqrt{f_{ck}} \times A_j$;

for nodes with a single open end: $1.2\sqrt{f_{ck}} \times A_j$;

for other cases: $1.0\sqrt{f_{ck}} \times A_j$.

where f_{ck} is given in MPa and A_j (in squared meter) determined by Figure 5.

An example of conventional detailing in comparison with a special earthquake-resistant detail suggested by the American standard can be seen in Figure 6. For the example, it was considered in a simplified way, the design of one of the beams of the model building presented in the study, with the following loads: self-weight; seismic loads; 3.5 kN/m^2 of permanent loads additionally to the self-weight; 5.0 kN/m^2 of accidental overload.

7. Conclusions

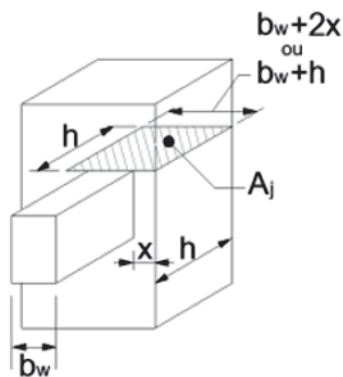


Figure 5

A_j in frame knot

Source: Galvão [10]

- 1) Although ABNT NBR 15421: 2006 [1] is based on an old American standard - UBC [7], it presents acceptable results for current seismic conditions in Brazil. However, in a globalized world and Brazil being so close to other regions of high seismicity in South America, a more complete standard with updated concepts, like a few discussed within this paper, would be more adequate.
- 2) The NBR gives a great focus on the implementation of the EFM; however, the application of an improved method (such as the RSM or non-linear analysis) could generate attractively more economical solutions, although the American standard does not allow very significant reductions in relation to the EFM.
- 3) The use of a specific seismic-resistant detail for regions of high seismicity generates a considerable decrease in the design stresses, through the response-modification coefficients, which can lead to economically more favorable situations, as shown in Table 9 and Table 10, in addition to being a more adequate detailing with respect to the safety and durability of the building. Despite this, NBR does not specify the details that characterize an acceptable earthquake-resistant project, in a way that forces one to seek references in international standards.
- 4) For the model building analyzed, the compared results were quite different amongst the standards. The parameters used to define the design spectra and consequently the acting forces are quite different, besides the limitations imposed by each standard and the weighting coefficients. Nevertheless, the results have the same order of magnitude and are, therefore, suitable for what they are proposed.
- 5) Although the RSM does not always produce more favorable results than the EFM, the use of three-dimensional models and more accurate procedures make it possible to precisely capture imperfections and irregularities in the structures, which generally returns more accurate results. New case studies should be studied in order to represent a greater variety of systems and structural arrangements, allowing to better understand the divergences and similarities among the responses of the methods analyzed for each normative instruction.

8. Acknowledgments

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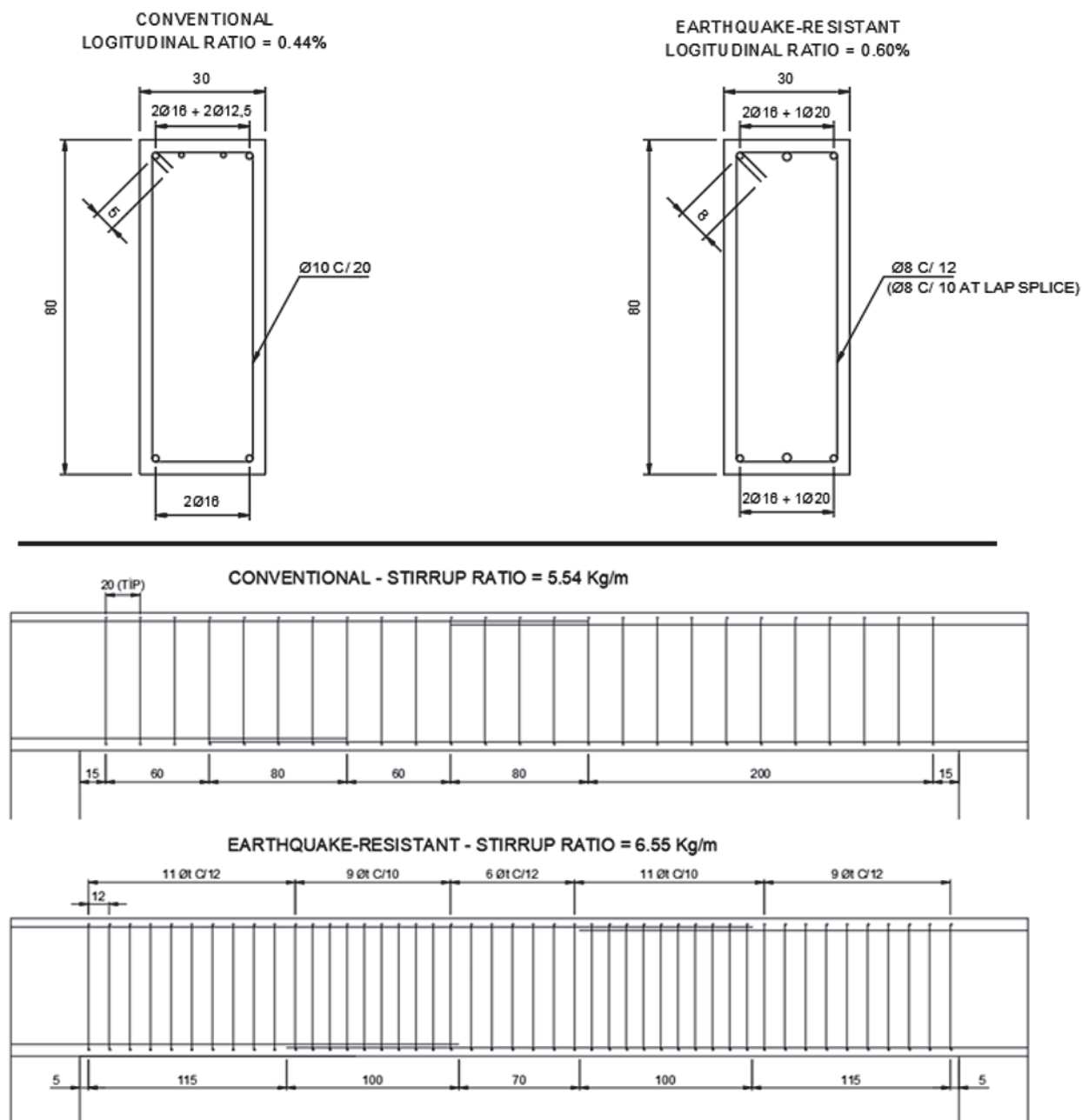


Figure 6
Comparison between conventional detailing and seismic special detailing

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